

The basic principles, main methods and all the formulas in physical geodesy and Earth gravity field have been realized completely in PAGravf4.5 to popularize higher education.

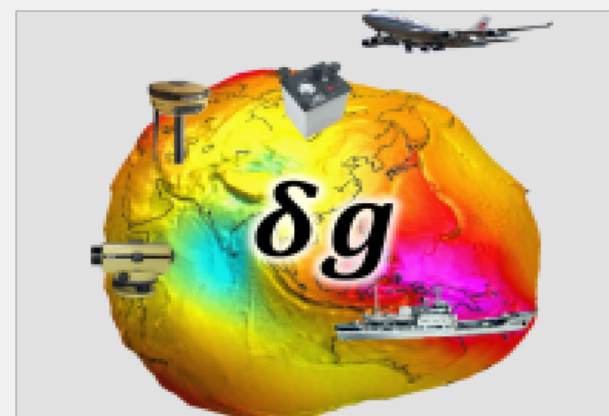
Program Examples for Precise Approach of Earth Gravity Field and Geoid

- **Cross aliasing of heterogeneous observations in land-sea-space**
- **Various terrain effects on all-element gravity field in whole space**
- **Loop closed analytical operations on outer gravity field elements**
- **All-element modeling on Earth gravity field in whole outer space**
- **Index measurement of observation errors and computation control**
- **Gravity prospecting modelling from heterogeneous observations**

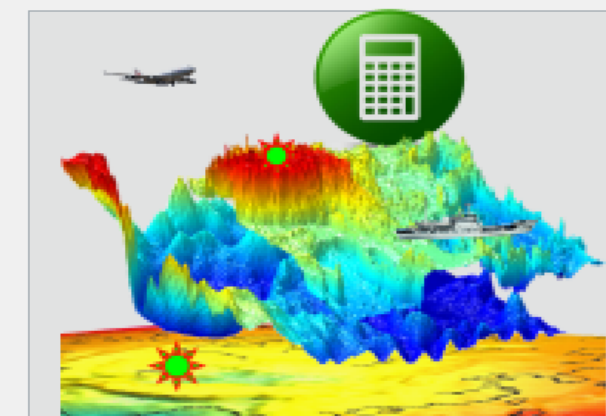
Classroom Teaching Self-Exercise Science Research Engineer Computing



Summary, parameter settings and visualization for PAGravf4.5



Data analysis and preprocessing calculation of Earth gravity field



Computation of various terrain effects on various field elements outside geoid

☆ The basic principles, main methods and all the formulas in physical geodesy and Earth gravity field have been realized completely in PAGravf4.5 to improve high education environment.


☆ Many long-term puzzles such as various terrain effects on various observations, all-element analytical modelling on gravity field, fine gravity prospecting modelling from heterogeneous observations, external accuracy index measurement and computational performance control have been effectively solved to strengthen the application capacity of Earth gravity field.


www.zcyphygeodesy.com/en/

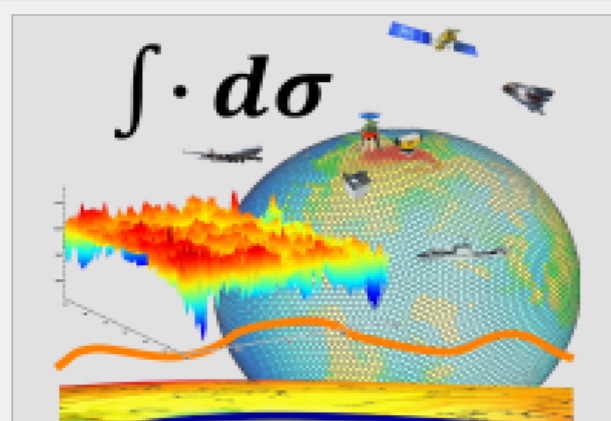


☆ PAGravf4.5 is suitable for senior under-graduates, graduate students, scientific researchers, and engineer technicians in geodesy and geophysics, geology and geoscience, geomatics and geographic information, seismic and geodynamics.

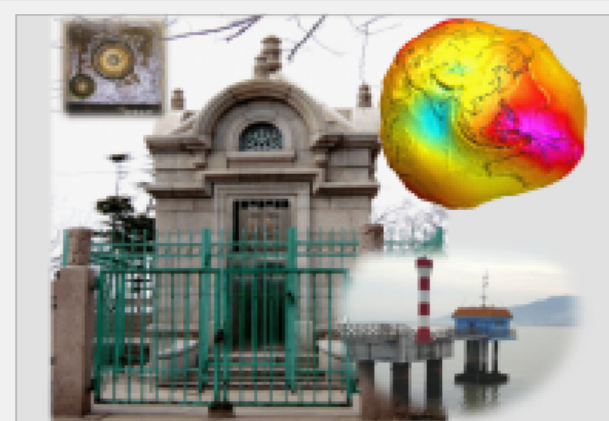
☆ There are the example files saved in the folder C:\PAGravf4.5_win64en\examples for each program, which includes the operation process file process.txt, some input-output data files and screenshots. It will take about 5 working days to complete all the example exercises. Thereafter, you can use PAGravf4.5 alone.

 PAGravf4.5 scientific computation programs organization structure

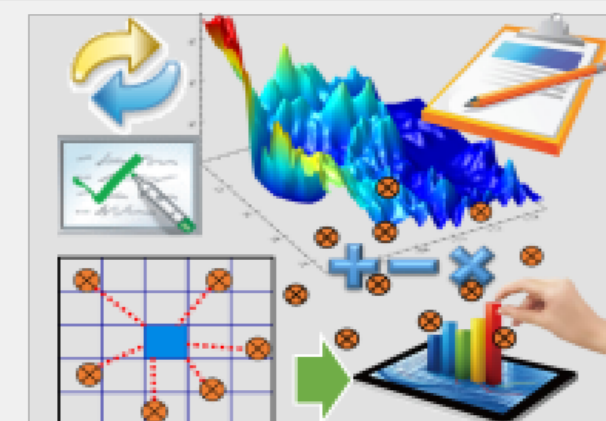
 Geodetic data format and geodetic quantity convention in PAGravf4.5



Precise approach and all-element modeling on Earth gravity field








Optimization, unification, and application for regional height datum



Editing and calculation tools for geodetic data files

Classroom Teaching, Self-Exercise, Science Research and Engineer Computing

-  Cross aliasing of heterogeneous observations in land-sea-space
-  Loop closed analytical operations on outer gravity field elements
-  Index measurement of observation errors and computation control

-  Various terrain effects on all-element gravity field in whole space
-  All-element modeling on Earth gravity field in whole outer space
-  Gravity prospecting modelling from heterogeneous observations

Calculation of normal Earth gravity field, ellipsoid constants and Wg analysis

Calculation of global geopotential model and its spectral character analysis

Calculation of observed anomalous field element and error analysis of geoid

Correction of boundary value problem for gravity field element on non-equipotential surface

Analytical continuation of anomalous field elements using multi-order radial gradient

Gross error detection and basis function gridding of discrete field elements

External height anomaly computation using Stokes/Hotine integral

External vertical deflection computation using Vening-Meinesz integral

Inverse integral and integral of inverse operation on anomalous field element

Gradient and Poisson integral of external gravity field element

Feature and performance analysis of spherical radial basis functions

Gravity field approach using SRBFs in spectral domain and performance test

All-element modelling on gravity field using SRBFs from heterogeneous observations

Modeling process exercise of regional gravity field and geoid

Converting of general ASCII records into PAGravf4.5 format

Data interpolation, extracting and separation of land and sea

Simple and direct calculation on geodetic data files

Low-pass filtering operation on geodetic grid file

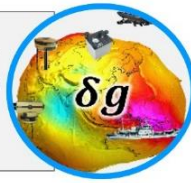
Simple gridding and regional geodetic grid construction

Constructing and transforming of vector grid file

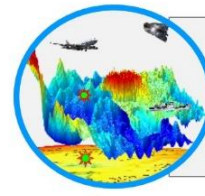
Statistical analysis on various geodetic data file

Calculation of grid horizontal gradient and vector grid inner product

Data analysis and pre-processing calculation of the Earth gravity field



Computation of various terrain effects on various field elements outside geoid



Computation of local terrain effect on various field elements on or outside the geoid

Computation of land, ocean, and lake complete Bouguer effect on gravity outside geoid

Computation of terrain Helmert condensation effect on various field elements outside geoid

Computation of residual terrain effect on various field elements outside geoid

Computation of land-sea unified classical gravity Bouguer / equilibrium effect

Ultrahigh degree spherical harmonic analysis on land-sea terrain and construction of model

Spherical harmonic synthesis of complete Bouguer or residual terrain effects

Computation process demo of various terrain effects outside geoid

Precise approach and full element modelling on Earth gravity field



Precise Approach of Earth Gravity Field and Geoid

PAGravf4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Optimization, unification, and application for regional height datum

Calculation of height difference correction of height anomaly and height system difference

Construction and refinement of equipotential surface passing through specified point

Construction of terrain equiheight surface passing through specified point

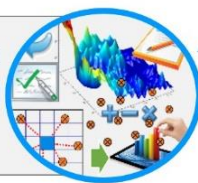
Assessment of gravimetric geoid using GNSS-levelling data

GNSS-levelling data fusion and regional height datum optimization

GNSS replaces leveling to calculate the orthometric or normal height

Editing, calculation and visualization for geodetic data files

Geodetic data files edit and calculation tool



PAGravf4.5 Summary, Setting and visualization

PAGravf4.5 Goals, Features and strengths

Dominant concepts and ideas in PAGravf4.5

Algorithm features and use notes of PAGravf4.5

PAGravf4.5 Parameter settings

Visualization of multi-attribute curves from 2D geodetic data

Visualization for specified attribute in discrete point record file

Visualization for the geodetic grid file

Visualization for the geodetic vector grid file

Computation of normal Earth gravity field elements of the Earth space point

Calculation of Earth ellipsoid constants and geopotential W_g analysis

Calculation of anomalous field elements at observed points

Statistical error estimation of regional gravimetric geoid

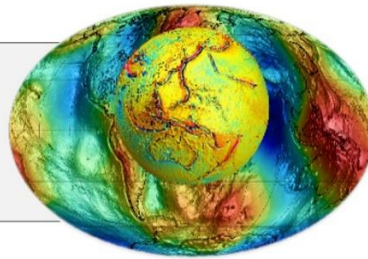
Calculation of influence of gravity system bias on gravimetric geoid

Gross error detection on observations based on low-pass reference surface

Estimation of observation weight with specified reference attribute

Gridding of heterogeneous data by basis function weighted interpolation

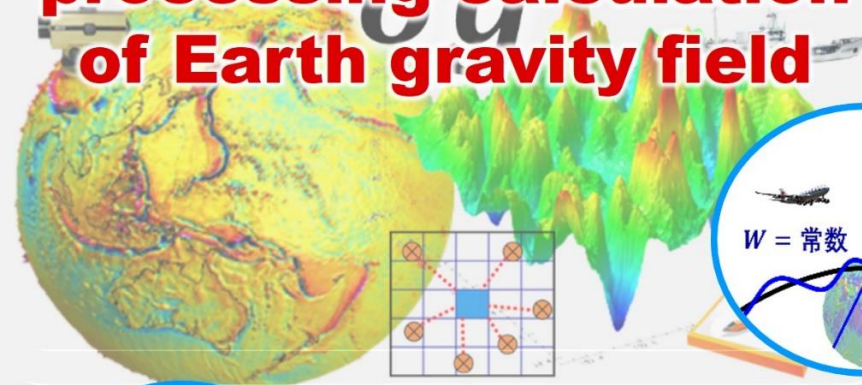
Calculation of normal Earth gravity field, ellipsoid constants and W_g analysis



Calculation of observed anomalous field element and error analysis of geoid

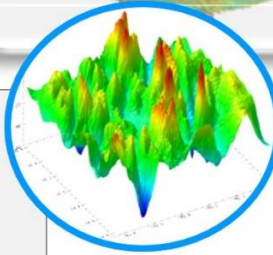


Data analysis and pre-processing calculation of Earth gravity field



Correction of boundary value problem for field element on non-equipotential surface

Gross error detection and basis function gridding of discrete gravity field elements



Analytical continuation of anomalous field elements using multi-order radial gradient



Calculation of gravity field elements from global geopotential model



Calculation of model value for residual terrain (complete Bouguer) effects

Global geopotential coefficient model Calculator

Calculation and analysis of spectral character of Earth's gravity field

Correction calculation of boundary value for spherical or ellipsoidal boundary surface

Molodensky boundary value correction for arbitrary shape boundary surface

Computation of normal Earth gravity field elements of the Earth space point

Precise Approach of Earth Gravity Field and Geoid

PAGrav4.5

Calculation formulas of normal gravity field
Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Computation of normal Earth gravity field elements of the Earth space point

Calculation of Earth ellipsoid constants and geopotential Wg analysis

Save computation process as

Open space calculation point file

Set input point file format

Number of rows of file header

Column ordinal number of ellipsoidal height in the record

- Select elements to be calculated
- Normal geopotential (m²/s²)
 - Normal gravity (mGal)
 - Normal gravity gradient (E)
 - Normal gravity line direction (')
 - Normal gravity gradient direction (')

Save the results as

Import setting parameters

Start Computation

>> Computation Process ** Operation Prompts

>> [Purpose] Calculate the normal gravity field elements at the Earth space point, geometrical and physical constants of the normal Earth ellipsoid and geoidal geopotential Wg according to the rigorous analytical algorithm of spherical harmonic expansion.

>> Select the computation function from the two control buttons on the left-top of the interface...

>> [Function] Using the spherical harmonic expansion formula, calculate the normal geopotential (m²/s²), normal gravity (mGal), normal gravity gradient (E), normal gravity line direction ('), expressed by its north declination relative to the Earth center of mass) or normal gravity gradient direction ('), expressed by its north declination relative to the Earth center of mass).

** Click on the control button [Open space calculation point file] or the tool button [Open calculation points] ...

>> Open calculation point file C:/PAGrav4.5_win64en/examples/PrNormalgravfdcalc/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters, select the elements to be calculated, and click the [Import setting parameters] button to input the parameters into the system...

>> Save the calculation result file as C:/PAGrav4.5_win64en/examples/PrNormalgravfdcalc/result.txt.

** Behind the record of the calculation point file, appends one or several columns of normal gravity field element calculation values, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-21 12:01:17

>> Complete the computation of the normal gravity field parameters!

>> Computation end time: 2024-09-21 12:01:18

Display of the input-output file↓

no	lon(deg)	lat(deg)	ellipheight(m)						
3248	103.671939	31.938051	2743.9394	62609994.0026	978633.0022	3074.9063	-10.3533	5.1183	
3249	103.696944	31.864721	2501.2449	62612369.3305	978701.8741	3075.2510	-10.3399	5.1446	
3250	103.718330	31.831114	2435.4206	62613013.6271	978719.4456	3075.3432	-10.3339	5.1567	
3251	103.735559	31.795280	2366.5700	62613687.5573	978737.7722	3075.4395	-10.3273	5.1696	
3252	103.777216	31.776390	2294.0304	62614397.5729	978758.6092	3075.5429	-10.3239	5.1764	
3253	103.822773	31.758333	2233.2317	62614992.6837	978775.8948	3075.6293	-10.3206	5.1828	
3254	103.849717	31.724168	2215.6606	62615164.7271	978778.5505	3075.6515	-10.3144	5.1951	
3255	103.816666	31.650003	2242.9951	62614897.3184	978764.1322	3075.6047	-10.3009	5.2217	
3256	103.783335	31.616667	2297.3654	62614365.2277	978744.6783	3075.5227	-10.2949	5.2337	
3257	103.740556	31.581110	2218.6104	62615136.1113	978766.0935	3075.6335	-10.2883	5.2464	
3258	103.703884	31.560833	2207.1173	62615248.6381	978768.0029	3075.6482	-10.2846	5.2537	
3259	103.682782	31.531391	2245.2634	62614875.3318	978753.8691	3075.5901	-10.2793	5.2643	

Save data in the text box as

The geoidal geopotential Wg is always equal to the normal geopotential U₀ of the normal ellipsoid. PAGrav4.5 suggests that the geoidal geopotential Wg should replace the appoint empirical W₀ in the IERS numerical standard. The latter is calculated from the global geopotential model and mean sea surface height model according to the Gaussian geoid appoint.

Set four basic parameters of Earth ellipsoid

Geocentric gravitational constant $GM(10^{14}m^2/s^3)$ of the Earth Mean angular velocity $\omega(10^{-5}/s)$ of the Earth

Select the fourth basic parameter from $\bar{C}_{20}(10^{-3})$, $J_2(10^{-3})$, $1/f$ and U_0

Geometric derived constants of Earth ellipsoid

Reciprocal flattening $1/f$

Minor semi axis of the Earth $b(m)$

Radius of sphere of same volume $R(m)$

Linear eccentricity $E(m)$

Square of first eccentricity e^2

Square of second eccentricity e'^2

Equatorial curvature radius $M(m)$

Polar radius of curvature $c(m)$

Physical derived constants of Earth ellipsoid

Dynamic form factor J_2 Normal potential at ellipsoid $U_0=Wg(m^2/s^2)$

Geodetic parameter m Normal gravity at equator $g_a(m/s^2)$

>> Computation Process ** Operation Prompts

>> [Function] From four basic parameters of the Earth ellipsoid, calculate the main geometric constants of the Earth ellipsoid. This function can be used for classroom teaching demonstrations.

** The fourth basic parameter can be selected from the second-degree zonal harmonic coefficient \bar{C}_{20} from global geopotential model, reciprocal $1/f$ of the ellipsoid flattening, and the ellipsoid normal geopotential U_0 .

** The coefficient \bar{C}_{20} from global geopotential model is selected currently as the fourth basic parameter.

>> The four basic parameters of the Earth ellipsoid have been entered into the system!

** Click the [Calculation of the derived constants of Earth ellipsoid] control button, or the [Calculation of ellipsoid constants] tool button...

The tide system of the normal ellipsoid is consistent with \bar{C}_{20} or J_2 .

PAGrav4.5 suggests that the scale parameters (GM, a) of global geopotential model, second-degree zonal harmonic coefficient \bar{C}_{20} and the mean rotation angular velocity ω should be employed as the four basic parameters of the normal ellipsoid. Using such a normal ellipsoid as the reference datum, the second-degree zonal harmonic term of anomalous gravity field is always zero, which is beneficial to improve the performance of the gravity field approach.

Calculation of Earth ellipsoid constant and geopotential Wg analysis

Set four basic parameters of Earth ellipsoid

Geocentric gravitational constant $GM(10^{14}m^2/s^3)$ of the Earth Mean angular velocity $\omega(10^{-5}/s)$ of the Earth Major semi axis $a(m)$ of the Earth

Select the fourth basic parameter from $\bar{C}_{20}(10^{-3})$, $J_2(10^{-3})$, $1/f$ and U_0

Geometric derived constants of Earth ellipsoid

Reciprocal flattening $1/f$

Minor semi axis of the Earth $b(m)$

Radius of sphere of same volume $R(m)$

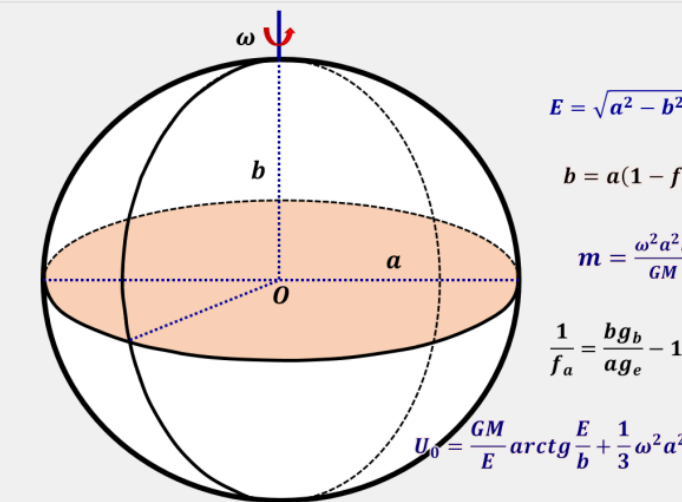
Linear eccentricity $E(m)$

Square of first eccentricity e^2

Square of second eccentricity e'^2

Equatorial curvature radius $M(m)$

Polar radius of curvature $c(m)$



Physical derived constants of Earth ellipsoid

Dynamic form factor J_2 Normal potential at ellipsoid $U_0=Wg(m^2/s^2)$ Gravity flattening reciprocal $1/f_a$

Geodetic parameter m Normal gravity at equator $g_a(m/s^2)$ Normal gravity at pole $g_p(m/s^2)$

>> Computation Process ** Operation Prompts

>> [Function] From four basic parameters of the Earth ellipsoid, calculate the main geometric and physical derived constants of the Earth ellipsoid. This function can be used for classroom teaching demonstrations.

** The fourth basic parameter can be selected from the second-degree zonal harmonic coefficient \bar{C}_{20} from global geopotential model, dynamic form factor J_2 , reciprocal $1/f$ of the ellipsoid flattening, and the ellipsoid normal geopotential U_0 .

** The coefficient \bar{C}_{20} from global geopotential model is selected currently as the fourth basic parameter.

>> The four basic parameters of the Earth ellipsoid have been entered into the system!

** Click the [Calculation of the derived constants of Earth ellipsoid] control button, or the [Calculation of ellipsoid constants] tool button...

>> Complete the calculation of the main geometric and physical derived constants of the Earth ellipsoid!

>> Summary of the calculation results of the Earth ellipsoid constants (see the interface for units):

Geocentric gravitational constant of the Earth (including the atmosphere) $GM = 3.986004415$
 Major semi axis of the Earth $a = 6378136.3000$
 Dynamical form factor of the Earth $J_2 = 1.0826261739$
 Mean angular velocity of the Earth $\omega = 7.292115$
 Reciprocal flattening $1/f = 298.2577612334$
 Minor semi axis of the Earth $b = 6356751.6551$
 Radius of sphere of same volume $R = 6371000.1037$
 Linear eccentricity $E = 521853.4816$
 Square of first eccentricity $e^2 = 0.006694367942422894$
 Square of second eccentricity $e'^2 = 0.006739333137719190$
 Equatorial curvature radius $M = 6335438.7088$
 Polar radius of curvature $c = 6399592.8846$
 Normal potential at ellipsoid $U_0 = 62636858.3919$
 Gravity flattening reciprocal $1/f_a = 517.6353224813$
 Geodetic parameter $m = 0.0034497853945$
 Normal gravity at equator $g_a = 9.7803274325$
 Normal gravity at pole $g_p = 9.8321870775$

PAGrav4.5 suggests that the scale parameters (GM, a) of global geopotential model, second-degree zonal harmonic coefficient \bar{C}_{20} and the mean rotation angular velocity ω should be employed as the four basic parameters of the normal ellipsoid. Using such a normal ellipsoid as the reference datum, the second-degree zonal harmonic term of anomalous gravity field is always zero, which is beneficial to improve the performance of the gravity field approach.

Set four basic parameters of Earth ellipsoid

Geocentric gravitational constant GM(10¹⁴m²/s³) of the Earth Mean angular velocity ω(10⁻⁵/s) of the Earth

Select the fourth basic parameter from $\bar{C}_{20}(10^{-3})$, $J_2(10^{-3})$, $1/f$ and U_0

Enter the four basic parameters of Earth ellipsoid

Geometric derived constants of Earth ellipsoid

Reciprocal flattening 1/f

Minor semi axis of the Earth b(m)

Radius of sphere of same volume R(m)

Linear eccentricity E(m)

Square of first eccentricity e²

Square of second eccentricity e'²

Equatorial curvature radius M(m)

Polar radius of curvature c(m)

Physical derived constants of Earth ellipsoid

Dynamic form factor J₂ Normal potential at ellipsoid U₀=Wg(m²/s²)

Geodetic parameter m Normal gravity at equator g_a(m/s²)

>> Computation Process ** Operation Prompts

Polar radius of curvature c = 6399592.8846
 Normal potential at ellipsoid U₀ = 62636858.3919
 Gravity flattening reciprocal 1/f_a = 517.6353224813
 Geodetic parameter m = 0.0034497853945
 Normal gravity at equator g_a = 9.7803274325
 Normal gravity at pole g_p = 9.8321870775

>> The reciprocal 1/f of the ellipsoid flattening selected as the fourth basic parameter.
 >> The four basic parameters of the Earth ellipsoid have been entered into the system!
 ** Click the [Calculation of the derived constants of Earth ellipsoid] control button, or the [Calculation of ellipsoid constants] tool button...

>> Complete the calculation of the main geometric and physical derived constants of the Earth ellipsoid!
 >> Summary of the calculation results of the Earth ellipsoid constants (see the interface for units):
 Geocentric gravitational constant of the Earth (including the atmosphere) GM = 3.986004415
 Major semi axis of the Earth a = 6378136.3000
 Dynamical form factor of the Earth J₂ = 1.0826261739
 Mean angular velocity of the Earth ω = 7.292115
 Reciprocal flattening 1/f = 298.2577612300
 Minor semi axis of the Earth b = 6356751.6551
 Radius of sphere of same volume R = 6371000.1037
 Linear eccentricity E = 521853.4816
 Square of first eccentricity e² = 0.006694367942498012
 Square of second eccentricity e'² = 0.006739333137795320
 Equatorial curvature radius M = 6335438.7088
 Polar radius of curvature c = 6399592.8846
 Normal potential at ellipsoid U₀ = 62636858.3919
 Gravity flattening reciprocal 1/f_a = 517.6353225016
 Geodetic parameter m = 0.0034497853945
 Normal gravity at equator g_a = 9.7803274325
 Normal gravity at pole g_p = 9.8321870775

PAGrav4.5 suggests that the scale parameters (GM, a) of global geopotential model, second-degree zonal harmonic coefficient \bar{C}_{20} and the mean rotation angular velocity ω should be employed as the four basic parameters of the normal ellipsoid. Using such a normal ellipsoid as the reference datum, the second-degree zonal harmonic term of anomalous gravity field is always zero, which is beneficial to improve the performance of the gravity field approach.

Calculation of Earth ellipsoid constant and geopotential Wg analysis

Set four basic parameters of Earth ellipsoid

Geocentric gravitational constant GM(10¹⁴m²/s³) of the Earth Mean angular velocity ω(10⁻⁵/s) of the Earth Major semi axis a(m) of the Earth

Select the fourth basic parameter from $\bar{C}_{20}(10^{-3})$, $J_2(10^{-3})$, $1/f$ and U_0

Enter the four basic parameters of Earth ellipsoid

Calculation of the derived constants of Earth ellipsoid

Geometric derived constants of Earth ellipsoid

Reciprocal flattening 1/f

Minor semi axis of the Earth b(m)

Radius of sphere of same volume R(m)

Linear eccentricity E(m)

Square of first eccentricity e²

Square of second eccentricity e'²

Equatorial curvature radius M(m)

Polar radius of curvature c(m)

Physical derived constants of Earth ellipsoid

Dynamic form factor J₂ Normal potential at ellipsoid U₀=Wg(m²/s²) Gravity flattening reciprocal 1/f_a

Geodetic parameter m Normal gravity at equator g_a(m/s²) Normal gravity at pole g_p(m/s²)

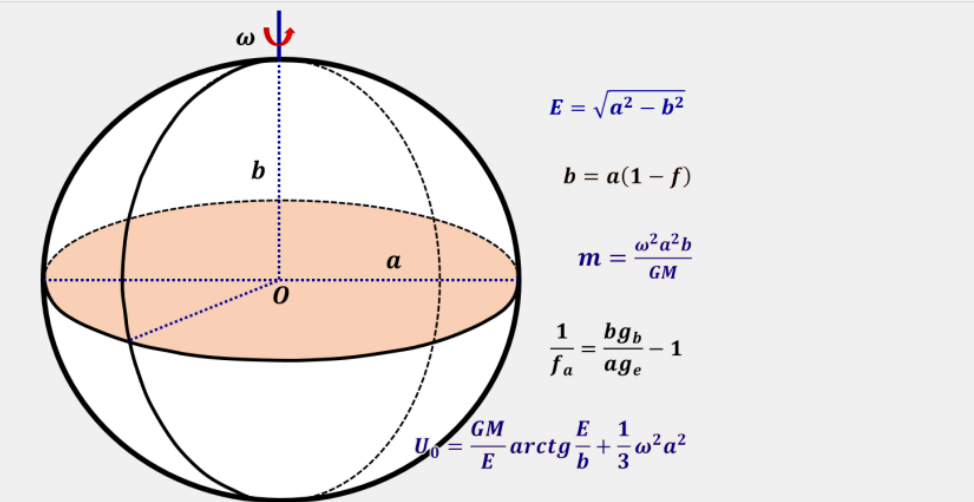
>> Computation Process ** Operation Prompts

Polar radius of curvature c = 6399592.8846
 Normal potential at ellipsoid U₀ = 62636858.3919
 Gravity flattening reciprocal 1/f_a = 517.6353225016
 Geodetic parameter m = 0.0034497853945
 Normal gravity at equator g_a = 9.7803274325
 Normal gravity at pole g_p = 9.8321870775

>> The ellipsoid normal geopotential U₀ selected as the fourth basic parameter.
 >> The four basic parameters of the Earth ellipsoid have been entered into the system!
 ** Click the [Calculation of the derived constants of Earth ellipsoid] control button, or the [Calculation of ellipsoid constants] tool button...

>> Complete the calculation of the main geometric and physical derived constants of the Earth ellipsoid!
 >> Summary of the calculation results of the Earth ellipsoid constants (see the interface for units):
 Geocentric gravitational constant of the Earth (including the atmosphere) GM = 3.986004415
 Major semi axis of the Earth a = 6378136.3000
 Dynamical form factor of the Earth J₂ = 1.0826362774
 Mean angular velocity of the Earth ω = 7.292115
 Reciprocal flattening 1/f = 298.2564115287
 Minor semi axis of the Earth b = 6356751.5584
 Radius of sphere of same volume R = 6371000.0713
 Linear eccentricity E = 521854.6604
 Square of first eccentricity e² = 0.006694398185685759
 Square of second eccentricity e'² = 0.006739363787946455
 Equatorial curvature radius M = 6335438.5159
 Polar radius of curvature c = 6399592.9820
 Normal potential at ellipsoid U₀ = 62636858.3919
 Gravity flattening reciprocal 1/f_a = 517.6435137497
 Geodetic parameter m = 0.0034497853420
 Normal gravity at equator g_a = 9.7803275820
 Normal gravity at pole g_p = 9.8321870774

PAGrav4.5 suggests that the scale parameters (GM, a) of global geopotential model, second-degree zonal harmonic coefficient \bar{C}_{20} and the mean rotation angular velocity ω should be employed as the four basic parameters of the normal ellipsoid. Using such a normal ellipsoid as the reference datum, the second-degree zonal harmonic term of anomalous gravity field is always zero, which is beneficial to improve the performance of the gravity field approach.



The tide system of the normal ellipsoid is consistent with \bar{C}_{20} or J_2 .

Calculation of gravity field elements from global geopotential model

Precise Approach of Earth Gravity Field and Geoid
PAGravf4.5

Algorithmic Formulas
Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Calculation of gravity field elements from global geopotential model

Calculation of model value for residual terrain (complete Bouguer) effects

Global geopotential coefficient model Calculator

Calculation and analysis of spectral character of Earth's gravity field

Open global geopotential coefficient model file

Select calculation file format
Discrete calculation point file

Open space calculation point file

Set input point file format

Number of rows of file header 1
Column ordinal number of ellipsoidal height in the record 4

- Select elements to be calculated
- height anomaly (m)
 - gravity anomaly (mGal)
 - gravity disturbance (mGal)
 - vertical deflection (" , SW)
 - disturbing gravity gradient (E, radial)
 - tangential gravity gradient (E, NW)
 - Laplace operator (E)

Minimum degree 2
Maximum degree 360

Extract elements to be plot Plot↓

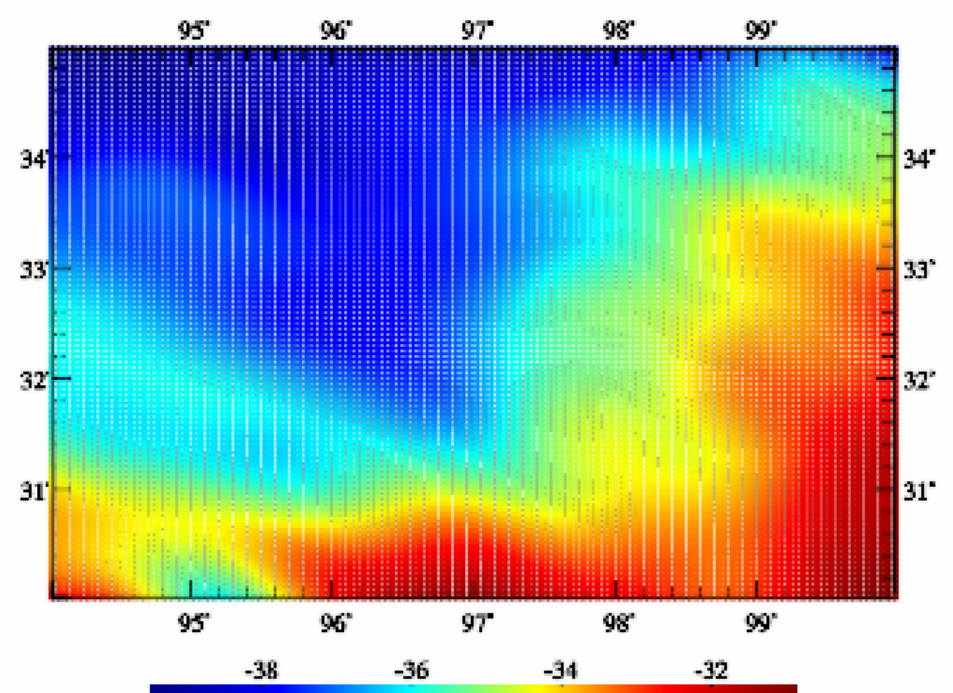
Save computation process as

```
>> [Function] From global geopotential coefficient model, calculate the model value of the (residual) height anomaly (m), gravity anomaly (mGal), gravity disturbance (mGal), vertical deflection vector (" , south, west), disturbing gravity gradient (E, radial), tangential gravity gradient vector (E, north, west) or Laplace operator (E).
** Click the [Open global geopotential coefficient model file] control button, or the [Open geopotential model] tool button...
>> Open global geopotential coefficient model file C:/PAGravf4.5_win64en/data/EGM2008.gfc.
** The window below only shows the geopotential coefficients data with no more than 2000 rows in it.
>> Open space calculation point file C:/PAGravf4.5_win64en/examples/PrModelgravfdcalc/calcpnt.txt.
** Look at the file information in the window below and set the discrete point file format...
>> Save the results as C:/PAGravf4.5_win64en/examples/PrModelgravfdcalc/result.txt.
** Behind the record of the calculation point file, appends one or more columns of model values of anomalous field elements, and keeps 4 significant figures.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
** The calculation process need wait, during which you can open the output file to look at the calculation progress...
>> Computation start time: 2024-09-21 12:50:51
```

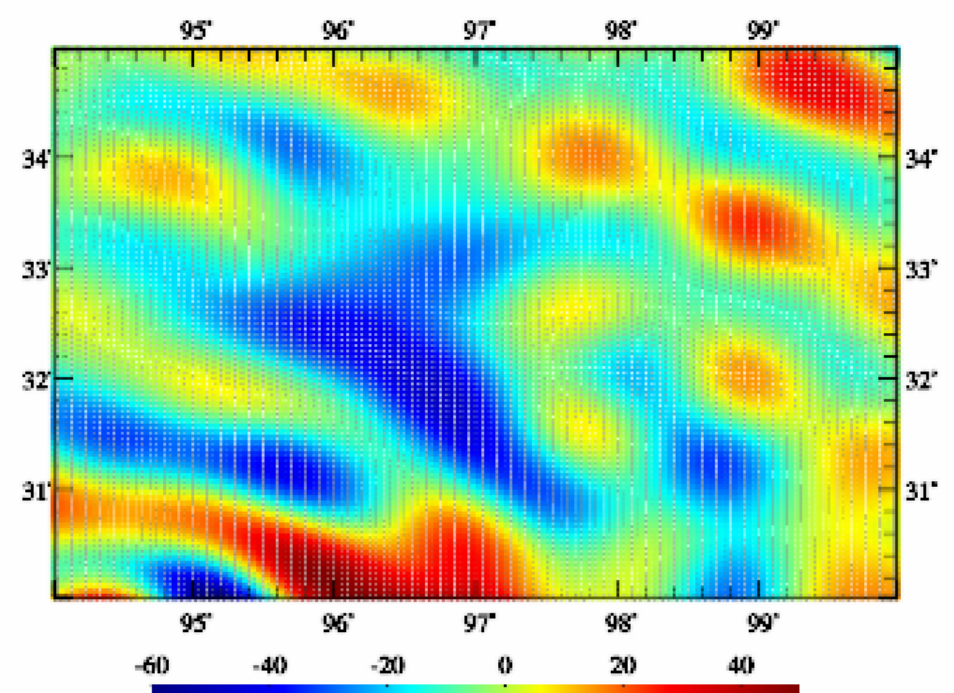
Save the results as Import setting parameters

Start Computation

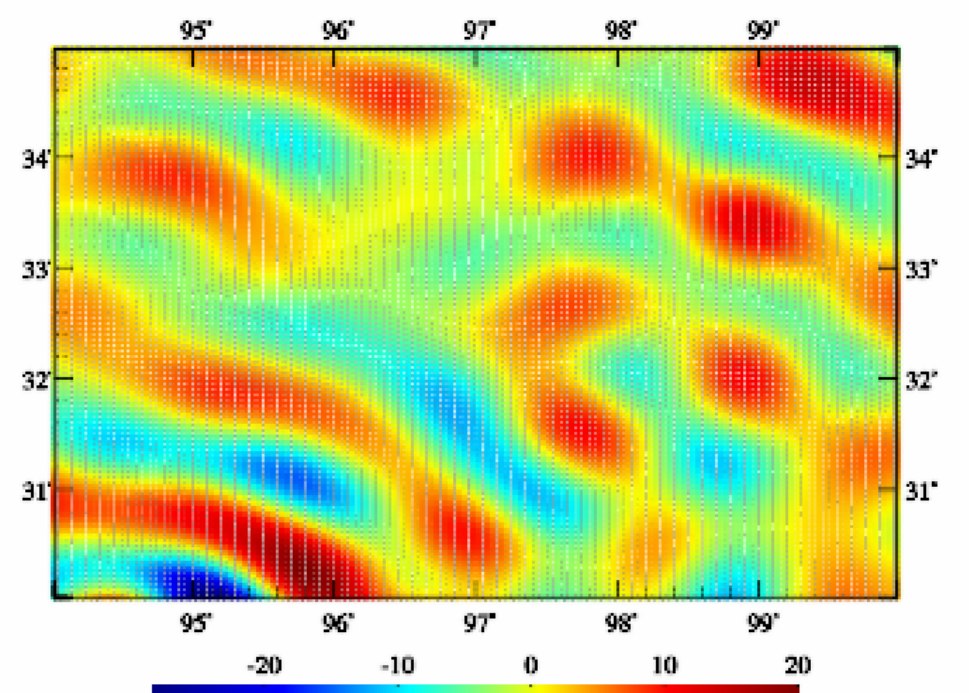
no	lon(deg)	lat(deg)	ellipheight(m)				
1	94.025000	30.025000	3984.353	-32.5696	9.9303	-7.0197	
2	94.075000	30.025000	4226.989	-32.5825	13.2926	-5.1102	
3	94.125000	30.025000	4461.719	-32.6027	16.5996	-3.1215	
4	94.175000	30.025000	4422.914	-32.6266	19.5823	-1.2269	
5	94.225000	30.025000	4335.893	-32.6637	22.1364	0.5431	
6	94.275000	30.025000	4463.689	-32.7271	23.9898	2.0700	



height anomaly (m)



gravity disturbance (mGal)



disturbing gradient (E, R)

When the minimum and maximum degree n to be set is equal, the program calculates the contribution of the degree n geopotential coefficients to the anomalous gravity field element, which can be employed to analyze and evaluate the spectral and space properties of the geopotential coefficient model.

Calculation of gravity field elements from global geopotential model

Precise Approach of Earth Gravity Field and Geoid PAgGrav4.5

Algorithmic Formulas
Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Calculation of gravity field elements from global geopotential model

Calculation of model value for residual terrain (complete Bouguer) effects

Global geopotential coefficient model Calculator

Calculation and analysis of spectral character of Earth's gravity field

Open global geopotential coefficient model file

Select calculation file format
Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

- Select elements to be calculated
- height anomaly (m)
 - gravity anomaly (mGal)
 - gravity disturbance (mGal)
 - vertical deflection (", SW)
 - disturbing gravity gradient (E, radial)
 - tangential gravity gradient (E, NW)
 - Laplace operator (E)

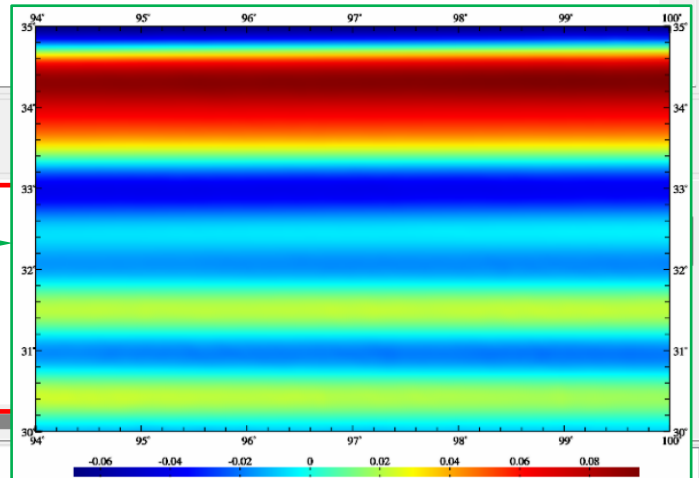
Minimum degree 2
Maximum degree 360

Save computation process as

>> [Function] From global geopotential coefficient model, calculate the model value of the (residual) height anomaly (m), gravity anomaly (mGal), gravity disturbance (mGal), vertical deflection vector (", south, west), disturbing gravity gradient (E, radial), tangential gravity gradient vector (E, north, west) or Laplace operator (E).
 ** Click the [Open global geopotential coefficient model file] control button, or the [Open geopotential model] tool button...
 >> Open global geopotential coefficient model file C:/PAGrav4.5_win64en/data/EGM2008.gfc.
 ** The window below only shows the geopotential coefficients data with no more than 2000 rows in it.
 >> Open ellipsoidal height grid file of calculation surface C:/PAGrav4.5_win64en/examples/PrModelgravfdcalc/surfhgt.dat.
 >> Save the results as C:/PAGrav4.5_win64en/examples/PrModelgravfdcalc/Gravfd360.txt.
 ** The record format: ID (point no/name), longitude, latitude, ellipsoidal height, several columns of the model values of anomalous field elements.
 ** The program also outputs (residual) height anomaly (*.ksi), gravity anomaly (*.gra), gravity disturbance (*.rga), vertical deflection vector (*.dft), disturbing gravity gradient (*.grr), tangential gravity gradient vector (*.hgd) or Laplace operator (*.lps) model value grid files into the current directory. Where * is the output file name entered in the interface, and the program outputs the corresponding (residual) model value grid file according to the selected gravity field element type.
 >> The parameter settings have been entered into the system!

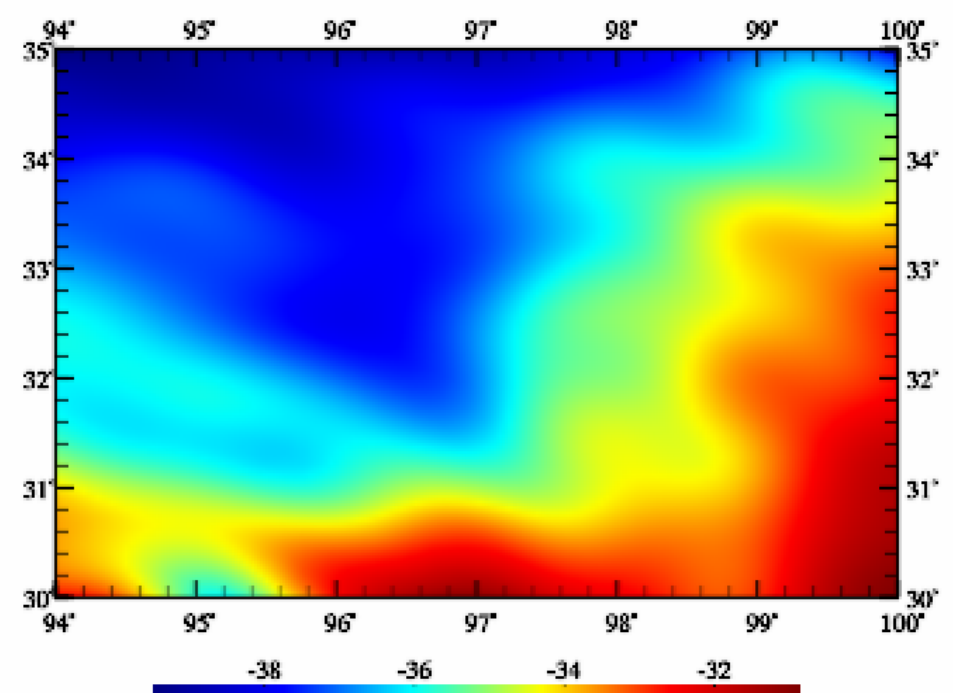
Save the results as Import setting parameters

1	94.02500	30.02500	3984.353	-32.5696	19.9216	9.9303
2	94.07500	30.02500	4226.989	-32.5825	23.2867	13.2926
3	94.12500	30.02500	4461.719	-32.6027	26.5988	16.5996
4	94.17500	30.02500	4422.914	-32.6266	29.5890	19.5823
5	94.22500	30.02500	4335.893	-32.6637	32.1549	22.1364
6	94.27500	30.02500	4463.689	-32.7271	34.0272	23.9898

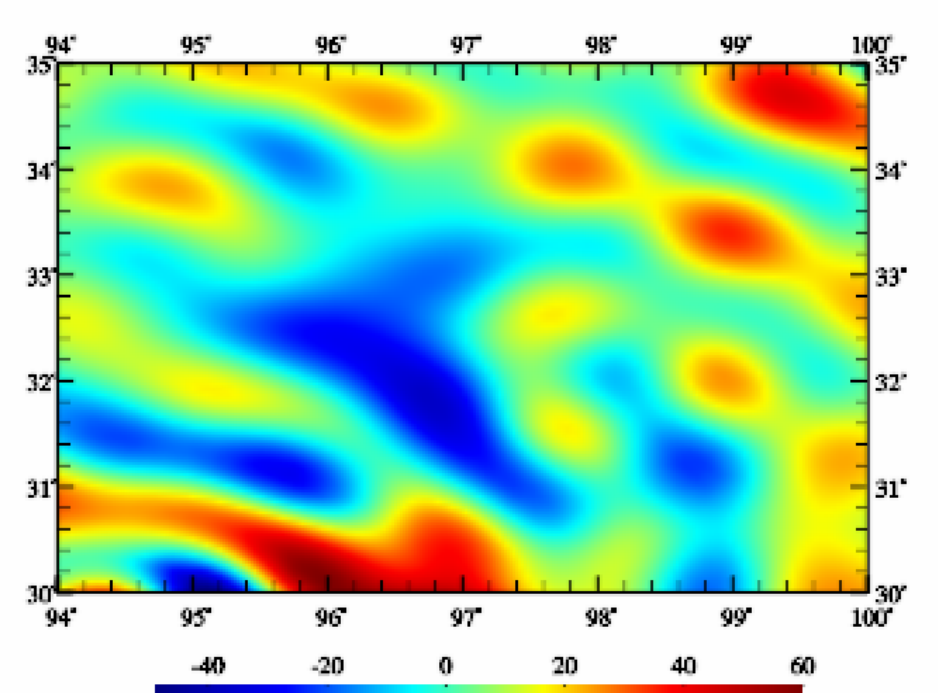


Extract elements to be plot

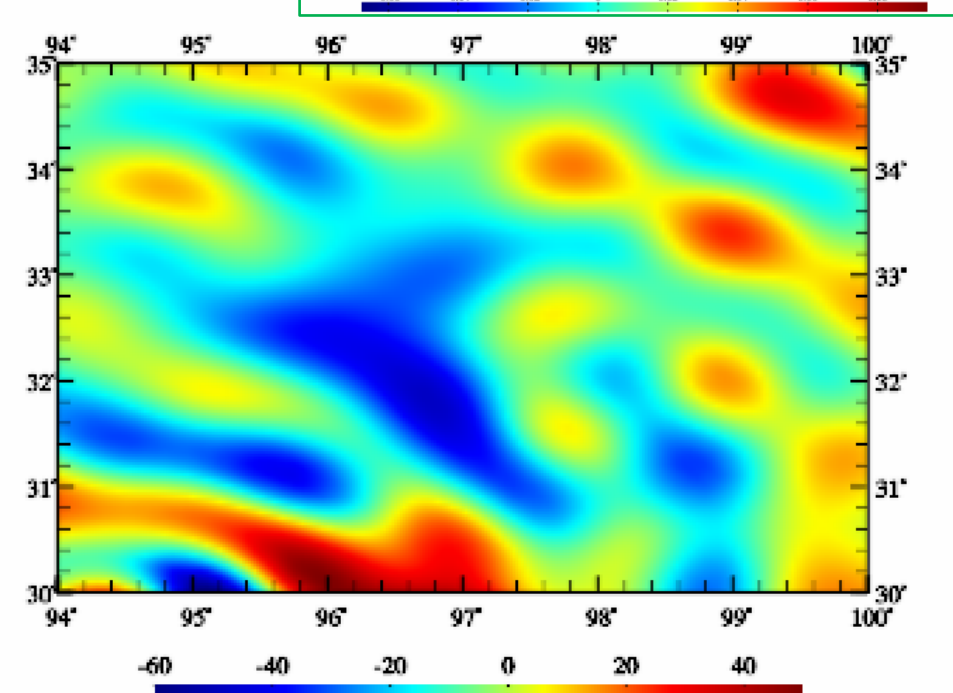
Plot↓



height anomaly (m)



gravity anomaly (mGal)




gravity disturbance (mGal)

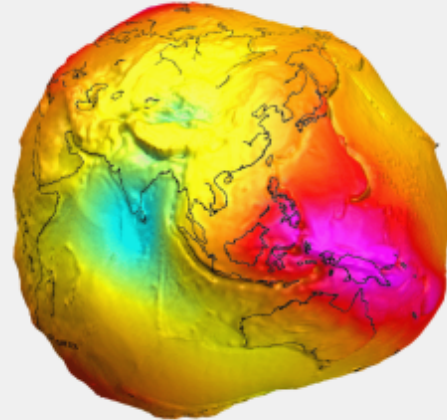
When the minimum and maximum degree n to be set is equal, the program calculates the contribution of the degree n geopotential coefficients to the anomalous gravity field element, which can be employed to analyze and evaluate the spectral and space properties of the geopotential coefficient model.

Input the geodetic coordinates of calculation point


Longitude Latitude Ellipsoidal height


 Open global geopotential coefficient model file

When opening an ultrahigh-degree geopotential coefficient model file, program need read and initialize, please wait...



Set maximum calculation degree

 Calculating the geopotential W_g of the geoid from the calculator, it can be verified that W_g is equal to the normal potential U_0 of the normal ellipsoid. (1) Given the latitude and longitude at any point, input the ellipsoidal height of the point as zero for the first time, and calculate the height anomaly of the point, then (2) input the height anomaly as the ellipsoidal height of the point for the second time, and calculate again. (3) When the calculated height anomaly is equal to the input ellipsoidal height, the calculation point is on the geoid, and the calculated geopotential of the point is W_g , namely the geopotential of the gravimetric geoid.

 Start Computation

Model gravity field elements calculated

height anomaly/geoidal height (m)	<input type="text" value="13.0099"/>	gravity anomaly (mGal)	<input type="text" value="32.6014"/>	gravity m/s ²	<input type="text" value="9.793115777"/>
gravity disturbance (mGal)	<input type="text" value="36.5996"/>	vertical deflection S (")	<input type="text" value="2.3487"/>	vertical deflection W (")	<input type="text" value="-3.5341"/>
disturbing gravity gradient (E)	<input type="text" value="42.9662"/>	tangential gradient N (E)	<input type="text" value="-7.8402"/>	tangential gradient W (E)	<input type="text" value="-35.1869"/>
Laplace operator (E)	<input type="text" value="-0.0610"/>	gravity gradient (E)	<input type="text" value="3121.5910"/>	geopotential (m ² /s ²)	<input type="text" value="62636811.507"/>

Global geopotential coefficient model

<input type="text" value="3.986004415d0"/>	<input type="text" value="6378136.3d0"/>	<input type="text" value="tide_free"/>			
2	0	-4.841651437908E-04	0.000000000000E+00	5.2900E-12	0.0000E+00
2	1	-2.066155090742E-10	1.384413891380E-09	4.9948E-12	5.1961E-12
2	2	2.439383573283E-06	-1.400273703859E-06	5.1125E-12	5.2500E-12
3	0	9.571612070935E-07	0.000000000000E+00	4.0527E-12	0.0000E+00
3	1	2.030462010479E-06	2.482004158569E-07	4.0493E-12	4.2260E-12
3	2	9.047878948095E-07	-6.190054751776E-07	4.5076E-12	4.5260E-12
3	3	7.213217571216E-07	1.414349261929E-06	4.2632E-12	4.2627E-12
4	0	5.399658666390E-07	0.000000000000E+00	3.1333E-12	0.0000E+00
4	1	-5.361573893889E-07	-4.735673465181E-07	3.2301E-12	3.3121E-12
4	2	3.505016239626E-07	6.624800262758E-07	3.7532E-12	3.6671E-12


The scale parameters of the geopotential coefficient model whose surface harmonic functions are defined on the spherical surface whose radius is equal to the semi-major axis a of the Earth.

Input the geodetic coordinates of calculation point

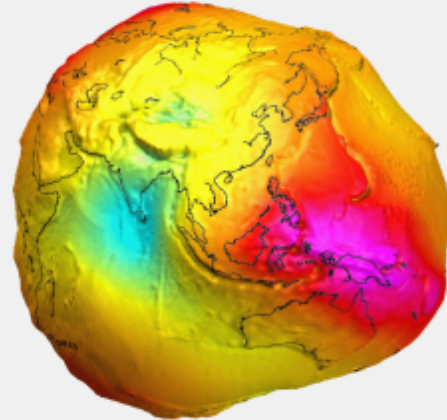
Longitude 87.240000°

Latitude 31.428100°

Ellipsoidal height 5417.8300 m


 Open global geopotential coefficient model file

When opening an ultrahigh-degree geopotential coefficient model file, program need read and initialize, please wait...



Set maximum calculation degree 1800

Calculating the geopotential W_g of the geoid from the calculator, it can be verified that W_g is equal to the normal potential U_0 of the normal ellipsoid. (1) Given the latitude and longitude at any point, input the ellipsoidal height of the point as zero for the first time, and calculate the height anomaly of the point, then (2) input the height anomaly as the ellipsoidal height of the point for the second time, and calculate again. (3) When the calculated height anomaly is equal to the input ellipsoidal height, the calculation point is on the geoid, and the calculated geopotential of the point is W_g , namely the geopotential of the gravimetric geoid.

 Start Computation

Model gravity field elements calculated

height anomaly/geoidal height (m)	-28.6109	gravity anomaly (mGal)	35.8449	gravity m/s ²	9.777951466
gravity disturbance (mGal)	27.0723	vertical deflection S (")	5.0582	vertical deflection W (")	-1.0667
disturbing gravity gradient (E)	1.9139	tangential gradient N (E)	-30.5760	tangential gradient W (E)	28.7014
Laplace operator (E)	0.0393	gravity gradient (E)	3072.8990	geopotential (m ² /s ²)	62583559.925

Global geopotential coefficient model

```

3.986004415d0 6378136.3d0 tide_free
2 0 -4.841651437908E-04 0.000000000000E+00 5.2900E-12 0.0000E+00
2 1 -2.066155090742E-10 1.384413891380E-09 4.9948E-12 5.1961E-12
2 2 2.439383573283E-06 -1.400273703859E-06 5.1125E-12 5.2500E-12
3 0 9.571612070935E-07 0.000000000000E+00 4.0527E-12 0.0000E+00
3 1 2.030462010479E-06 2.482004158569E-07 4.0493E-12 4.2260E-12
3 2 9.047878948095E-07 -6.190054751776E-07 4.5076E-12 4.5260E-12
3 3 7.213217571216E-07 1.414349261929E-06 4.2632E-12 4.2627E-12
4 0 5.399658666390E-07 0.000000000000E+00 3.1333E-12 0.0000E+00
4 1 -5.361573893889E-07 -4.735673465181E-07 3.2301E-12 3.3121E-12
4 2 3.505016239626E-07 6.624800262758E-07 3.7532E-12 3.6671E-12

```


The scale parameters of the geopotential coefficient model whose surface harmonic functions are defined on the spherical surface whose radius is equal to the semi-major axis a of the Earth.

Input the geodetic coordinates of calculation point

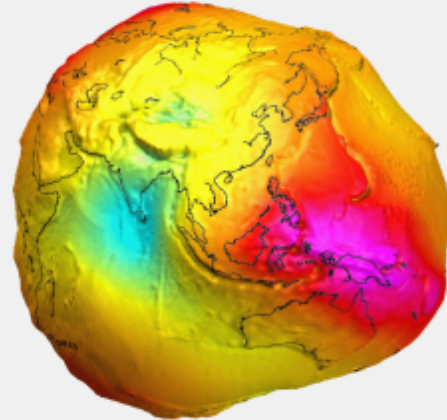
Longitude 130.240000°

Latitude 21.428100°

Ellipsoidal height -35.8300 m


 Open global geopotential coefficient model file

When opening an ultrahigh-degree geopotential coefficient model file, program need read and initialize, please wait...



Set maximum calculation degree 1800

Calculating the geopotential W_g of the geoid from the calculator, it can be verified that W_g is equal to the normal potential U_0 of the normal ellipsoid. (1) Given the latitude and longitude at any point, input the ellipsoidal height of the point as zero for the first time, and calculate the height anomaly of the point, then (2) input the height anomaly as the ellipsoidal height of the point for the second time, and calculate again. (3) When the calculated height anomaly is equal to the input ellipsoidal height, the calculation point is on the geoid, and the calculated geopotential of the point is W_g , namely the geopotential of the gravimetric geoid.

 Start Computation

Model gravity field elements calculated

height anomaly/geoidal height (m)	36.5055	gravity anomaly (mGal)	-4.6059	gravity m/s ²	9.787399347
gravity disturbance (mGal)	6.6028	vertical deflection S (")	2.3436	vertical deflection W (")	-1.9081
disturbing gravity gradient (E)	-4.5026	tangential gradient N (E)	0.9093	tangential gradient W (E)	3.5423
Laplace operator (E)	-0.0510	gravity gradient (E)	3073.5406	geopotential (m ² /s ²)	62637566.679

Global geopotential coefficient model

```

3.986004415d0 6378136.3d0 tide_free
2 0 -4.841651437908E-04 0.000000000000E+00 5.2900E-12 0.0000E+00
2 1 -2.066155090742E-10 1.384413891380E-09 4.9948E-12 5.1961E-12
2 2 2.439383573283E-06 -1.400273703859E-06 5.1125E-12 5.2500E-12
3 0 9.571612070935E-07 0.000000000000E+00 4.0527E-12 0.0000E+00
3 1 2.030462010479E-06 2.482004158569E-07 4.0493E-12 4.2260E-12
3 2 9.047878948095E-07 -6.190054751776E-07 4.5076E-12 4.5260E-12
3 3 7.213217571216E-07 1.414349261929E-06 4.2632E-12 4.2627E-12
4 0 5.399658666390E-07 0.000000000000E+00 3.1333E-12 0.0000E+00
4 1 -5.361573893889E-07 -4.735673465181E-07 3.2301E-12 3.3121E-12
4 2 3.505016239626E-07 6.624800262758E-07 3.7532E-12 3.6671E-12

```

The scale parameters of the geopotential coefficient model whose surface harmonic functions are defined on the spherical surface whose radius is equal to the semi-major axis a of the Earth.

Calculation and analysis of spectral character of Earth's gravity field

Calculation and analysis of spectral character of Earth's gravity field

Open the 1st global geopotential coefficient model file

Open the 2nd global geopotential coefficient model file

Save the results as

Start Computation

The current number of global geopotential models input

0

Chart plot↓

Start end row number 30 720 curve type

Geopotential coefficient degree variance curves

After clicking [Start Computation], you need to wait until [Chart plot] becomes available.

The program can plot up to ten spectral curves of the global geopotential model.

```
3.986004415d0 6378136.46d0 tide_free
2 0 -4.84165217061e-04 0.000000000000e+00 1.1081e-13 0.0000e+00
3 0 9.57173592933e-07 0.000000000000e+00 6.5264e-14 0.0000e+00
4 0 5.39998754738e-07 0.000000000000e+00 2.9945e-14 0.0000e+00
5 0 6.86465403533e-08 0.000000000000e+00 2.2918e-14 0.0000e+00
6 0 -1.49975580611e-07 0.000000000000e+00 1.8644e-14 0.0000e+00
7 0 9.04993977725e-08 0.000000000000e+00 1.6557e-14 0.0000e+00
8 0 4.94771152555e-08 0.000000000000e+00 1.5132e-14 0.0000e+00
9 0 2.80189081183e-08 0.000000000000e+00 1.4193e-14 0.0000e+00
```

10
11
12
13
14
15
16
17
18
19
20
21
22
23

Calculation and analysis of spectral character of Earth's gravity field

Open the 3th global geopotential coefficient model file

The program can plot up to ten spectral curves of the global geopotential model.

```
2 3.125000E-01 7.911381E-02 1.336401E-12 1.132710E-05 7.373306E-05 7.911290E-02 5.7318
3 8.641975E-02 8.823035E-02 1.278378E-12 1.584411E-05 1.031363E-04 8.823024E-02 5.1312
4 3.515625E-02 2.289217E-02 1.193316E-12 1.912071E-05 1.244651E-04 2.289248E-02 5.2544
5 1.760000E-02 1.366044E-02 1.028261E-12 2.154812E-05 1.402662E-04 1.365972E-02 5.2227
6 1.003086E-02 8.191773E-03 9.314054E-13 2.353173E-05 1.531784E-04 8.191840E-03 4.6443
7 6.247397E-03 5.675256E-03 8.969146E-13 2.529529E-05 1.646582E-04 5.675040E-03 6.0828
8 4.150391E-03 2.379274E-03 8.857627E-13 2.692380E-05 1.752588E-04 2.379201E-03 4.1747
9 2.895900E-03 1.819157E-03 8.972851E-13 2.847869E-05 1.853803E-04 1.819042E-03 6.6549
10 2.100000E-03 1.264171E-03 9.295262E-13 3.000461E-05 1.953132E-04 1.264069E-03 4.8878
11 1.570931E-03 6.892058E-04 9.267179E-13 3.145230E-05 2.047369E-04 6.891495E-04 6.3386
12 1.205633E-03 2.284380E-04 9.893414E-13 3.292766E-05 2.143406E-04 2.284436E-04 6.3453
13 9.453451E-04 5.736342E-04 1.073660E-12 3.445735E-05 2.242980E-04 5.736203E-04 5.8004
14 7.548938E-04 2.158315E-04 1.157452E-12 3.603376E-05 2.345596E-04 2.158393E-04 5.3293
15 6.123457E-04 1.950448E-04 1.323097E-12 3.775523E-05 2.457654E-04 1.950386E-04 4.7335
16 5.035400E-04 1.898962E-04 1.398471E-12 3.949329E-05 2.570792E-04 1.898916E-04 4.5364
17 4.190563E-04 1.308700E-04 1.562868E-12 4.134931E-05 2.691608E-04 1.308675E-04 6.0347
18 3.524615E-04 1.393244E-04 1.715295E-12 4.329485E-05 2.818252E-04 1.393118E-04 8.7300
19 2.992611E-04 1.033262E-04 1.923900E-12 4.537787E-05 2.953845E-04 1.033288E-04 9.1430
20 2.562500E-04 9.200739E-05 2.143124E-12 4.759102E-05 3.097909E-04 9.200352E-05 1.3341
21 2.211013E-04 9.555692E-05 2.409070E-12 4.996190E-05 3.252240E-04 9.555385E-05 1.2128
22 1.920975E-04 8.205035E-05 2.696481E-12 5.248877E-05 3.416725E-04 8.205169E-05 1.5534
23 1.679525E-04 6.618978E-05 3.043117E-12 5.520172E-05 3.593323E-04 6.618503E-05 1.3874
```

Save the results as

Start Computation

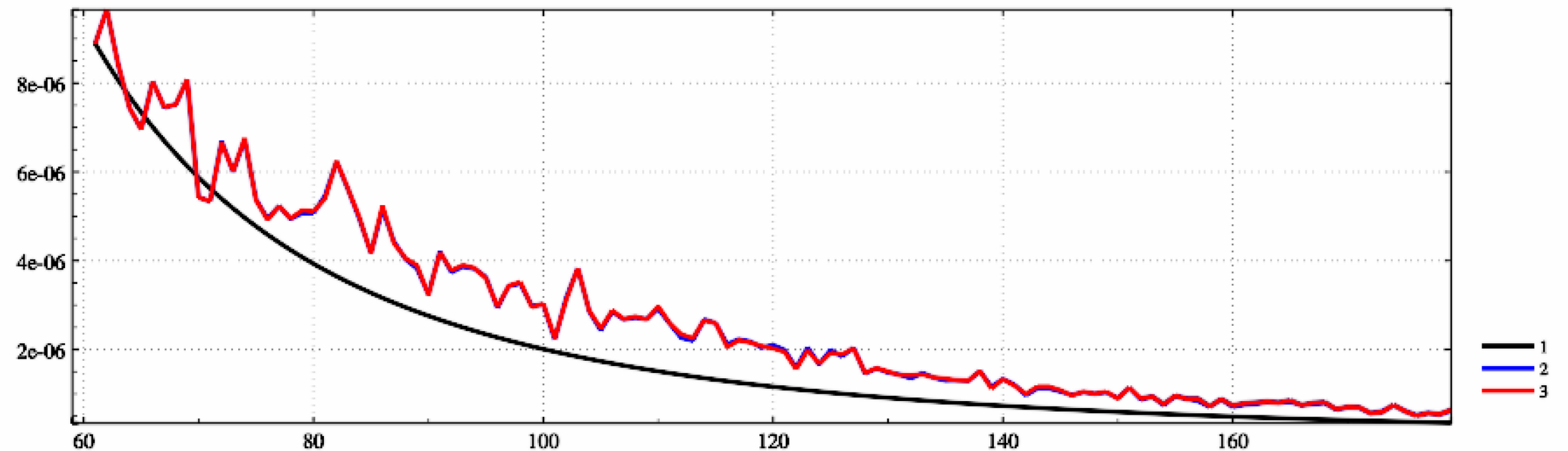
The current number of global geopotential models input

2

Chart plot↓

Start end row number 60 180 curve type Geopotential coefficient degree variance line thickness 3 Save current plot as

Geopotential coefficient degree variance curves



Open the 4th global geopotential coefficient model file

The program can plot up to ten spectral curves of the global geopotential model.

2	3.125000E-01	7.911381E-02	1.336401E-12	1.132710E-05	7.373306E-05	7.911290E-02	5.7318
3	8.641975E-02	8.823035E-02	1.278378E-12	1.584411E-05	1.031363E-04	8.823024E-02	5.1312
4	3.515625E-02	2.289217E-02	1.193316E-12	1.912071E-05	1.244651E-04	2.289248E-02	5.2544
5	1.760000E-02	1.366044E-02	1.028261E-12	2.154812E-05	1.402662E-04	1.365972E-02	5.2227
6	1.003086E-02	8.191773E-03	9.314054E-13	2.353173E-05	1.531784E-04	8.191840E-03	4.6443
7	6.247397E-03	5.675256E-03	8.969146E-13	2.529529E-05	1.646582E-04	5.675040E-03	6.0828
8	4.150391E-03	2.379274E-03	8.857627E-13	2.692380E-05	1.752588E-04	2.379201E-03	4.1747
9	2.895900E-03	1.819157E-03	8.972851E-13	2.847869E-05	1.853803E-04	1.819042E-03	6.6549
10	2.100000E-03	1.264171E-03	9.295262E-13	3.000461E-05	1.953132E-04	1.264069E-03	4.8878
11	1.570931E-03	6.892058E-04	9.267179E-13	3.145230E-05	2.047369E-04	6.891495E-04	6.3386
12	1.205633E-03	2.284380E-04	9.893414E-13	3.292766E-05	2.143406E-04	2.284436E-04	6.3453
13	9.453451E-04	5.736342E-04	1.073660E-12	3.445735E-05	2.242980E-04	5.736203E-04	5.8004
14	7.548938E-04	2.158315E-04	1.157452E-12	3.603376E-05	2.345596E-04	2.158393E-04	5.3293
15	6.123457E-04	1.950448E-04	1.323097E-12	3.775523E-05	2.457654E-04	1.950386E-04	4.7335
16	5.035400E-04	1.898962E-04	1.398471E-12	3.949329E-05	2.570792E-04	1.898916E-04	4.5364
17	4.190563E-04	1.308700E-04	1.562868E-12	4.134931E-05	2.691608E-04	1.308675E-04	6.0347
18	3.524615E-04	1.393244E-04	1.715295E-12	4.329485E-05	2.818252E-04	1.393118E-04	8.7300
19	2.992611E-04	1.033262E-04	1.923900E-12	4.537787E-05	2.953845E-04	1.033288E-04	9.1430
20	2.562500E-04	9.200739E-05	2.143124E-12	4.759102E-05	3.097909E-04	9.200352E-05	1.3341
21	2.211013E-04	9.555692E-05	2.409070E-12	4.996190E-05	3.252240E-04	9.555385E-05	1.2128
22	1.920975E-04	8.205035E-05	2.696481E-12	5.248877E-05	3.416725E-04	8.205169E-05	1.5534

Save the results as

Start Computation

The current number of global geopotential models input

3

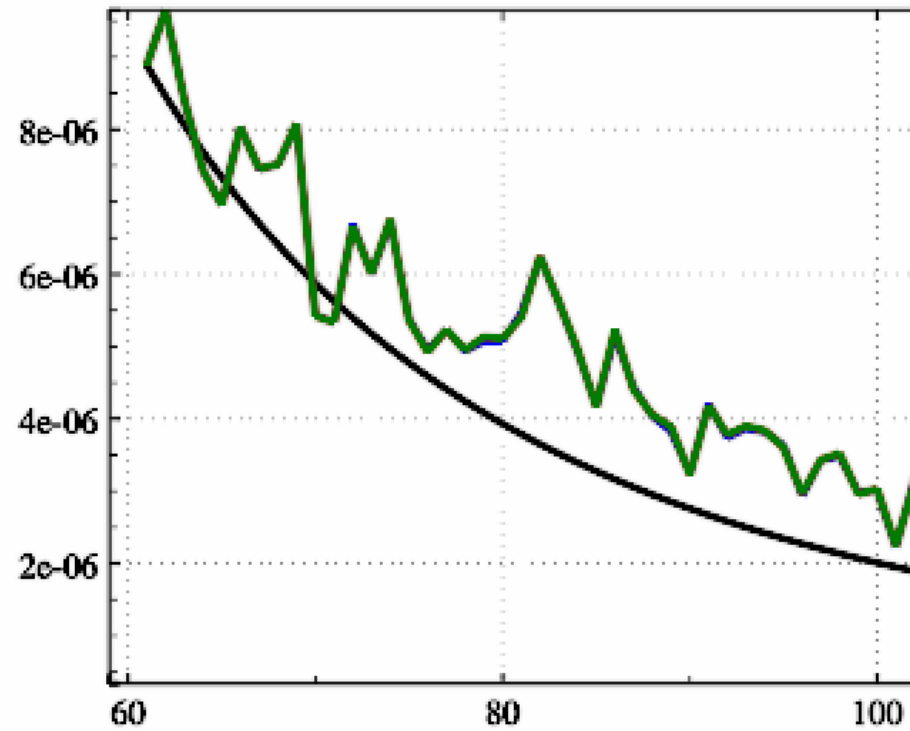
Chart plot

Start end row number 60

180

curve type Geop

Geopotential coefficient degree variance curves



Open the 4th global geopotential coefficient model file

The program can plot up to ten spectral curves of the global geopotential model.

2	3.125000E-01	7.911381E-02	1.336401E-12	1.132710E-05	7.373306E-05	7.911290E-02	5.7318
3	8.641975E-02	8.823035E-02	1.278378E-12	1.584411E-05	1.031363E-04	8.823024E-02	5.1312
4	3.515625E-02	2.289217E-02	1.193316E-12	1.912071E-05	1.244651E-04	2.289248E-02	5.2544
5	1.760000E-02	1.366044E-02	1.028261E-12	2.154812E-05	1.402662E-04	1.365972E-02	5.2227
6	1.003086E-02	8.191773E-03	9.314054E-13	2.353173E-05	1.531784E-04	8.191840E-03	4.6443
7	6.247397E-03	5.675256E-03	8.969146E-13	2.529529E-05	1.646582E-04	5.675040E-03	6.0828
8	4.150391E-03	2.379274E-03	8.857627E-13	2.692380E-05	1.752588E-04	2.379201E-03	4.1747
9	2.895900E-03	1.819157E-03	8.972851E-13	2.847869E-05	1.853803E-04	1.819042E-03	6.6549
10	2.100000E-03	1.264171E-03	9.295262E-13	3.000461E-05	1.953132E-04	1.264069E-03	4.8878
11	1.570931E-03	6.892058E-04	9.267179E-13	3.145230E-05	2.047369E-04	6.891495E-04	6.3386
12	1.205633E-03	2.284380E-04	9.893414E-13	3.292766E-05	2.143406E-04	2.284436E-04	6.3453
13	9.453451E-04	5.736342E-04	1.073660E-12	3.445735E-05	2.242980E-04	5.736203E-04	5.8004
14	7.548938E-04	2.158315E-04	1.157452E-12	3.603376E-05	2.345596E-04	2.158393E-04	5.3293
15	6.123457E-04	1.950448E-04	1.323097E-12	3.775523E-05	2.457654E-04	1.950386E-04	4.7335
16	5.035400E-04	1.898962E-04	1.398471E-12	3.949329E-05	2.570792E-04	1.898916E-04	4.5364
17	4.190563E-04	1.308700E-04	1.562868E-12	4.134931E-05	2.691608E-04	1.308675E-04	6.0347
18	3.524615E-04	1.393244E-04	1.715295E-12	4.329485E-05	2.818252E-04	1.393118E-04	8.7300
19	2.992611E-04	1.033262E-04	1.923900E-12	4.537787E-05	2.953845E-04	1.033288E-04	9.1430
20	2.562500E-04	9.200739E-05	2.143124E-12	4.759102E-05	3.097909E-04	9.200352E-05	1.3341
21	2.211013E-04	9.555692E-05	2.409070E-12	4.996190E-05	3.252240E-04	9.555385E-05	1.2128
22	1.920975E-04	8.205035E-05	2.696481E-12	5.248877E-05	3.416725E-04	8.205169E-05	1.5534

Save the results as

Start Computation

The current number of global geopotential models input

3

Chart plot

Start end row number 30

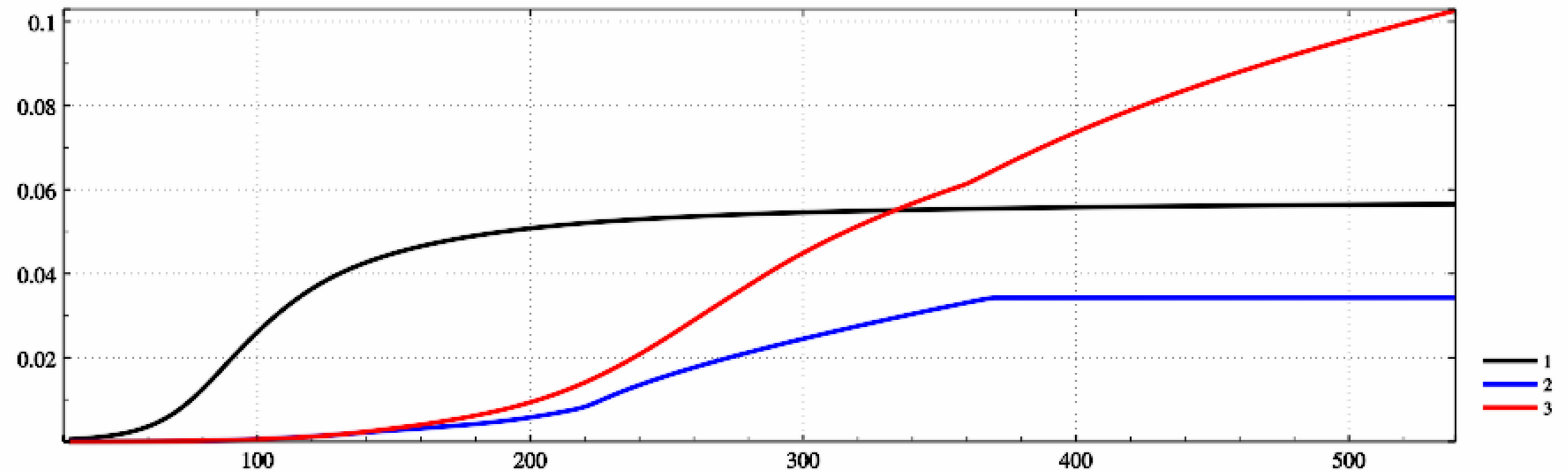
540

curve type The cumulative error of the geoidal height

line thickness 3

Save current plot as

The cumulative error curves of the geoidal height



Calculation of anomalous field elements at observed points

Open observations Save as Import parameters Start Computation Save process Follow example



Calculation of anomalous field elements at observed points

Statistical error estimation of regional gravimetric geoid

Calculation of influence of gravity system bias on gravimetric geoid

Open the observed gravity data file

>> Computation Process ** Operation Prompts

Save computation process as

Set input point file format

Number of rows of file header: 1

Column ordinal number of height in the record: 4

Column ordinal number of observation in the record: 6

Select calculation type: gravity anomaly (mGal)

>> [Function] Using the rigorous spherical harmonic expansion formula, calculate the normal gravity field elements, and then calculate the gravity anomaly (mGal), gravity disturbance (mGal) or disturbing gravity gradient (E, radial) from the observed gravity (mGal) or gravity gradient (E).

** Click the [Open the observed gravity data file] control button, or the [Open observation file] tool button...

>> Open the observed gravity data file C:/PAGrav4.5_win64en/examples/ProbsAnomousgrav/obsgrav.txt.

** Look at the file information in the window below, set the input file format parameters, select the anomalous field element, and click the [Import setting parameters] button to input the parameters into the system...

** When the height is normal (orthometric) height, the program calculates the gravity anomaly at the observed point, and when the height is the ellipsoidal height, the program calculates the gravity disturbance or disturbing gravity gradient at the observed point.

>> Save the results as C:/PAGrav4.5_win64en/examples/ProbsAnomousgrav/result.txt.

** Behind the input file record, appends a column of gravity anomaly, gravity disturbance or disturbing gravity gradient calculated value at the observed point, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Prepare to calculate gravity anomaly (mGal)...

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-21 17:09:51

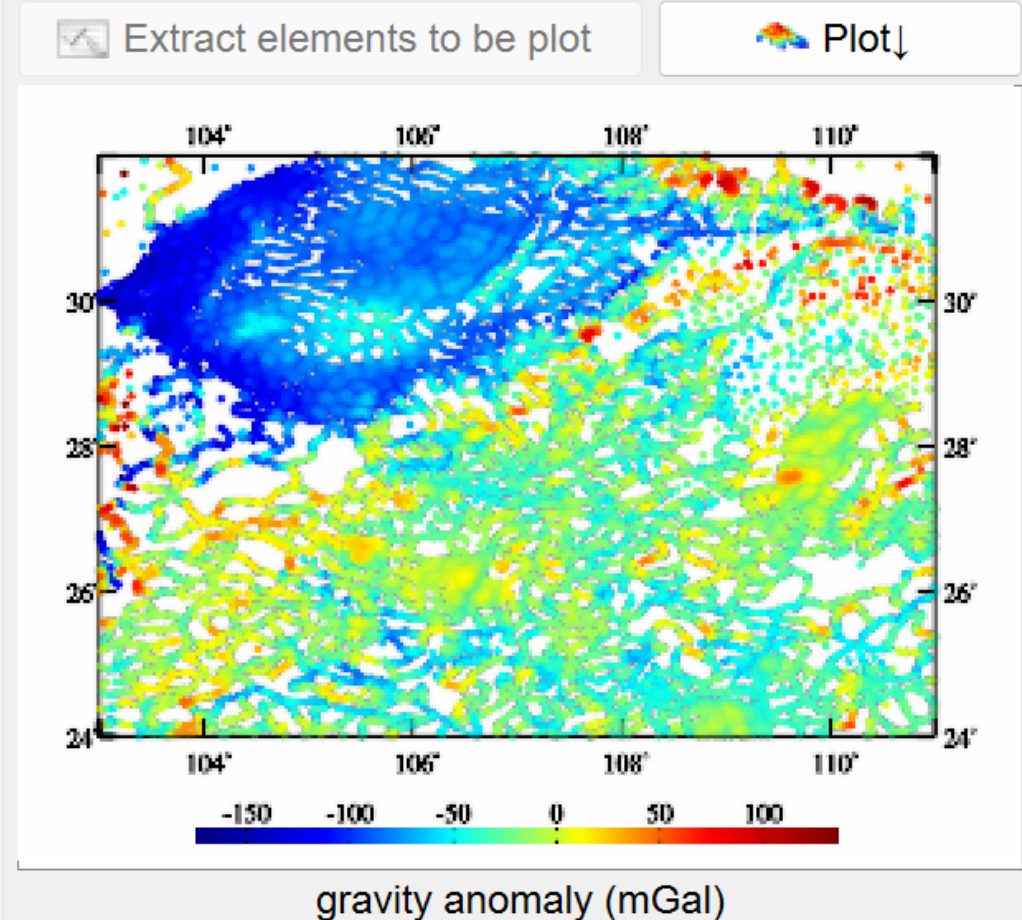
>> Complete the calculation of the observed anomalous field element!

Save the results as

Import setting parameters

Start Computation

no	lon(degree/decimal)	lat	ellipHeight(m)	normalHeight(m)	obsGrav(mGal)
3248	103.671939	31.938051	2743.9394	2774.9485	978685.3537
3249	103.696944	31.864721	2501.2449	2532.6723	978711.5370
3250	103.718330	31.831114	2435.4206	2467.0248	978720.1941
3251	103.735559	31.795280	2366.5700	2398.2238	978757.9613
3252	103.777216	31.776390	2294.0304	2325.9778	978784.3962
3253	103.822773	31.758333	2233.2317	2265.6064	978787.9523
3254	103.849717	31.724168	2215.6606	2248.2924	978780.1624
3255	103.816666	31.650003	2242.9951	2275.1975	978785.6408
3256	103.783335	31.616667	2297.3654	2329.3256	978762.6285
3257	103.740556	31.581110	2218.6104	2250.3209	978787.4579
3258	103.703884	31.560833	2207.1173	2238.6600	978797.9046
3259	103.682782	31.531391	2245.2634	2276.8015	978786.2913
3260	103.651939	31.510554	2219.9076	2251.4497	978780.8011
3261	103.613883	31.491662	2080.5161	2112.0781	978799.7103
3262	103.545003	31.444998	2051.8797	2083.3689	978803.4042
3263	103.516664	31.386384	2187.5689	2219.2172	978769.9887
3264	103.499170	31.362780	2175.1817	2206.9690	978758.0577
3265	103.474724	31.325836	2075.9238	2107.9969	978756.2234
3266	103.469164	31.282503	1931.3869	1963.8325	978794.8112
3267	103.486671	31.251384	1935.5737	1968.3811	978806.5352



Statistical error estimation of regional gravimetric geoid

Statistical error estimation of regional gravimetric geoid

The grid mean gravity representative error

The grid mean gravity spatial resolution

Gravimetric geoid error cm

Statistical error estimation of regional gravimetric geoid

The grid mean gravity representative error

The grid mean gravity spatial resolution

Gravimetric geoid error cm

Calculation of influence of gravity system bias on gravimetric geoid

Calculation of influence of gravity system bias on gravimetric geoid

System bias of gravity anomaly (disturbance)

Local Stokes/Hotine integral radius

Calculation of system bias influence on geoid cm

Calculation of influence of gravity system bias on gravimetric geoid

System bias of gravity anomaly (disturbance)

Local Stokes/Hotine integral radius

Calculation of system bias influence on geoid cm

Correction calculation of boundary value for spherical or ellipsoidal boundary surface

Open calculation points Import parameters Save as Start Computation Save process Follow example



Correction calculation of boundary value for spherical or ellipsoidal boundary surface

Molodensky boundary value correction for arbitrary shape boundary surface

Boundary value correction formula

Open global geopotential coefficient model file

>> Computation Process ** Operation Prompts

Open the calculation point file on non-equipotential surface

surface, thereby converting the Molodensky boundary value problem into the Stokes problem.
 >> The ellipsoidal boundary value correction is mainly employed for ellipsoidal harmonic analysis of the global gravity field by FFT integral method. Spherical boundary value correction is commonly employed for the Bjerhammar boundary value problem.
 ** Input the global geopotential coefficient model file and the calculation point file on the boundary surface...
 >> Open global geopotential coefficient model file C:/PAGrav4.5_win64en/data/EGM2008.gfc.
 ** The window below only shows the geopotential coefficients data with no more than 2000 rows in it.
 >> Open the calculation point file on the boundary surface C:/PAGrav4.5_win64en/examples/PrBoundaryvalueAdj/calcpnt.txt.
 ** Look at the file information in the window below, set the input file format parameters, select the field element and boundary surface, enter the output file name, click the [Import setting parameters] button to input the parameters into the system...
 >> Save the results as C:/PAGrav4.5_win64en/examples/PrBoundaryvalueAdj/result.txt.
 ** The boundary surface is an ellipsoidal surface. The program appends a column of the vertical deflection correction value of gravity behind the input file record.
 >> The parameter settings have been entered into the system!

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

Select type of field element

gravity disturbance (mGal)

Select type of boundary surface

ellipsoidal surface

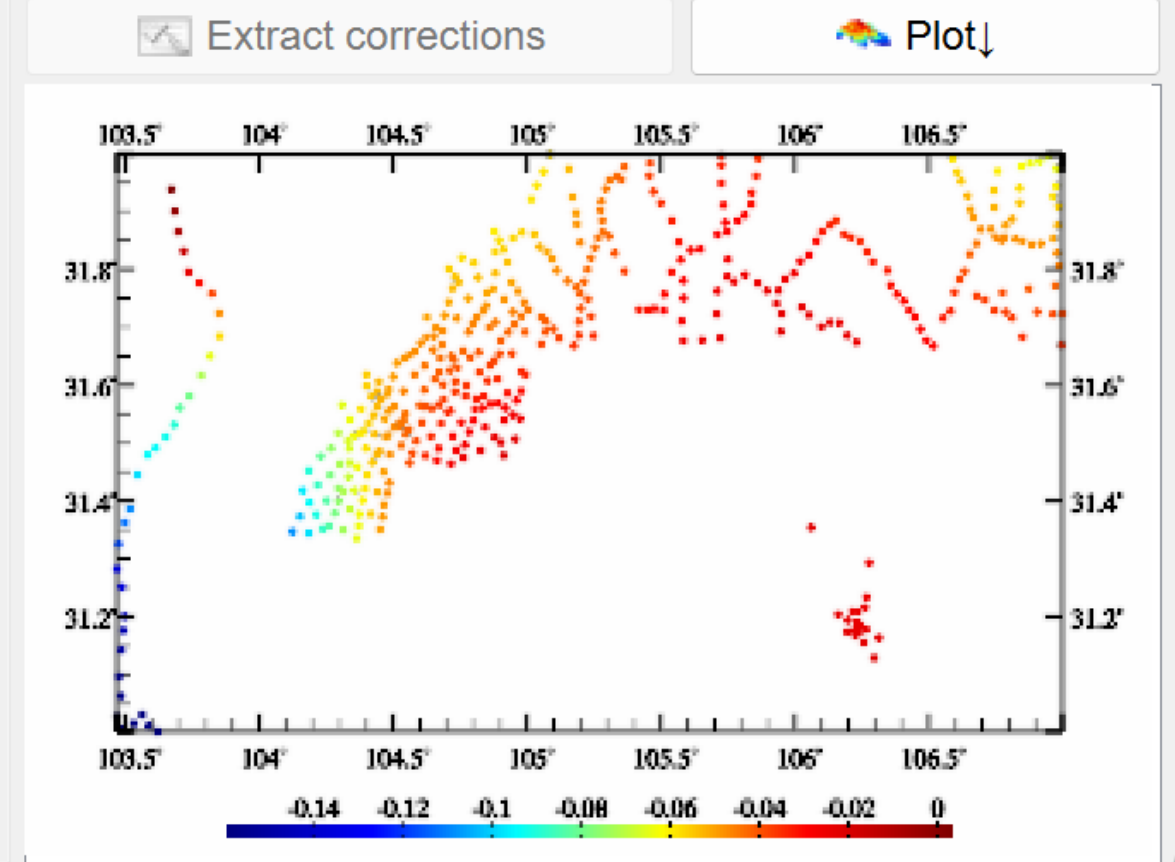
Maximum calculation degree 360

Save the results as

Import setting parameters

Start Computation

number (vvalue or str)	long (degree/decimal)	lat (degree/decimal)	ellipHeight (m)
3248	103.671939	31.938051	2743.9394
3249	103.696944	31.864721	2501.2449
3250	103.718330	31.831114	2435.4206
3251	103.735559	31.795280	2366.5700
3252	103.777216	31.776390	2294.0304
3253	103.822773	31.758333	2233.2317
3254	103.849717	31.724168	2215.6606
3255	103.816666	31.650003	2242.9951
3256	103.783335	31.616667	2297.3654
3257	103.740556	31.581110	2218.6104
3258	103.703884	31.560833	2207.1173
3259	103.682782	31.531391	2245.2634
3260	103.651939	31.510554	2219.9076
3261	103.613883	31.491662	2080.5161
3262	103.545003	31.444998	2051.8797
3263	103.516664	31.386384	2187.5689
3264	103.499170	31.362780	2175.1817
3265	103.474724	31.325836	2075.9238



Correction calculation of boundary value for spherical or ellipsoidal boundary surface

Open calculation points Import parameters Save as Start Computation Save process Follow example



Correction calculation of boundary value for spherical or ellipsoidal boundary surface

Molodensky boundary value correction for arbitrary shape boundary surface

Boundary value correction formula

Open global geopotential coefficient model file

>> Computation Process ** Operation Prompts

Open the calculation point file on non-equipotential surface

>> Open the calculation point file on the boundary surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/calcpnt.txt.

Set input point file format

Number of rows of file header 1

** Look at the file information in the window below, set the input file format parameters, select the field element and boundary surface, enter the output file name, click the [Import setting parameters] button to input the parameters into the system...

Column ordinal number of ellipsoidal height in the record 4

>> Save the results as C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/result1.txt.

Select type of field element

gravity disturbance (mGal)

** The boundary surface is spherical. The program appends 4 columns of correction values behind the input file record. The first to third columns are the vertical deflection correction, correction for the gravity from the normal gravity direction to the geocentric direction and correction for the normal gravity from the normal gravity direction to the geocentric direction, respectively, and the fourth column is the sum of the three corrections.

Select type of boundary surface

spherical surface

>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...

** The calculation process need wait, during which you can open the output file to view the calculation progress...

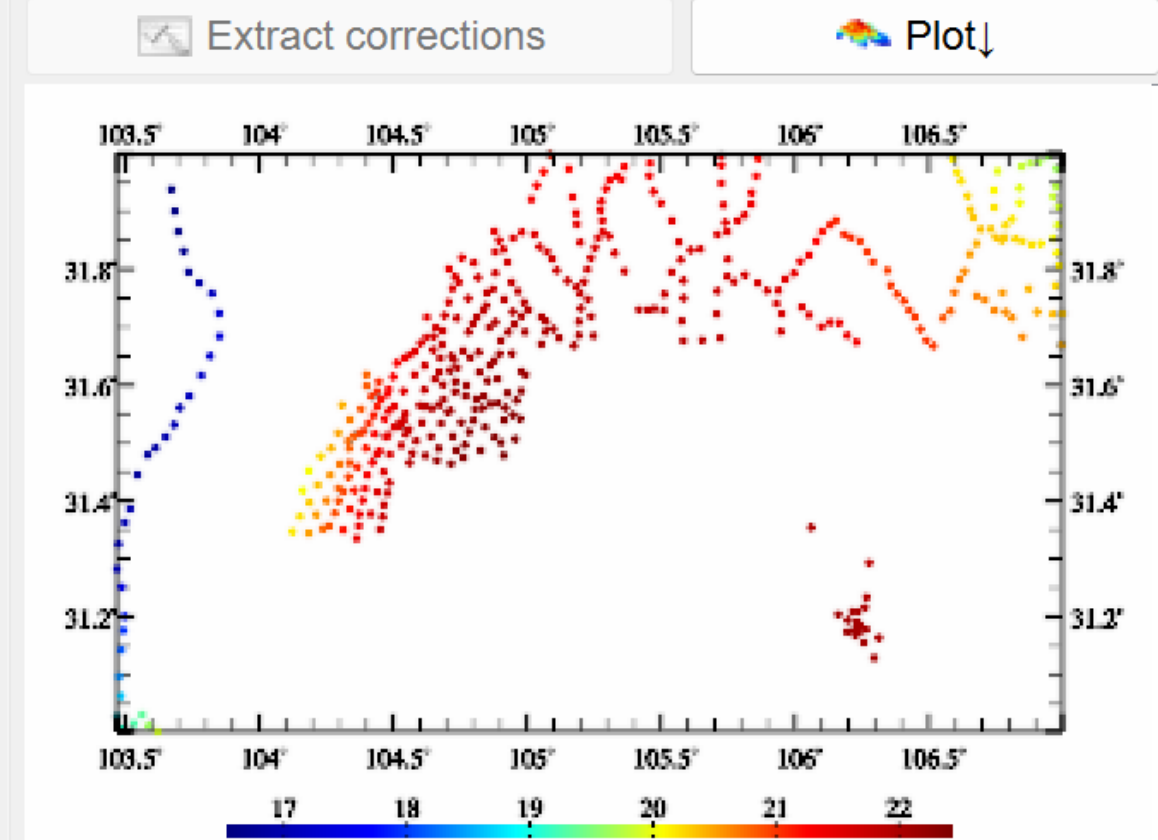
Maximum calculation degree 360

Save the results as

Import setting parameters

Start Computation

number (vvalue or str)	long (degree/decimal)	lat (degree/decimal)	ellipHeight (m)			
3248	103.671939	31.938051	2743.9394	0.0035	0.0072	16.5172
3249	103.696944	31.864721	2501.2449	-0.0075	-0.0154	16.6091
3250	103.718330	31.831114	2435.4206	-0.0149	-0.0308	16.7035
3251	103.735559	31.795280	2366.5700	-0.0233	-0.0480	16.8032
3252	103.777216	31.776390	2294.0304	-0.0307	-0.0632	16.9908
3253	103.822773	31.758333	2233.2317	-0.0380	-0.0782	17.2192
3254	103.849717	31.724168	2215.6606	-0.0476	-0.0979	17.4206
3255	103.816666	31.650003	2242.9951	-0.0645	-0.1328	17.4644
3256	103.783335	31.616667	2297.3654	-0.0718	-0.1478	17.4181
3257	103.740556	31.581110	2218.6104	-0.0794	-0.1634	17.3475
3258	103.703884	31.560833	2207.1173	-0.0825	-0.1699	17.2643
3259	103.682782	31.531391	2245.2634	-0.0892	-0.1836	17.2944
3260	103.651939	31.510554	2219.9076	-0.0924	-0.1902	17.2517
3261	103.613883	31.491662	2080.5161	-0.0940	-0.1936	17.1707
3262	103.545003	31.444998	2051.8797	-0.0982	-0.2022	17.0996
3263	103.516664	31.386384	2187.5689	-0.1092	-0.2247	17.2681
3264	103.499170	31.362780	2175.1817	-0.1123	-0.2313	17.3115



Molodensky boundary value correction for arbitrary shape boundary surface

Open the calculation point file on non-equipotential surface

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

Input grid data on non-equipotential surface

Open the ellipsoidal height grid file of the boundary surface

Open the field element grid file on the boundary surface

Open the height anomaly grid file on the boundary surface

Open the ellipsoidal height grid file of the equipotential surface

Select type of field element

gravity disturbance (mGal)

Molodensky I integral radius 120 km

Save the results as

Import setting parameters

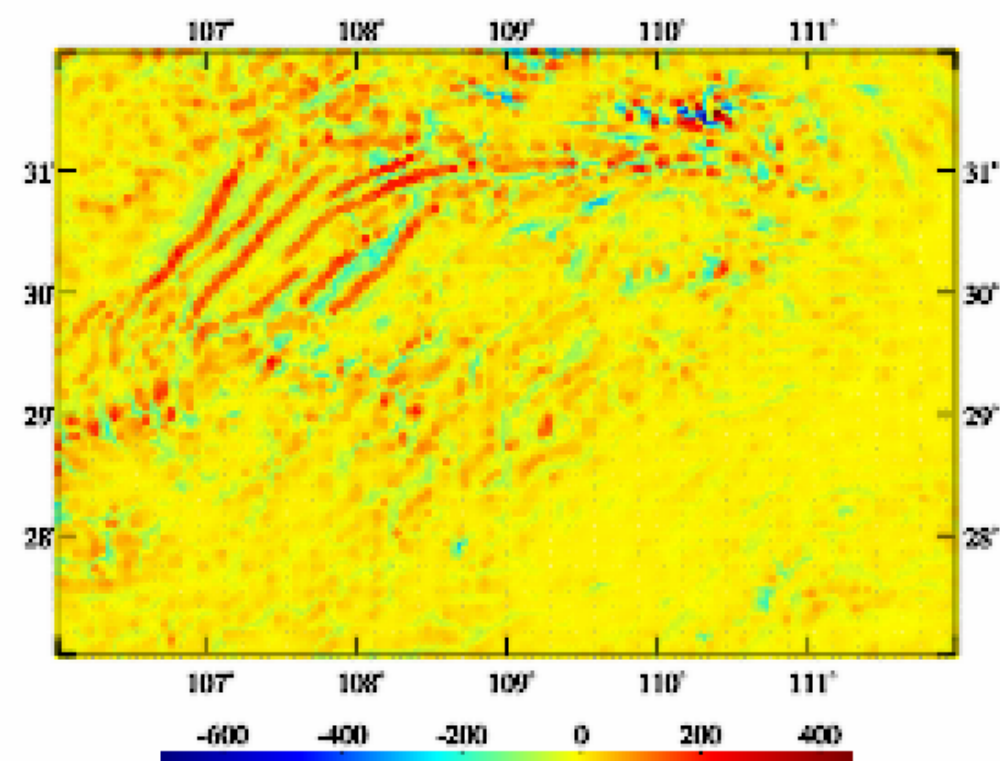
Start Computation

number	lon (degree/decimal)	ellipHeight (m)	disturbGrav (mGal)	
11569	106.020833	27.020833	1217.221	-31.0162
11570	106.062500	27.020833	1201.227	-33.8392
11571	106.104167	27.020833	1185.247	-33.9853
11572	106.145833	27.020833	1210.287	-30.7623
11573	106.187500	27.020833	1228.340	-25.5689
11574	106.229167	27.020833	1247.396	-21.2304
11575	106.270833	27.020833	1244.440	-20.7500
11576	106.312500	27.020833	1199.469	-25.2967
11577	106.354167	27.020833	1183.494	-32.6787
11578	106.395833	27.020833	1109.535	-37.6863
11579	106.437500	27.020833	1000.613	-35.4965
11580	106.479167	27.020833	1135.735	-25.6242
11581	106.520833	27.020833	1249.869	-14.5582
11582	106.562500	27.020833	1251.986	-8.4721
11583	106.604167	27.020833	1289.077	-9.8491
11584	106.645833	27.020833	1292.154	-14.3500
11585	106.687500	27.020833	1228.242	-15.3480
11586	106.729167	27.020833	1211.352	-9.6375

```
>> Computation Process ** Operation Prompts
files...
>> Open the calculation point file on the boundary surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/dbmrga.txt.
** Look at the file information in the window below, set the input file format parameters...
>> Open the ellipsoidal height grid file of the boundary surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/dbmhgt150s.dat.
>> Open the field element grid file on the boundary surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/dbmGM1800150srga.dat.
>> Open the height anomaly grid file on the boundary surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/dbmGM1800150sksi.dat.
>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/dwmhgt150s.dat.
>> Save the results as C:/PAGravf4.5_win64en/examples/PrBoundaryvalueAdj/result2.txt.
** Behind the record of the source calculation point file, appends a column of the Molodensky boundary value correction, and keeps 4 significant figures.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-21 18:28:22
>> Complete calculation of Molodensky boundary value correction!
>> Computation end time: 2024-09-21 18:34:06
```

Extract corrections

Plot



Analytical continuation of anomalous field elements using multi-order radial gradient

Open calculation points Import parameters Save as Start Computation Save process Follow example

Precise Approach of Earth Gravity Field and Geoid

PAGrav4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Open the space position file of anomalous field elements

Set input point file format

Number of rows of file header

Column ordinal number of ellipsoidal height for current field element

Column ordinal number of ellipsoidal height for target field element

Open the field element grid file on the current altitude surface

Open the ellipsoidal height grid file of the current altitude surface

Order number of the radial gradient continuation

Radial gradient integral radius

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the current altitude surface and anomalous field element grid on the surface calculate the 1st to 3rd order radial gradients using the rigorous radial gradient integral formula, and then calculate the continuation corrections of the field elements from the current altitude to the target altitude.

** Click the [Open the space position file of anomalous field elements] control button, and enter the ellipsoidal height and anomalous field element grid data on the current altitude surface...

>> Open the space position file of anomalous field elements C:/PAGrav4.5_win64en/examples/PrGradcontinuation/dbmgra.txt.

** Look at the file information in the window below and set the discrete point file format...

>> Open the field element grid file on the current altitude surface C:/PAGrav4.5_win64en/examples/PrGradcontinuation/dbmchgra.dat.

>> Open the ellipsoidal height grid file of the current altitude surface C:/PAGrav4.5_win64en/examples/PrGradcontinuation/dbmhgt150s.dat.

>> Save the results as C:/PAGrav4.5_win64en/examples/PrGradcontinuation/result.txt.

** Behind the source calculation point file record, appends 1 to 3 columns of field element gradient continuation corrections (the unit is the same as the field element), and keeps 4 significant figures.

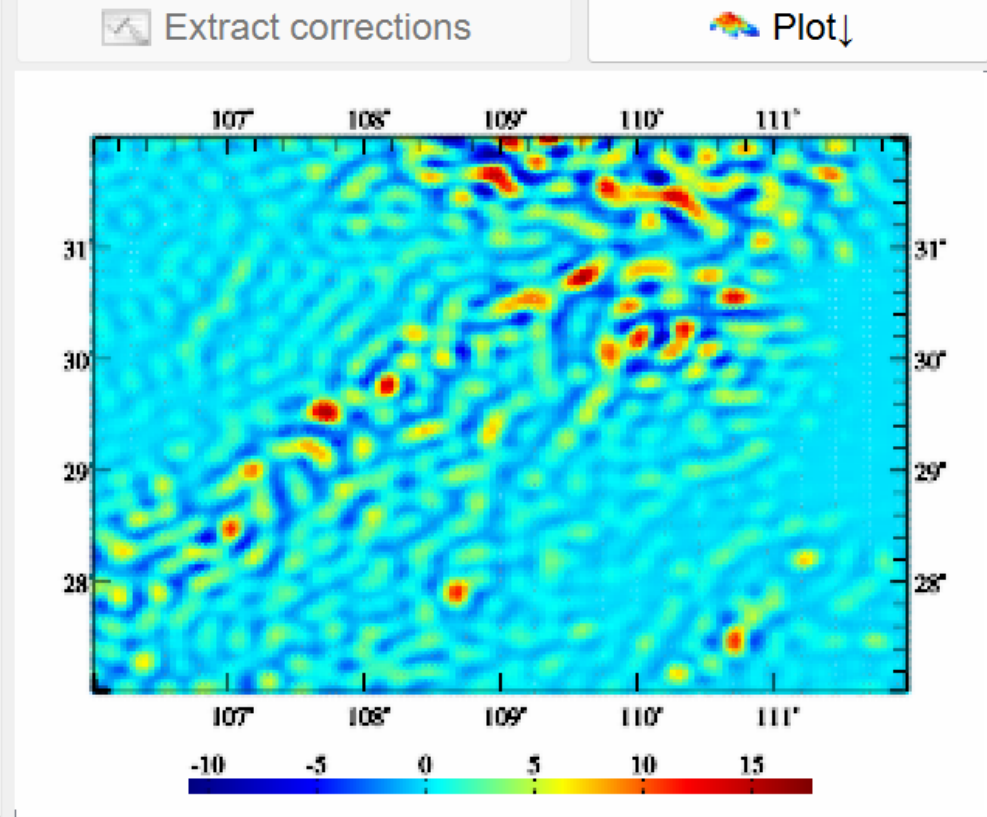
>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-21 20:28:42

Save the results as Import setting parameters Start Computation

no	lon(degree/decimal)	lat	ellipHeight(m)	geoidheight(m)	disturbGrav(mGal)		
11569	106.020833	27.020833	1217.221	-30.8082	-14.8212	-1.6832	
11570	106.062500	27.020833	1201.227	-30.8052	-16.1491	-1.9187	
11571	106.104167	27.020833	1185.247	-30.7849	-14.8039	-1.6058	
11572	106.145833	27.020833	1210.287	-30.7411	-10.1454	-0.6859	
11573	106.187500	27.020833	1228.340	-30.6802	-3.6100	0.6175	
11574	106.229167	27.020833	1247.396	-30.6183	1.9480	1.7425	
11575	106.270833	27.020833	1244.440	-30.5729	3.5017	2.0024	
11576	106.312500	27.020833	1199.469	-30.5503	-0.1382	1.0932	
11577	106.354167	27.020833	1183.494	-30.5360	-6.8208	-0.4436	
11578	106.395833	27.020833	1109.535	-30.4998	-11.3515	-1.4961	
11579	106.437500	27.020833	1000.613	-30.4157	-8.9350	-1.1580	
11580	106.479167	27.020833	1135.735	-30.2841	0.8626	0.4426	
11581	106.520833	27.020833	1249.869	-30.1357	11.6378	2.4377	
11582	106.562500	27.020833	1251.986	-30.0096	17.2750	3.1842	
11583	106.604167	27.020833	1289.077	-29.9216	15.2947	2.2168	
11584	106.645833	27.020833	1292.154	-29.8523	10.0757	0.5266	
11585	106.687500	27.020833	1228.242	-29.7662	8.2597	-0.1705	
11586	106.729167	27.020833	1211.352	-29.6471	13.0764	0.8541	
11587	106.770833	27.020833	1339.471	-29.5138	20.7468	2.8368	



- The radial gradient continuation method adopts the gradient of the observed field element to make analytical continuation, which is suitable for the upward and downward analytical continuation of ground, flight altitude and near range (10km).
- The main components of the field element gradient are short-wave and ultra-short-wave, and the integral radius for radial gradient calculation generally does not need to be large. Therefore, the analytical continuation by the radial gradient method is conducive to the efficient usage of gravity field observation resources.

Analytical continuation of anomalous field elements using multi-order radial gradient

Open calculation points Import parameters Save as Start Computation Save process Follow example



Open the space position file of anomalous field elements

Set input point file format

Number of rows of file header: 1

Column ordinal number of ellipsoidal height for current field element: 4

Column ordinal number of ellipsoidal height for target field element: 5

Open the field element grid file on the current altitude surface

Open the ellipsoidal height grid file of the current altitude surface

Order number of the radial gradient continuation: 2

Radial gradient integral radius: 30 km

>> Computation Process ** Operation Prompts

>> Save the results as C:/PAGrav4.5_win64en/examples/PrGradcontinuation/result.txt.

** Behind the source calculation point file record, appends 1 to 3 columns of field element gradient continuation corrections (the unit is the same as the field element), and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-21 20:28:42

>> Complete the computation of continuation correction of field elements!

>> Computation end time: 2024-09-21 20:28:44

>> Save the results as C:/PAGrav4.5_win64en/examples/PrGradcontinuation/result1.txt.

** Behind the source calculation point file record, appends 1 to 3 columns of field element gradient continuation corrections (the unit is the same as the field element), and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-21 20:30:40

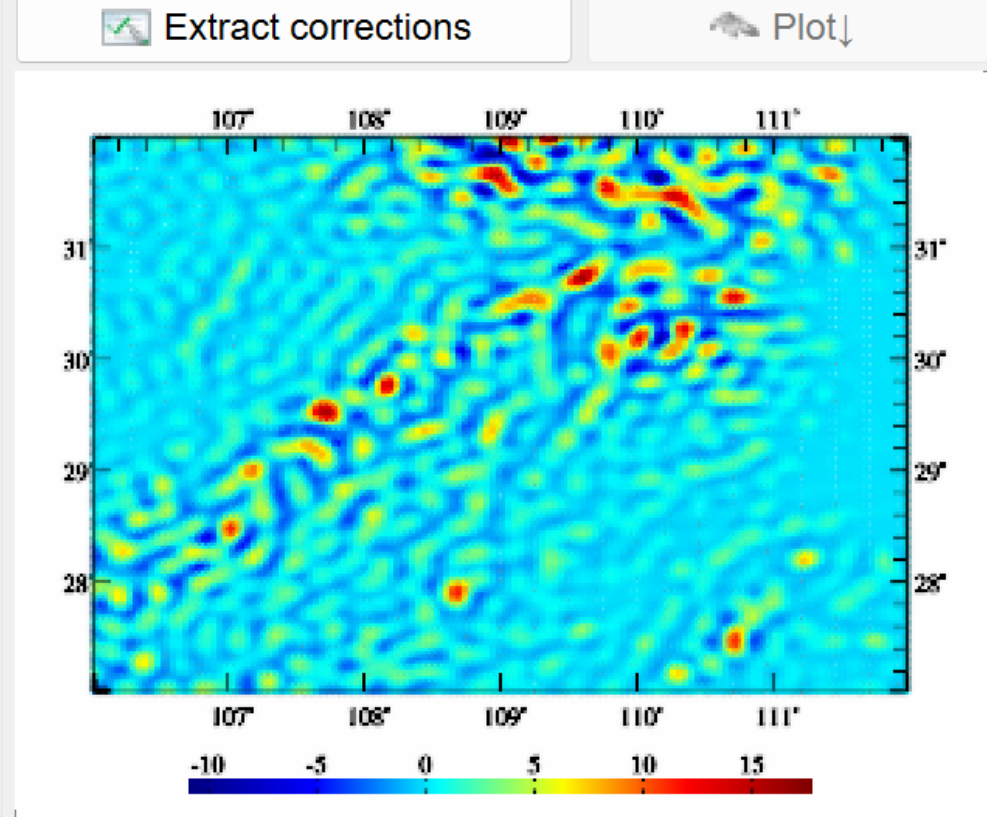
>> Complete the computation of continuation correction of field elements!

>> Computation end time: 2024-09-21 20:30:46

Save computation

Save the results as Import setting parameters Start Computation

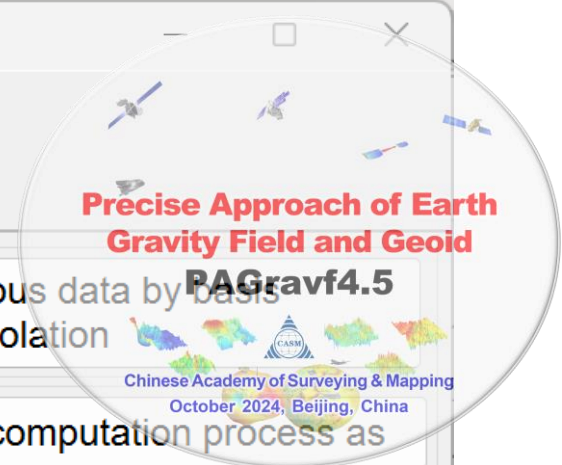
no	lon(degree/decimal)	lat	ellipHeight(m)	geoidheight(m)	disturbGrav(mGal)		
11569	106.020833	27.020833	1217.221	-30.8082	-14.8212	-1.6832	-1.8275
11570	106.062500	27.020833	1201.227	-30.8052	-16.1491	-1.9187	-2.0872
11571	106.104167	27.020833	1185.247	-30.7849	-14.8039	-1.6058	-1.7436
11572	106.145833	27.020833	1210.287	-30.7411	-10.1454	-0.6859	-0.7341
11573	106.187500	27.020833	1228.340	-30.6802	-3.6100	0.6175	0.7001
11574	106.229167	27.020833	1247.396	-30.6183	1.9480	1.7425	1.9451
11575	106.270833	27.020833	1244.440	-30.5729	3.5017	2.0024	2.2364
11576	106.312500	27.020833	1199.469	-30.5503	-0.1382	1.0932	1.2296
11577	106.354167	27.020833	1183.494	-30.5360	-6.8208	-0.4436	-0.4670
11578	106.395833	27.020833	1109.535	-30.4998	-11.3515	-1.4961	-1.6243
11579	106.437500	27.020833	1000.613	-30.4157	-8.9350	-1.1580	-1.2536
11580	106.479167	27.020833	1135.735	-30.2841	0.8626	0.4426	0.5050
11581	106.520833	27.020833	1249.869	-30.1357	11.6378	2.4377	2.7100
11582	106.562500	27.020833	1251.986	-30.0096	17.2750	3.1842	3.5191
11583	106.604167	27.020833	1289.077	-29.9216	15.2947	2.2168	2.4126
11584	106.645833	27.020833	1292.154	-29.8523	10.0757	0.5266	0.5016
11585	106.687500	27.020833	1228.242	-29.7662	8.2597	-0.1705	-0.2775
11586	106.729167	27.020833	1211.352	-29.6471	13.0764	0.8541	0.8714
11587	106.770833	27.020833	1339.471	-29.5138	20.7468	2.8368	3.0884



- The radial gradient continuation method adopts the gradient of the observed field element to make analytical continuation, which is suitable for the upward and downward analytical continuation of ground, flight altitude and near range (10km).
- The main components of the field element gradient are short-wave and ultra-short-wave, and the integral radius for radial gradient calculation generally does not need to be large. Therefore, the analytical continuation by the radial gradient method is conducive to the efficient usage of gravity field observation resources.

Gross error detection on observations based on low-pass reference surface

Open file Save as Import parameters Start Computation Save process Follow example



Gross error detection on observations based on low-pass reference surface

Estimation of observation weight with specified reference attribute

Gridding of heterogeneous data by basis function weighted interpolation

Save computation process as

The discrete point file to be detect

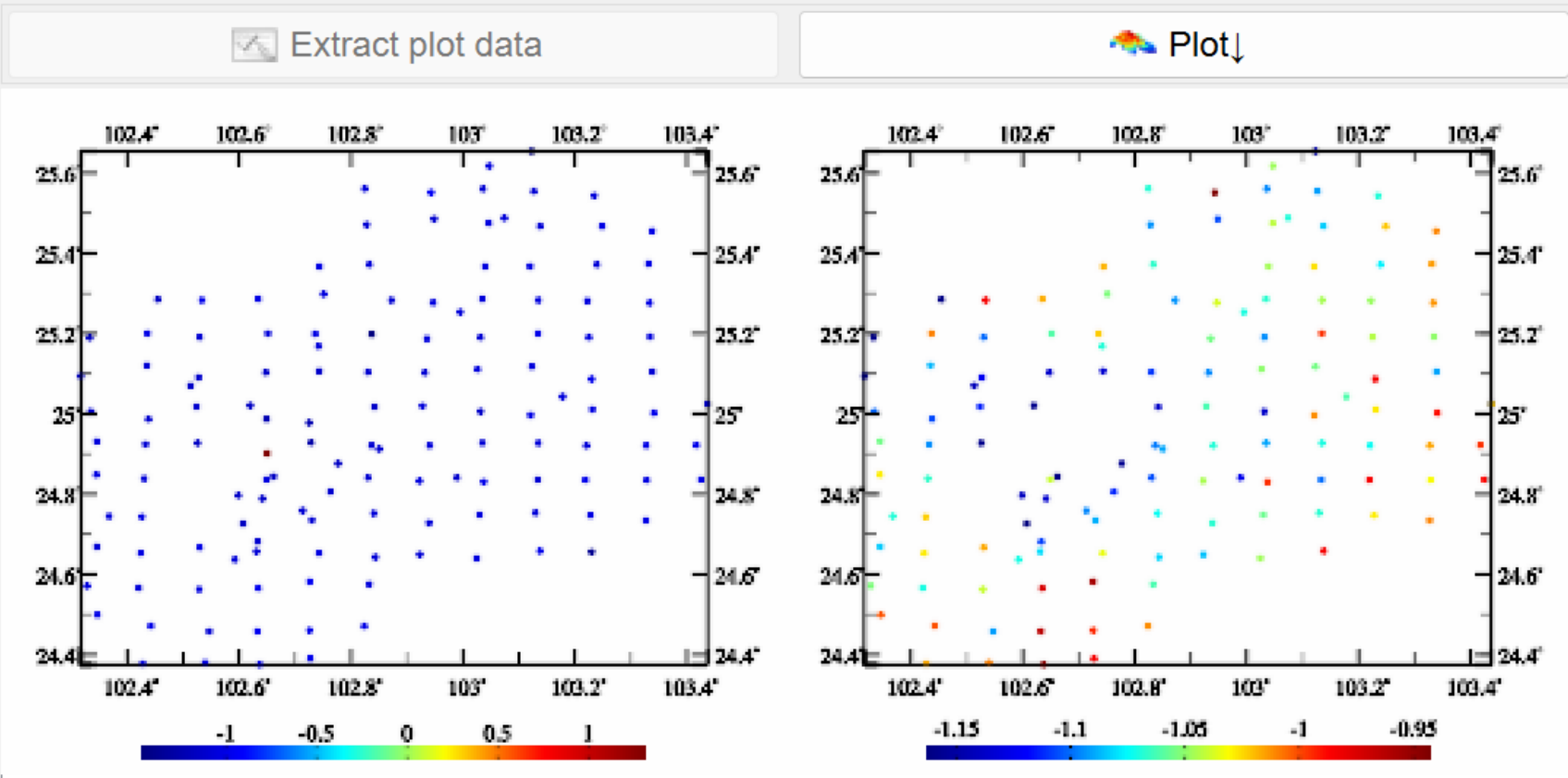
Number of rows of file header: 1
 Column ordinal number of the attribute to be detect: 5
 Beyond multiples of the standard deviation n: 3.0

Open low-pass reference surface grid file

Save the results as
 Save gross error as
 Import setting parameters
 Start Computation

>> Select the computation function from the three control buttons at the top of the interface...
 >> [Function] Select the low-pass grid as the reference surface, interpolate the reference value of the specified attribute value at the discrete point, and then detect and separate the gross error records according to the statistical properties of the differences between the specified attribute value and reference value.
 ** The reference surface can be constructed from discrete data by simple gridding and then low-pass filtering, and can also be the specified attribute grid constructed by weighted basis function gridding.
 >> Open the discrete geodetic file C:/PAGravf4.5_win64en/examples/PrGerrweighgriddat/pntdata.txt.
 ** Look at the file information in the window below and set the discrete point file format...
 >> Open low-pass reference surface grid file C:/PAGravf4.5_win64en/examples/PrGerrweighgriddat/lowpass.dat.
 >> Save the results as C:/PAGravf4.5_win64en/examples/PrGerrweighgriddat/pntdatanoerr.txt.
 >> Save no gross error results as C:/PAGravf4.5_win64en/examples/PrGerrweighgriddat/pntdataerror.txt.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-21 20:47:27
 >> Complete computation!
 >> Computation end time: 2024-09-21 20:47:27

	-0.9976	0.0517	-1.1347	-0.8754	
38	102.650330	24.901415	1906.8332	1.3251	-2.4011
39	102.728540	24.928290	1854.5060	-1.2841	-0.5680
51	102.725170	24.977718	1855.6502	-1.2383	-0.6228
70	102.837115	25.198024	1936.8741	-1.4671	-2.1049
112	103.229955	24.655854	1609.7162	-1.3869	-1.8896
2001	102.648977	24.986605	1856.7693	-1.2340	-1.4254



Source observations input

Observations without gross error

Estimation of observation weight with specified reference attribute

Open file Save as Import parameters Start Computation Save process Follow example



Gross error detection on observations based on low-pass reference surface

Estimation of observation weight with specified reference attribute

Gridding of heterogeneous data by basis function weighted interpolation

Save computation process as

The discrete geodetic observation file

Number of rows of file header

Column ordinal number of the reference attribute

Smoothing factor of weight function a

Weigh function $w(x, a) = 10\sigma / \sqrt{\sigma^2 + (ax)^2}$. Here, x is the given attribute, a is the smoothing factor of the weigh function, σ is the standard deviation of x calculated by the function module.

```
>> Save the results as C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntdatanoerr.txt.
>> Save no gross error results as C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntdataerror.txt.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-21 20:47:27
>> Complete computation!
>> Computation end time: 2024-09-21 20:47:27
>> [Function] Using the weight function defined by PAGrav4.5, estimate the observation weight according to the statistical property of the specified reference attribute in the input geodetic record file.
>> Open the discrete geodetic file C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntdatanoerr.txt.
** Look at the file information in the window below and set the discrete point file format...
>> Save the results as C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntwghrst.txt.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-21 20:49:27
>> Complete computation!
>> Computation end time: 2024-09-21 20:49:27
```

Save the results as

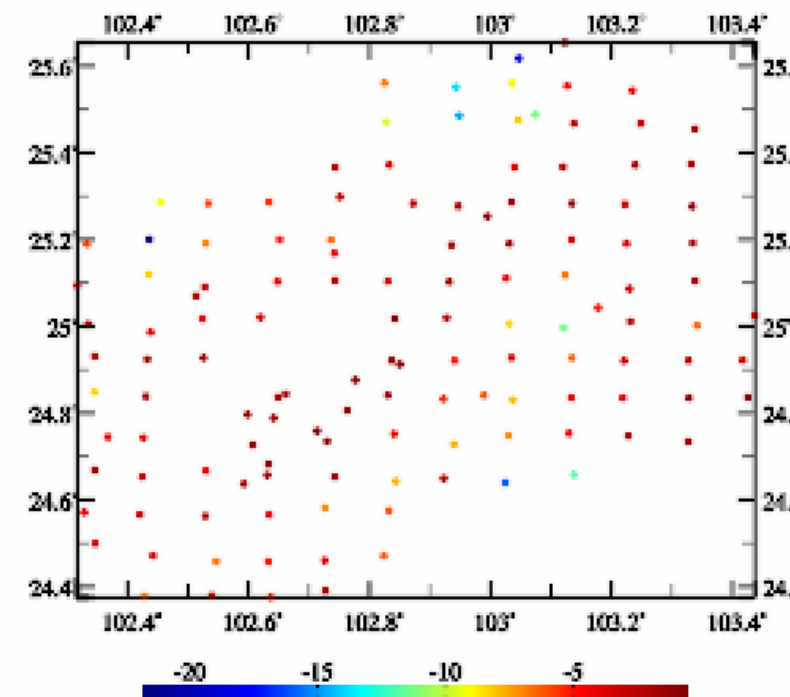
Import setting parameters

Start Computation

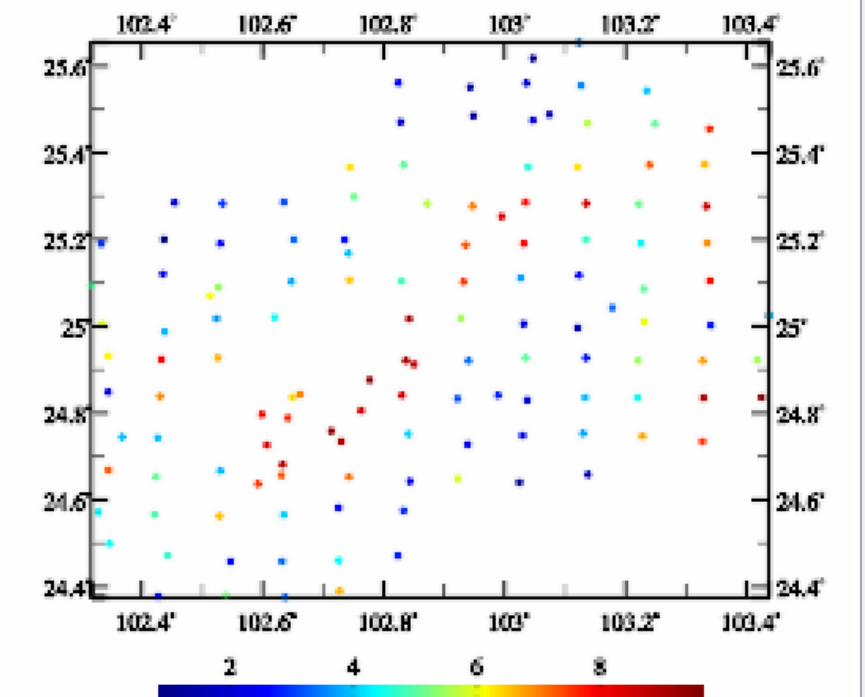
r	lon(deg/decimal)	lat	ellipHeight(m)	rntKsi(m)	TerEff(mGal)	
1	102.442457	24.471769	1972.7703	-1.0013	-3.3508	4.70
2	102.546777	24.458002	1659.0410	-1.0916	-6.6124	2.60
3	102.632412	24.458211	2120.2558	-0.9639	-5.0422	3.33
4	102.725921	24.460578	2111.3872	-0.9936	-3.6867	4.35
5	102.420803	24.566357	1990.6386	-1.0706	-3.1489	4.93
6	102.528697	24.562786	1936.4260	-1.0402	-2.0473	6.57
7	102.634437	24.565660	2192.9271	-0.9743	-4.0534	4.02
8	102.725888	24.581970	2303.7797	-0.9566	-7.1388	2.42
9	102.832641	24.575505	1977.4949	-1.0619	-5.9858	2.85
10	102.345532	24.668953	1919.7825	-1.0840	-1.6645	7.31
11	102.423972	24.652933	1959.3369	-1.0281	-3.0476	5.05
12	102.529771	24.667079	2157.7877	-1.0165	-4.2396	3.88
13	102.631063	24.657055	1906.3415	-1.0806	-1.6637	7.31
14	102.742718	24.652871	1935.7882	-1.0343	-1.7419	7.15
15	102.843573	24.642787	1880.7707	-1.0819	-7.7294	2.25
16	103.137778	24.658224	1838.4387	-0.9843	-11.7862	1.50
17	102.426305	24.743284	1929.0475	-1.0229	-4.1779	3.92
18	102.729945	24.734909	1856.2213	-1.0884	-0.8096	9.10
19	102.840819	24.752018	2117.8582	-1.0735	-3.9704	4.09
20	102.939253	24.728089	2050.9590	-1.0675	-7.6863	2.26

Extract plot data

Plot



Reference value of attribute



Observation weights

Gridding of heterogeneous data by basis function weighted interpolation

Open file Save as Import parameters Start Computation Save process Follow example

Gross error detection on observations based on low-pass reference surface

Estimation of observation weight with specified reference attribute

Gridding of heterogeneous data by basis function weighted interpolation

Save computation process as

The discrete geodetic observation file

Number of rows of file header 1

Column ordinal number of the attribute to be grid 5

Select the basis function

Cosine function Equal weight

```
>> Complete computation!
>> Computation end time: 2024-09-21 20:49:27
>> [Function] According to the given grid specification (grid range and spatial resolution), and specified basis function, grid the specified attribute in the input discrete geodetic point file by the weighted basis function interpolation method.
>> Open the discrete geodetic file C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntwghrst.txt.
** Look at the file information in the window below and set the discrete point file format...
>> Save the results as C:/PAGrav4.5_win64en/examples/PrGerrweighgrdate/pntgrid.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-21 20:52:28
>> Complete computation!
>> Computation end time: 2024-09-21 20:52:30
```

Save the results as

Import setting parameters

Start Computation

Set parameters

Column ordinal number of weight 7

Number of neighboring points 50

Kurtosis of basis function [1,20] 2

Grid specification

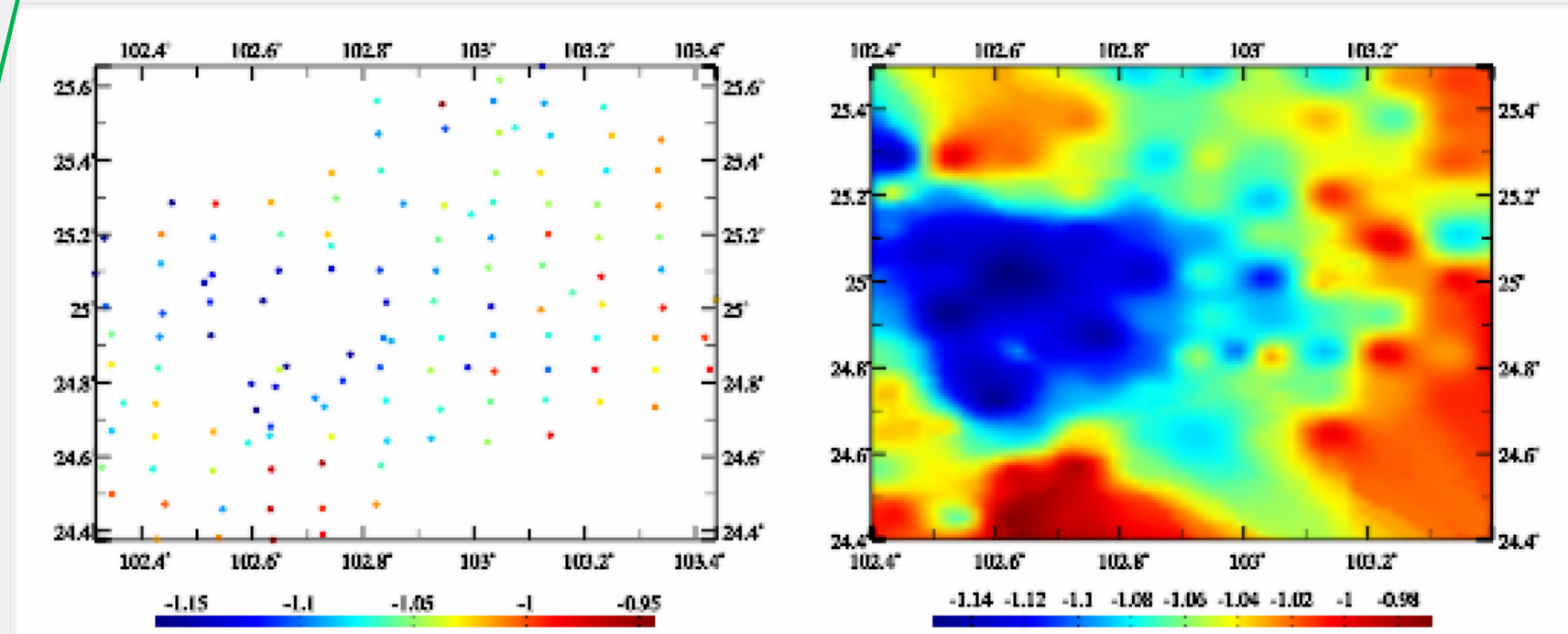
maxLat 25.500°
 minLon resolution maxLon 102.400° 1.000' 103.400°
 minLat 24.400°

Extract plot data

Plot

```
102.400000 103.400000 24.400000 25.500000 0.01666667 0.
-1.0121 -1.0132 -1.0143 -1.0161 -1.017
-0.9700 -0.9748 -0.9797 -0.9827 -0.984
-1.0080 -1.0163 -1.0193 -1.0209 -1.026
-1.0486 -1.0472 -1.0383 -1.0370 -1.034
-1.0098 -1.0101 -1.0123 -1.0145 -1.018
-0.9744 -0.9781 -0.9810 -0.9843 -0.985
-1.0149 -1.0206 -1.0209 -1.0267 -1.032
-1.0473 -1.0402 -1.0373 -1.0348 -1.034
-1.0100 -1.0081 -1.0090 -1.0113 -1.016
-0.9756 -0.9789 -0.9840 -0.9865 -0.988
-1.0200 -1.0225 -1.0267 -1.0324 -1.035
```

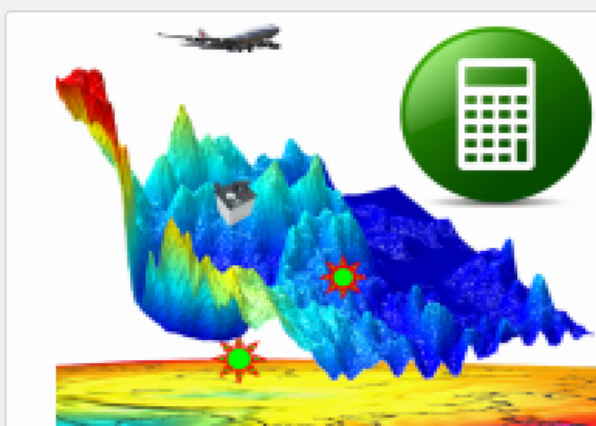
number	lon(deg/decimal)	lat	ellipHeight (m)	nntKsi (m)	TerEff (mGal)
1	102.442457	24.471769	1972.7703	-1.0013	4.70
2	102.546777	24.458002	1659.0410	-1.0916	2.60
3	102.632412	24.458211	2120.2558	-0.9639	3.33
4	102.725921	24.460578	2111.3872	-0.9936	4.35
5	102.420803	24.566357	1990.6386	-1.0706	4.93
6	102.528697	24.562786	1936.4260	-1.0402	6.57
7	102.634437	24.565660	2192.9271	-0.9743	4.02
8	102.725888	24.581970	2303.7797	-0.9566	2.42
9	102.832641	24.575505	1977.4949	-1.0619	2.85



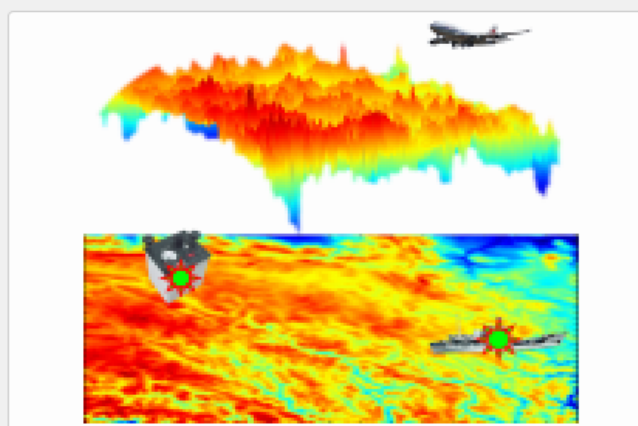
Source observations input

Gridding results

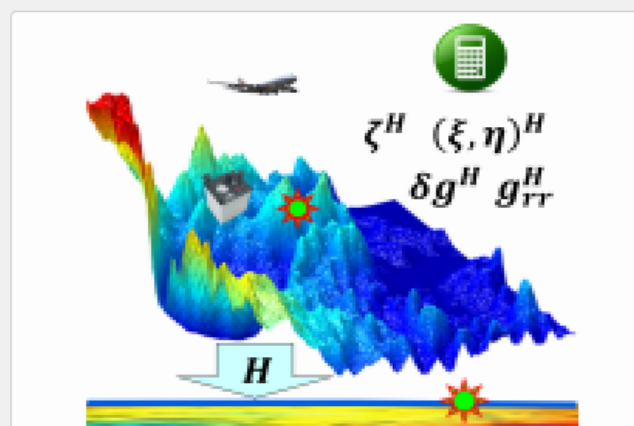
Computation of various terrain effects on various field elements outside geoid



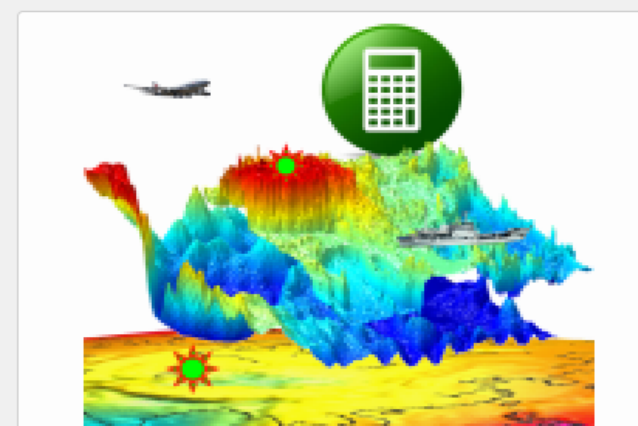
Computation of local terrain effect on various field elements on or outside the geoid



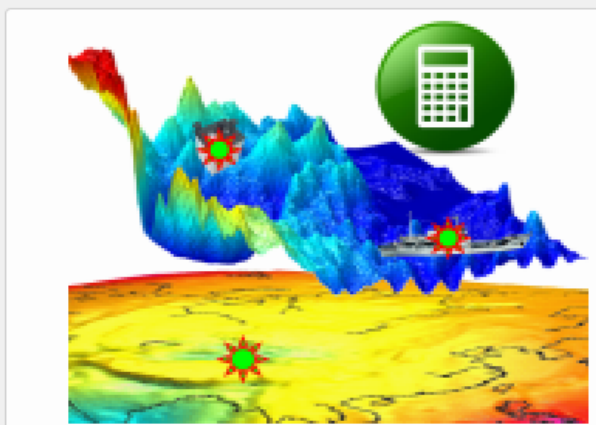
Integral of land, ocean and lake complete Bouguer effect on gravity outside geoid



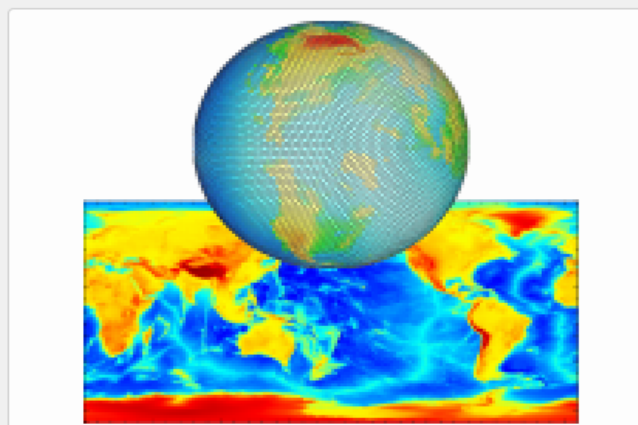
Computation of terrain Helmert condensation effect on various field elements outside geoid



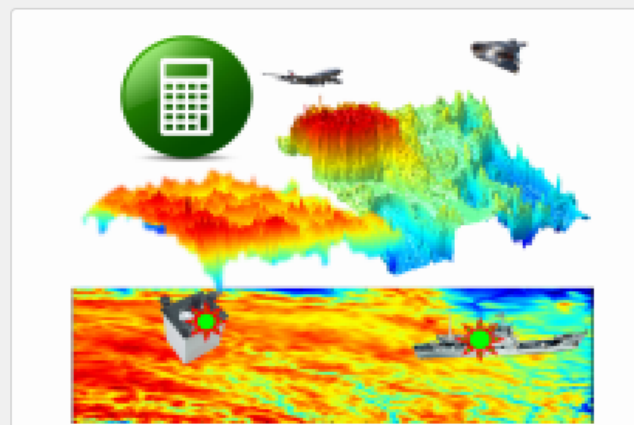
Computation of residual terrain effect on various field elements outside geoid



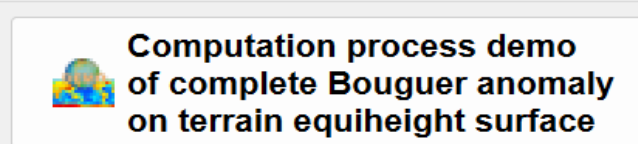
Computation of land-sea unified classical gravity Bouguer / equilibrium effect



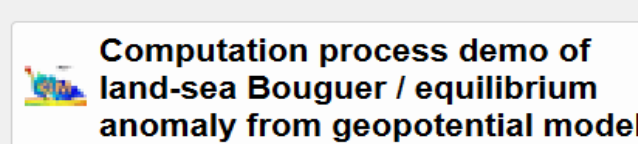
Ultrahigh degree spherical harmonic analysis on land-sea terrain and construction of model



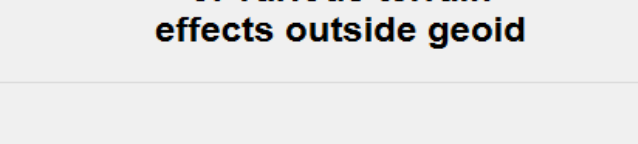
Spherical harmonic synthesis of complete Bouguer or residual terrain effects



Computation process demo of complete Bouguer anomaly on terrain equiheight surface



Computation process demo of land-sea Bouguer / equilibrium anomaly from geopotential model



Computation process demo of various terrain effects outside geoid

- Cross aliasing of heterogeneous observations in land-sea-space
- Full analytical compatibility and algorithm performance control

- Various terrain effects on all-element gravity field in whole space
- Gravity prospecting modelling from heterogeneous observations

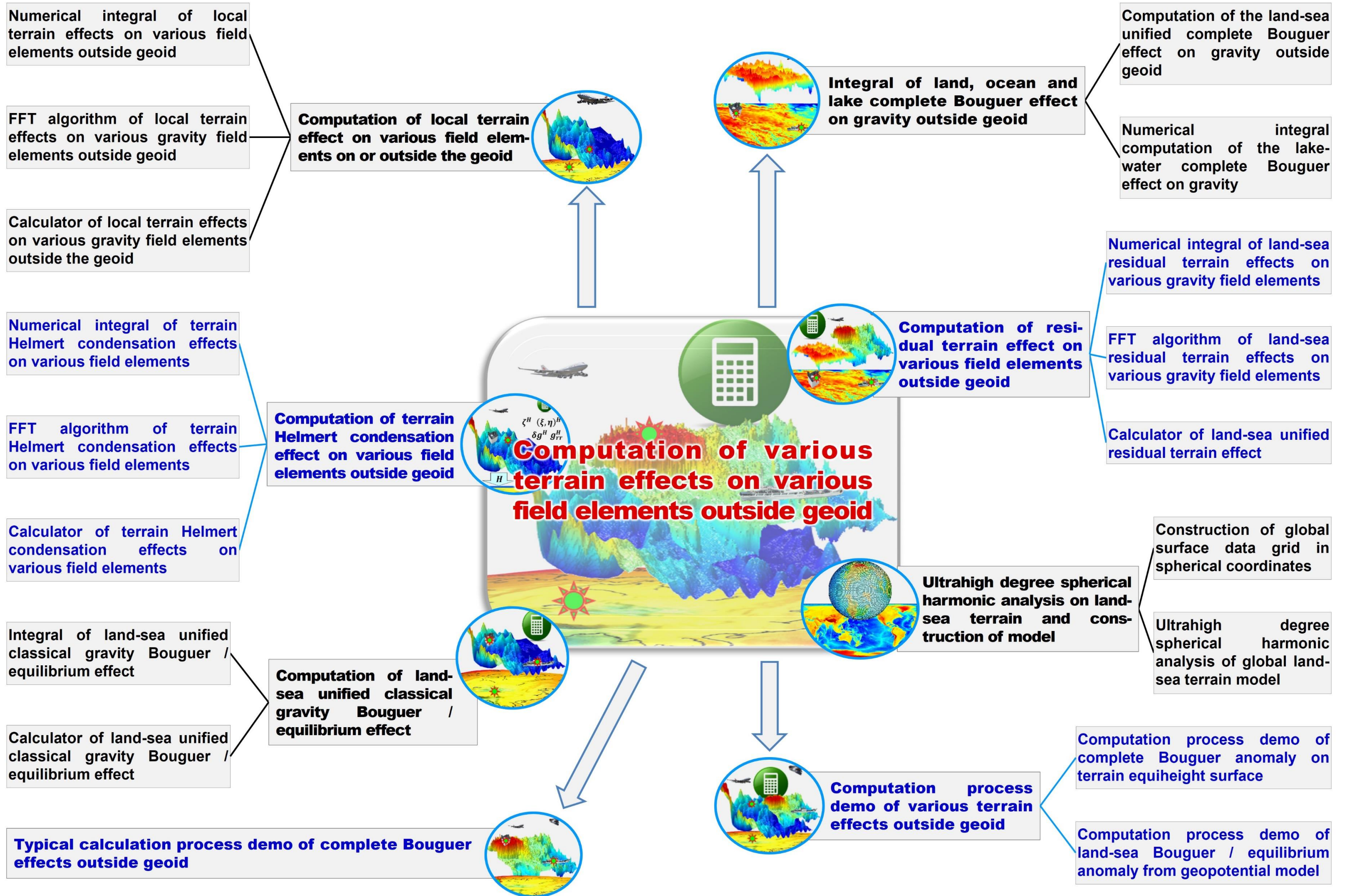
Programs and functions structure of the subsystem

Quantitative criterions for terrain effects defined by PAGravf4.5

(1) In order to improve the gridding performance of discrete field elements, it is expected to improve the smoothness of discrete field elements after the terrain effect removed. In this case, the optimal criterion for terrain effect is that the standard deviation of discrete field elements would decrease after the terrain effect removed. This quantitative criterion is also applicable for gravity prospecting modelling.

(2) The terrain effect is expected to consist of only ultrashort wave components for gravity field approach purpose, so the optimal criterion should be that the standard deviation of field elements after the terrain effect removed would decrease, and the statistical mean of terrain effects in the range of tens of kilometers is small.

The normal gravity field is the agreed starting datum for the anomalous gravity field, and there is no terrain effect on the normal gravity field. Therefore, the terrain effects on the gravity, gravity disturbance and gravity anomaly anywhere are exact equal, that on the geopotential and disturbing geopotential and that on the gravity gradient and disturbing gravity gradient are also equal, respectively.



Numerical integral of local terrain effects on various field elements outside geoid

Open DEM Import parameters Save as Start Computation Save process Follow example



Numerical integral of local terrain effects on various field elements outside geoid

FFT algorithm of local terrain effects on various field elements outside geoid

Calculator of local terrain effects on various field elements outside geoid

Algorithms of local terrain effect

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Select calculation point file format

discrete calculation point file

Open space calculation point file

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (")
- disturbing gravity gradient (E, radial)

>> Computation Process ** Operation Prompts

>> [Function] Using the rigorous numerical integral algorithm, from the ground digital elevation model and ground ellipsoidal height grid, compute the local terrain effects on the height anomaly (m), gravity (anomaly/disturbance, mGal), vertical deflection (", to south, to west) or (disturbing) gravity gradient (E, radial) on or outside the geoid.

** Input the ground digital elevation model and ground ellipsoidal height grid file with the same grid specifications...

>> Open ground digital elevation model file C:/PAGrav4.5_win64en/examples/TerLocalterraininfl/landtm1m.dat.

>> Open ground ellipsoidal height grid file C:/PAGrav4.5_win64en/examples/TerLocalterraininfl/landbmsurfhgt.dat.

>> Open calculation point position file C:/PAGrav4.5_win64en/examples/TerLocalterraininfl/surfhgt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/TerLocalterraininfl/surnintg.txt.

** Behind the source calculation point file record, appends several columns of local terrain effects on specified types of field elements, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button

Integral radius 90 km

Save the results as

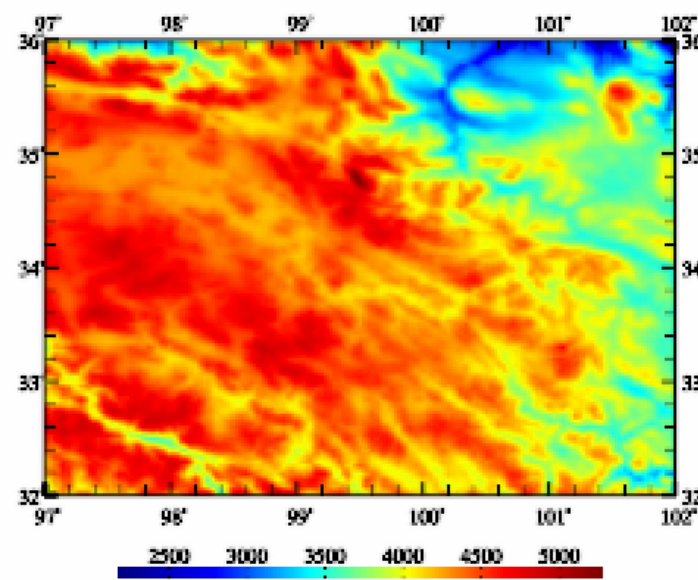
Import setting parameters

Start Computation

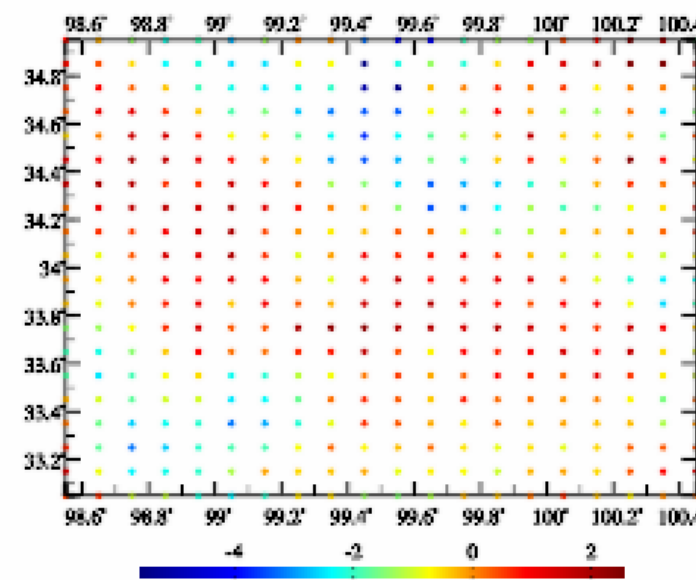
number	long(deg/decimal)	lat	ellipHeight(m)						
1	98.550000	33.050000	4372.431	0.4748	-0.6543	-4.3693	0.2496	1.4964	
2	98.650000	33.050000	4372.834	0.6019	-0.3868	-5.4945	-3.2741	0.2816	
3	98.750000	33.050000	4530.959	-1.0367	-2.0958	-6.5741	-4.6892	-1.4646	
4	98.850000	33.050000	4567.407	-1.0858	-2.0675	-6.9916	-1.1745	22.7751	
5	98.950000	33.050000	4646.551	-2.1223	-3.3753	-7.5768	-2.4547	7.9308	
6	99.050000	33.050000	4672.380	-2.4157	-2.7630	-4.5712	1.0716	11.8263	
7	99.150000	33.050000	4611.765	-2.0435	-2.6243	-0.6258	2.7601	-6.5803	

Extract effects

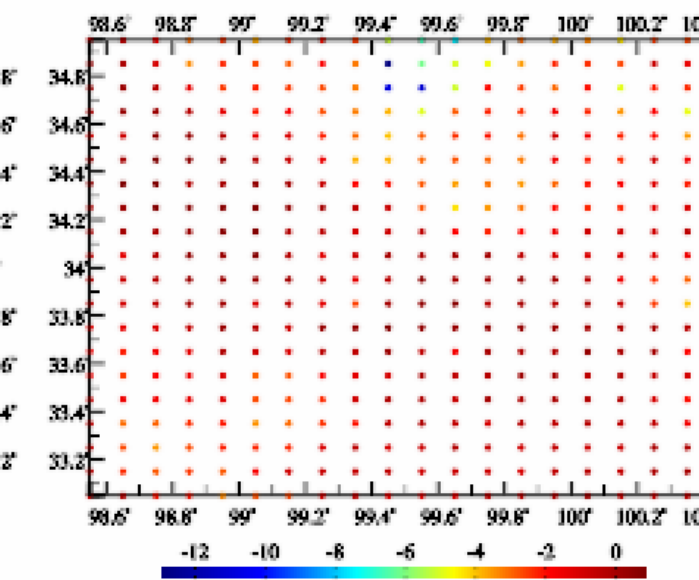
Plot



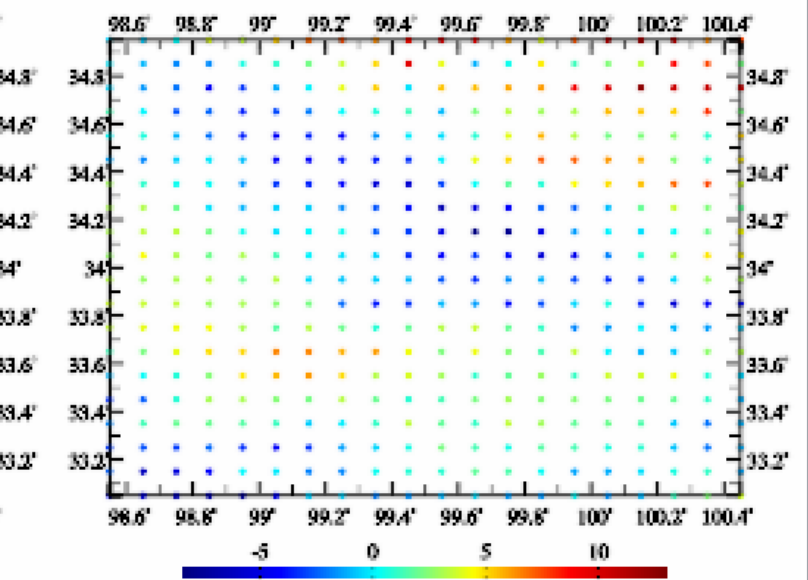
Digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (", S)

- The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.
- Within the integral radius of the grid margin of the ground digital elevation model, there is the integral edge effect. The local terrain effect on gravity is approximately equal to the linear Molodensky I term. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

Numerical integral of local terrain effects on various field elements outside geoid

Open DEM Import parameters Save as Start Computation Save process Follow example



Numerical integral of local terrain effects on various field elements outside geoid

FFT algorithm of local terrain effects on various field elements outside geoid

Calculator of local terrain effects on various field elements outside geoid

Algorithms of local terrain effect

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Select calculation point file format
ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (")
- disturbing gravity gradient (E, radial)

>> Computation Process ** Operation Prompts

>> [Function] Using the rigorous numerical integral algorithm, from the ground digital elevation model and ground ellipsoidal height grid, compute the local terrain effects on the height anomaly (m), gravity (anomaly/disturbance, mGal), vertical deflection (", to south, to west) or (disturbing) gravity gradient (E, radial) on or outside the geoid.

** Input the ground digital elevation model and ground ellipsoidal height grid file with the same grid specifications...

>> Open ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landtm1m.dat.
 >> Open ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landbmsurfhgt.dat.
 >> Open ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landbmsurfhgt.dat.
 >> Save the results as C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfnintg.dat.

** At the same time, the program also outputs the local terrain effect grid files on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the local terrain effect grid files on the specified types of elements.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button

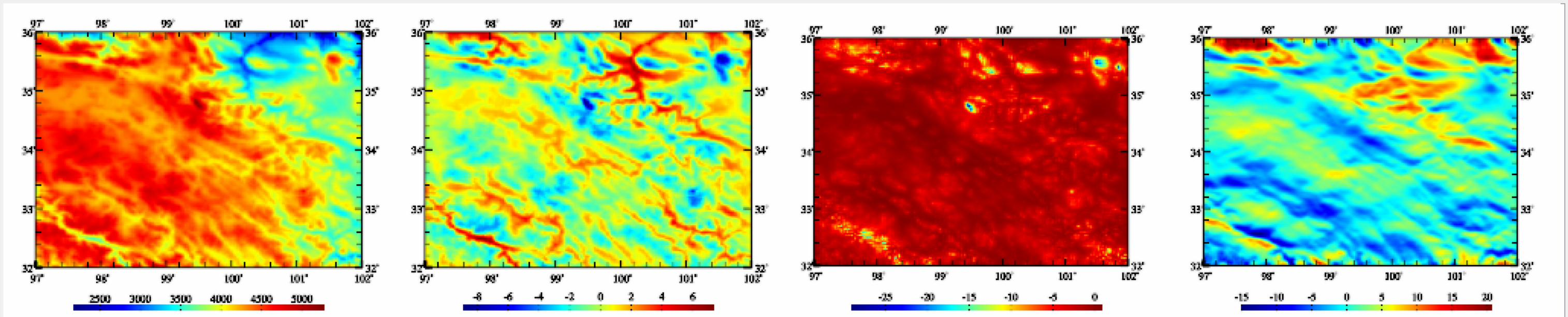
Integral radius 90 km

Save the results as Import setting parameters

Start Computation

C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfnintg.ksi
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfnintg.gra
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfnintg.dft
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfnintg.grr

Extract effects Plot



Digital elevation model (m)

height anomaly (m)

gravity (anomaly, mGal)

vertical deflection (", S)

- The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.
- Within the integral radius of the grid margin of the ground digital elevation model, there is the integral edge effect. The local terrain effect on gravity is approximately equal to the linear Molodensky I term. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

FFT algorithm of local terrain effects on various gravity field elements outside geoid

Numerical integral of local terrain effects on various field elements outside geoid

FFT algorithm of local terrain effects on various field elements outside geoid

Calculator of local terrain effects on various field elements outside geoid

Algorithms of local terrain effect

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (")
- disturbing gravity gradient (E, radial)

Fast algorithm 2D FFT

>> Computation Process ** Operation Prompts

>> Open ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landtm1m.dat.
 >> Open ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landbmsurfhgt.dat.
 >> Open ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landgeoidhgt.dat.

** Look at the file information in the window below, set the input file format parameters...

>> Compute the local terrain effects using 2D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT2.txt.

** At the same time, the program also outputs the local terrain effect grid files on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the local terrain effect grid files on the specified types of elements.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:44:54

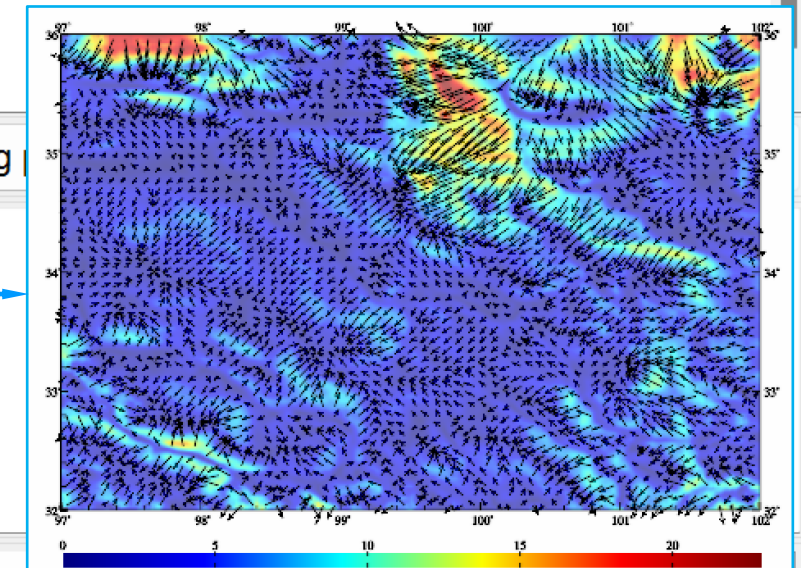
>> Complete the computation of the local terrain effect!

Integral radius 90 km

Save the results as

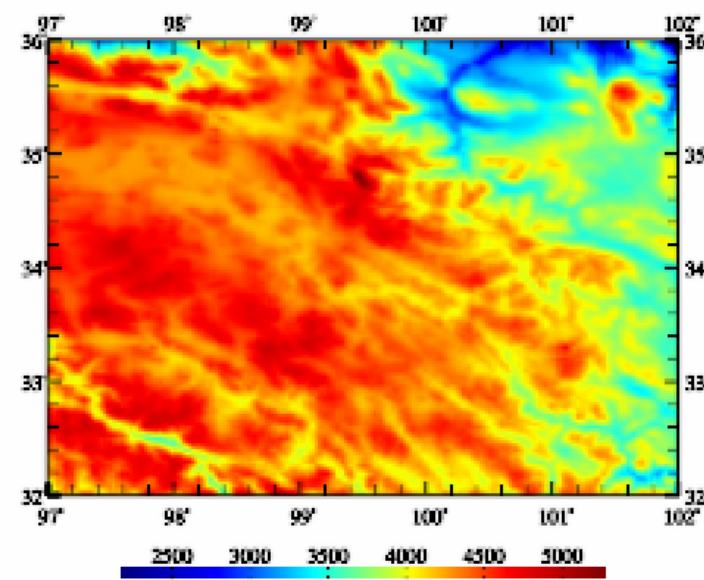
Import setting

C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT2.ksi
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT2.gra
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT2.dft
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT2.grr

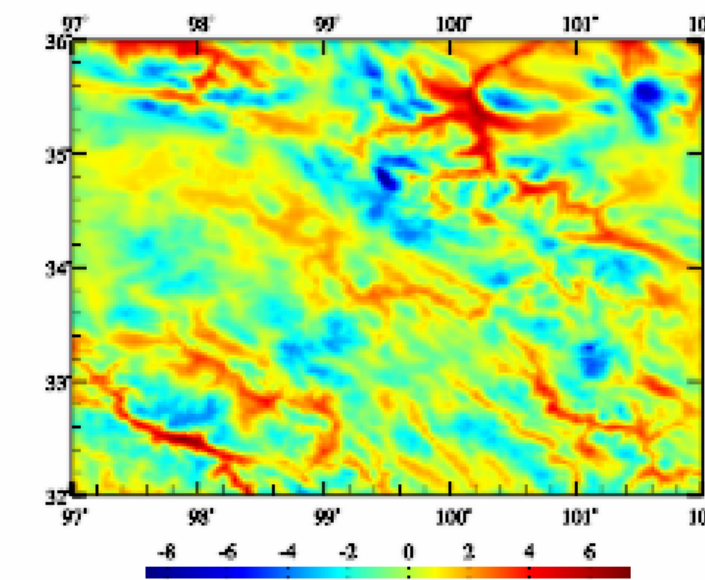


Extract effects

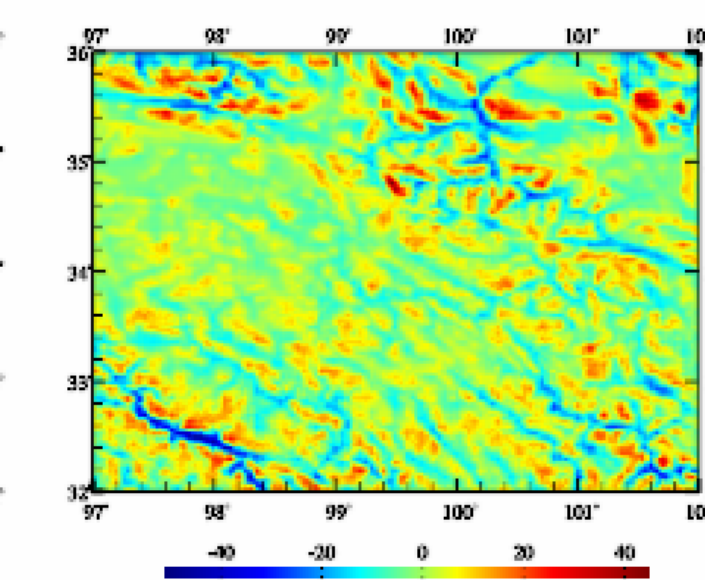
Plot



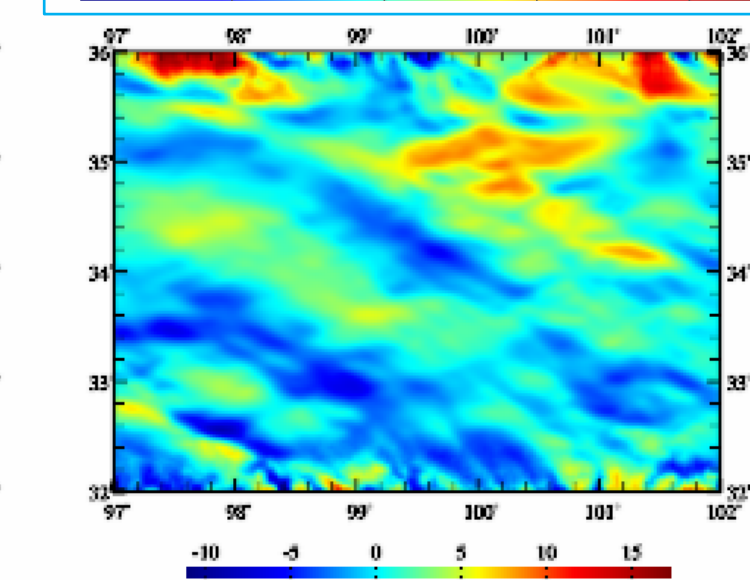
Digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (", S)

- The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.
- Within the integral radius of the grid margin of the ground digital elevation model, there is the integral edge effect. The local terrain effect on gravity is approximately equal to the linear Molodensky I term. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

FFT algorithm of local terrain effects on various gravity field elements outside geoid

Open DEM Import parameters Save as Start Computation Save process Follow example

Numerical integral of local terrain effects on various field elements outside geoid

FFT algorithm of local terrain effects on various field elements outside geoid

Calculator of local terrain effects on various field elements outside geoid

Precise Approach of Earth Gravity Field and Geoid
PAGrav4.5
 Algorithms of local terrain effect
 Chinese Academy of Surveying & Mapping
 October 2024, Beijing, China

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (")
- disturbing gravity gradient (E, radial)

Fast algorithm 1D FFT

>> Computation Process ** Operation Prompts

>> Open ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landtm1m.dat.
 >> Open ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landbmsurfhgt.dat.
 >> Open ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/landgeoidhgt.dat.

** Look at the file information in the window below, set the input file format parameters...
 >> Compute the local terrain effects using 1D FFT algorithm...
 >> Save the results as C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT1.txt.
 ** At the same time, the program also outputs the local terrain effect grid files on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the local terrain effect grid files on the specified types of elements.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:46:38

>> Complete the computation of the local terrain effect!

Integral radius 90 km

Save the results as

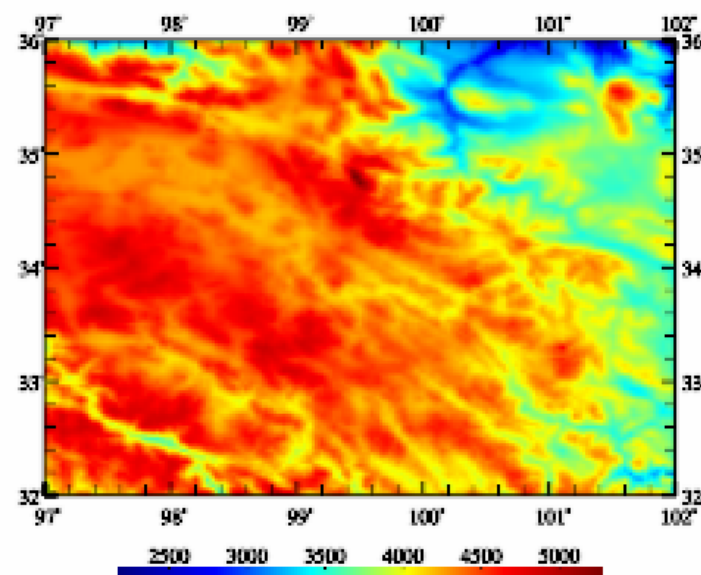
Import setting parameters

Start Computation

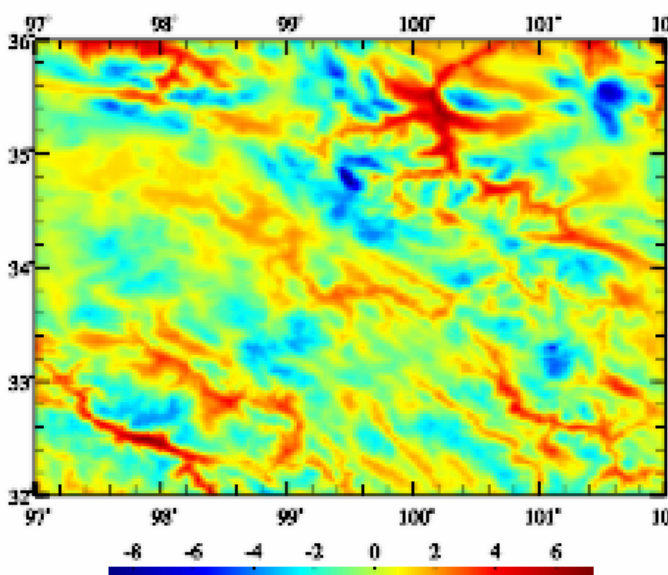
C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT1.ksi
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT1.gra
 C:/PAGravf4.5_win64en/examples/TerLocalterraininfl/surfFFT1.grr

Extract effects

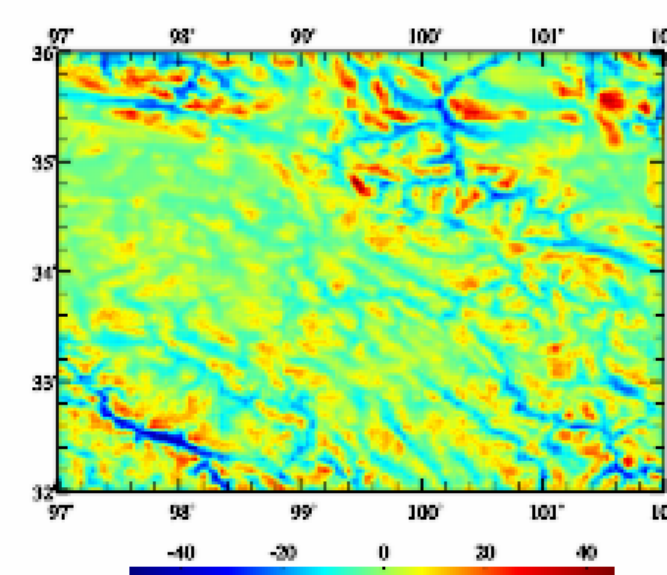
Plot



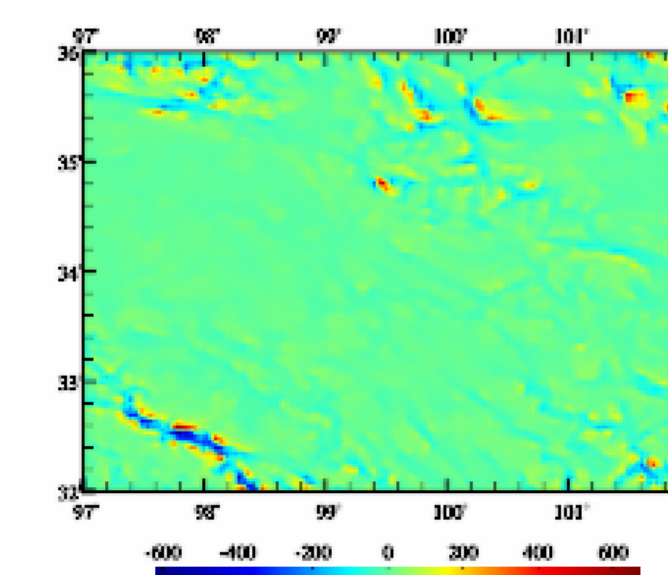
Digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)



(disturbing) gradient (E, R)

- The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.
- Within the integral radius of the grid margin of the ground digital elevation model, there is the integral edge effect. The local terrain effect on gravity is approximately equal to the linear Molodensky I term. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

Calculator of local terrain effects on various gravity field elements outside the geoid

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Input geodetic coordinates of calculation point

longitude 98.240000°

latitude 32.428000°

ellipsoidal height 2017.830m

Integral radius 90 km

Start calculation

Ground digital elevation model

97.000000	102.000000	32.000000	36.000000	0.01666667	0.01666667	
3988.0003	4048.9987	4129.9921	4151.9956	4155.9995	4177.9961	41
4277.9980	4373.9953	4466.9865	4479.9931	4520.9918	4547.9825	44
4242.0005	4229.0008	4211.0001	4165.0054	4150.0047	4157.0059	41
4429.0008	4511.9959	4529.9991	4531.0011	4539.9993	4531.9988	45
4273.0028	4221.0056	4196.0075		4251.0050	4337.9987	43
4643.9962	4607.0004	4605.9961		4457.0003	4379.9835	41
4500.0065	4593.9999			4485.9976	4473.0101	44
4272.0146	4409.0000			4400.0046	4729.0038	48
4530.9966	4456.9999			4442.0000	4071.0117	40
4371.0006	4429.9977				4520.9942	44
3868.0107	3964.9992				4124.0006	41
4243.0076	4270.0056	4353.9999			4347.9933	42
4161.9980	4189.9937	4163.9999		4143.9926	4040.0077	40
4050.9965	4023.0017	4012.0000	4029.9996	4171.9934	4235.0039	43
4051.0030	4022.0027	3977.0121	4029.9996	4032.9988	3996.0025	39
4299.0025	4415.9991	4516.9921	4514.9967	4458.0037	4431.9971	43
3672.0205	3912.9978	4073.9952	4159.0051	4313.9938	4374.9940	43
4389.9975	4386.9989	4385.9985	4382.9999	4358.9980	4337.9925	42
4185.9964	4135.0004	4099.9998	4073.9998	4073.9986	4110.9920	41

Local terrain effect calculation results

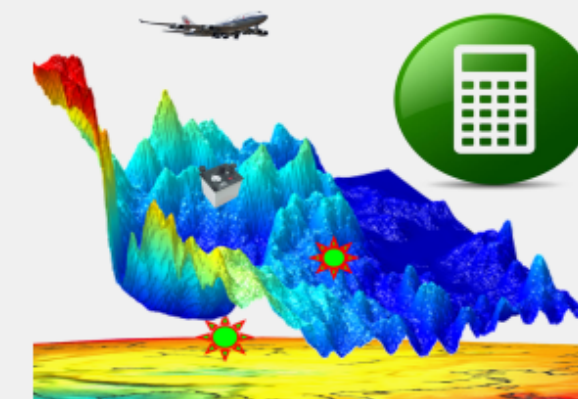
height anomaly (m) -0.1400

gravity (anomaly/disturbance, mGal) -0.8197

vertical deflection (" , S) -7.0751

vertical deflection (" , W) -0.6231

(disturbing) gradient (E, radial) 17.4820



Inputting the ground digital elevation model (standing for terrain relief) and ground geodetic ellipsoidal height grid (standing for the terrain surface location) files with the same grid specifications, the [Start Calculation] button becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the local terrain effects on various field elements at the calculation point can be computed and displayed in time.

The program allows to replace the ground digital elevation model and the ground ellipsoidal height grid file at any time from the interface, or to change the integral radius, and these user inputs will take effect at once.

The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

Calculator of local terrain effects on various gravity field elements outside the geoid

Open ground digital elevation model file

Open ground ellipsoidal height grid file

Input geodetic coordinates of calculation point

longitude 100.240000°

latitude 34.428000°

ellipsoidal height 201.830m

Integral radius 90 km

Start calculation

Ground digital elevation model

97.000000	102.000000	32.000000	36.000000	0.01666667	0.01666667	
3988.0003	4048.9987	4129.9921	4151.9956	4155.9995	4177.9961	41
4277.9980	4373.9953	4466.9865	4479.9931	4520.9918	4547.9825	44
4242.0005	4229.0008	4211.0001	4165.0054	4150.0047	4157.0059	41
4429.0008	4511.9959	4529.9991	4531.0014	4539.9993	4531.9988	45
4273.0028	4221.0056	4196.0075	4196.0093	4251.0050	4337.9987	43
4643.9962	4601.0004	4605.9961	4587.9986	4457.0003	4379.9835	41
4500.0065	4597.9997	4650.9951	4611.9989	4585.9976	4473.0101	44
4272.0146	4406.0057	4543.9991	4511.9991	4647.0046	4729.0038	48
4530.9966	4454.9979	4409.9999	4409.9999	4160.0042	4071.0117	40
4371.0006	4429.9999	4409.9999	4409.9999	4493.9994	4520.9942	44
3868.0107	3964.9999	4066.0037	4066.0037	4124.0006	4124.0006	41
4243.0076	4270.9999	4326.9999	4326.9999	4347.9933	4347.9933	42
4161.9980	4189.9999	4206.9999	4206.9999	4040.0077	4040.0077	40
4050.9965	4023.0017	4093.9999	4093.9999	4235.0039	4235.0039	43
4051.0030	4022.0027	4032.9988	4032.9988	3996.0025	3996.0025	39
4299.0025	4415.9991	4399.9999	4399.9999	4458.0037	4431.9971	43
3672.0205	3912.9978	4073.9999	4159.0051	4313.9938	4374.9940	43
4389.9975	4386.9989	4385.9955	4382.9967	4358.9980	4337.9925	42
4185.9964	4135.0004	4099.9998	4073.9998	4073.9986	4110.9920	41

Local terrain effect calculation results

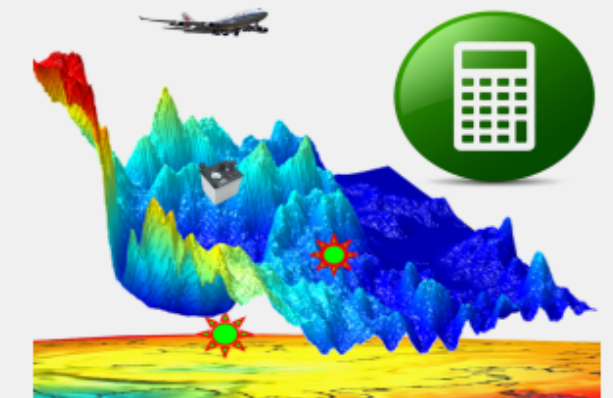
height anomaly (m) 2.3837

gravity (anomaly/disturbance, mGal) -12.3434

vertical deflection (" , S) 3.5957

vertical deflection (" , W) 5.5401

(disturbing) gradient (E, radial) -23.6988



Inputting the ground digital elevation model (standing for terrain relief) and ground geodetic ellipsoidal height grid (standing for the terrain surface location) files with the same grid specifications, the [Start Calculation] button becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the local terrain effects on various field elements at the calculation point can be computed and displayed in time.

The program allows to replace the ground digital elevation model and the ground ellipsoidal height grid file at any time from the interface, or to change the integral radius, and these user inputs will take effect at once.

The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude. There are local terrain effects in the coastal sea area, and that in the deep ocean area are equal to zero.

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid - Numerical integral

Open DTM Import parameters Save as Start Computation Save process Follow example

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Formulas of land-sea unified complete Bouguer effect

Open the land-sea terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format
discrete calculation point file

Open the calculation point location file

Set input point file format
Number of rows of file header 1
Column ordinal number of ellipsoidal height in the record 4

>> Computation Process ** Operation Prompts

>> [Function] Using the rigorous numerical integral method or FFT algorithm, from the land-sea terrain model and ellipsoidal height grid file of the land-sea surface, compute the land-sea unified complete Bouguer effect on the gravity (mGal) on the geoid or in near-Earth space.

** Input the land-sea terrain model and the ellipsoidal height grid files of the land-sea surface with the same grid specifications...

>> Open the land-sea terrain model file C:/PAGrav4.5_win64en/examples/TerCompleteBougure/dtm5m.dat.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGrav4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.

>> Open the calculation point location file C:/PAGrav4.5_win64en/examples/TerCompleteBougure/surfhgt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/TerCompleteBougure/bgpnt.txt.

>> Behind the source calculation point file record, appends the local terrain effect, spherical Bouguer effect and sea-water complete Bouguer effect, and keep 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:06:54

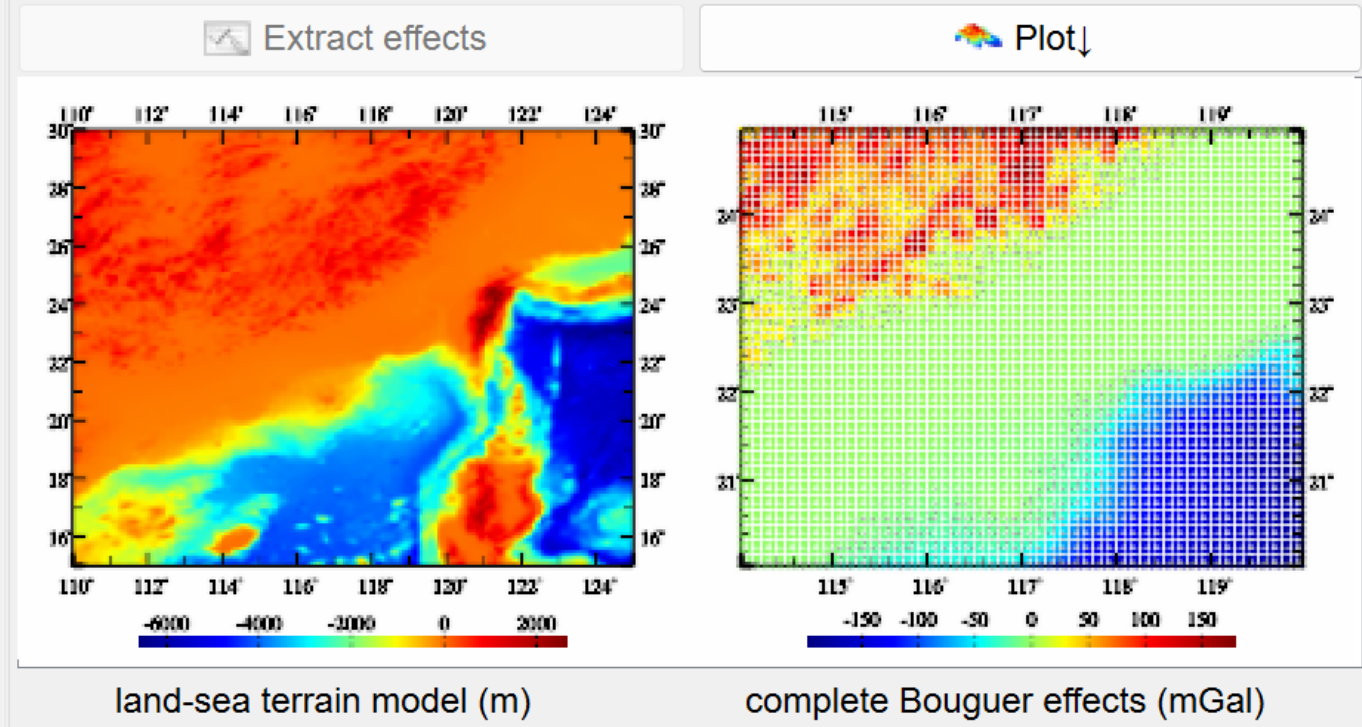
>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!

>> Computation end time: 2024-09-22 09:07:03

Land integral radius 90 km Sea integral radius 300 km

Save the results as Import setting parameters Start Computation

lon	lat	hgt				
10849	114.041667	20.041667	2.5061	0.0000	0.0000	-4.9874 -4.987
10850	114.125000	20.041667	2.8389	0.0000	0.0000	-5.7603 -5.760
10851	114.208333	20.041667	3.1673	0.0000	0.0000	-6.1912 -6.191
10852	114.291667	20.041667	3.4899	0.0000	0.0000	-5.7768 -5.776
10853	114.375000	20.041667	3.8056	0.0000	0.0000	-5.3795 -5.379
10854	114.458333	20.041667	4.1136	0.0000	0.0000	-5.3887 -5.388
10855	114.541667	20.041667	4.4137	0.0000	0.0000	-5.7310 -5.731
10856	114.625000	20.041667	4.7058	0.0000	0.0000	-6.4732 -6.473
10857	114.708333	20.041667	4.9907	0.0000	0.0000	-7.4594 -7.459
10858	114.791667	20.041667	5.2696	0.0000	0.0000	-10.2158 -10.215
10859	114.875000	20.041667	5.5440	0.0000	0.0000	-14.0367 -14.036
10860	114.958333	20.041667	5.8158	0.0000	0.0000	-17.8961 -17.896
10861	115.041667	20.041667	6.0875	0.0000	0.0000	-26.1346 -26.134
10862	115.125000	20.041667	6.3615	0.0000	0.0000	-31.5650 -31.565
10863	115.208333	20.041667	6.6404	0.0000	0.0000	-33.8370 -33.837
10864	115.291667	20.041667	6.9265	0.0000	0.0000	-33.5514 -33.551
10865	115.375000	20.041667	7.2221	0.0000	0.0000	-33.4861 -33.486



- The program is suitable for the unified computation of the complete Bouguer effect on gravity, gravity anomaly and gravity disturbance in land, land-sea junction and sea area. The calculation point may be on the geoid or in near-Earth space.
- If the ocean water depth in the land-sea terrain model is set to zero, the program automatically computes the land complete Bouguer effect in the near-Earth space. If the terrain height in the land-sea terrain model is set to zero, the program automatically computes the seawater complete Bouguer effect in the near-Earth space.
- The complete Bouguer effect here is defined as the variation of Earth gravity field because of the terrain masses above the geoid removed and the seawater density compensated to the terrain density. There is the sea water Bouguer effect in the offshore land area, while there is the local terrain effect in the coastal sea area.

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid - Numerical integral

Open DTM Import parameters Save as Start Computation Save process Follow example

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Formulas of land-sea unified complete Bouguer effect

Open the land-sea terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format

ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select integral algorithm

numerical integral

>> Computation Process ** Operation Prompts

>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!

>> Computation end time: 2024-09-22 09:07:03

>> [Function] Using the rigorous numerical integral method or FFT algorithm, from the land-sea terrain model and ellipsoidal height grid file of the land-sea surface, compute the land-sea unified complete Bouguer effect on the gravity (mGal) on the geoid or in near-Earth space.

** Input the land-sea terrain model and the ellipsoidal height grid files of the land-sea surface with the same grid specifications...

>> Open the land-sea terrain model file C:/PAGrav4.5_win64en/examples/TerCompleteBougure/dtm5m.dat.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGrav4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.

>> Open the ellipsoidal height grid file of calculation surface C:/PAGrav4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.

>> Compute the land-sea unified complete Bouguer effects using numerical integral...

>> Save the results as C:/PAGrav4.5_win64en/examples/TerCompleteBougure/Indseanintg.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:09:34

>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!

>> Computation end time: 2024-09-22 09:10:26

Land integral radius 90 km

Sea integral radius 300 km

Save the results as

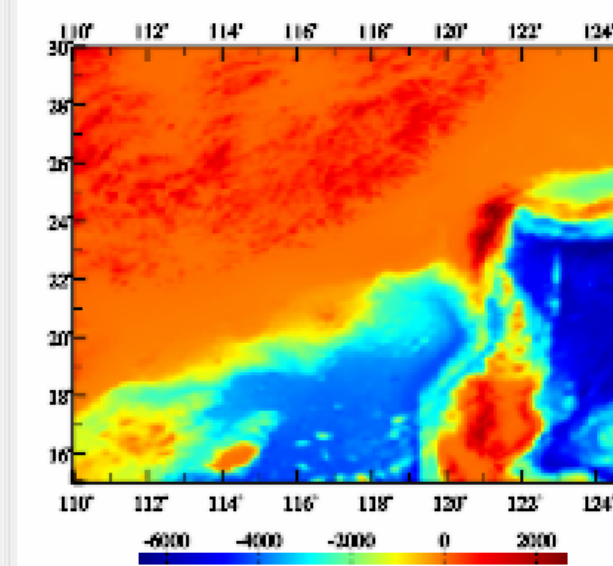
Import setting parameters

Start Computation

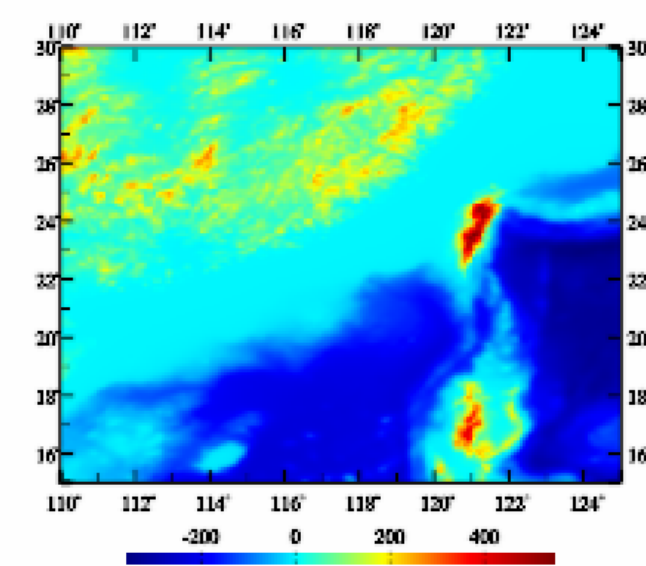
110.000000	125.000000	15.000000	30.000000	0.08333333	0.08333333	
-7.8971	-7.8766	-9.1329	-13.9564	-17.1850	-18.6294	-20.8450
-44.6578	-46.2931	-47.8725	-49.2206	-49.7490	-52.1642	-58.2028
-122.3702	-130.1366	-140.1488	-153.4317	-160.9914	-163.4580	-162.3793
-191.4158	-194.5725	-195.9800	-197.2639	-198.6141	-200.3888	-202.6294
-200.4928	-205.5214	-206.6093	-205.9741	-204.5037	-202.9258	-202.5885
-178.2261	-149.0168	-128.2677	-123.2072	-148.5989	-171.0931	-190.9696
-171.9145	-151.3418	-131.5769	-117.4720	-134.9318	-155.1051	-177.0088
-205.7689	-213.4690	-219.2022	-222.2357	-217.2625	-201.2612	-170.7498
-2.2319	37.0377	49.9421	103.4139	109.8637	67.4917	9.9533
107.4283	80.5898	76.5395	-2.8018	-3.8227	-5.0755	-5.0368
-55.8005	-60.4478	-68.3144	-80.9337	-82.7537	-79.9747	-69.3090
-80.1272	-109.2082	-131.7292	-159.3266	-177.3378	-194.1377	-219.8577
-9.7228	-9.3627	-9.8369	-13.9679	-17.8883	-19.5395	-21.4966
-44.6752	-46.2503	-47.7995	-50.0060	-49.1645	-50.0281	-49.0029
-134.8074	-139.8302	-146.6228	-160.3309	-172.5591	-178.2125	-178.0323
-193.4552	-198.5444	-202.4213	-206.8460	-210.7303	-213.6701	-216.0972
-222.1076	-225.8486	-226.2187	-224.2652	-222.6408	-222.4899	-223.7217

Extract effects

Plot



land-sea terrain model (m)



complete Bouguer effects (mGal)

- The program is suitable for the unified computation of the complete Bouguer effect on gravity, gravity anomaly and gravity disturbance in land, land-sea junction and sea area. The calculation point may be on the geoid or in near-Earth space.
- If the ocean water depth in the land-sea terrain model is set to zero, the program automatically computes the land complete Bouguer effect in the near-Earth space. If the terrain height in the land-sea terrain model is set to zero, the program automatically computes the seawater complete Bouguer effect in the near-Earth space.
- The complete Bouguer effect here is defined as the variation of Earth gravity field because of the terrain masses above the geoid removed and the seawater density compensated to the terrain density. There is the sea water Bouguer effect in the offshore land area, while there is the local terrain effect in the coastal sea area.

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid - FFT integral

Open DTM Import parameters Save as Start Computation Save process Follow example

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Formulas of land-sea unified complete Bouguer effect

Open the land-sea terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select integral algorithm
2D FFT algorithm

>> Computation Process ** Operation Prompts

>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!

>> Computation end time: 2024-09-22 09:10:26

>> [Function] Using the rigorous numerical integral method or FFT algorithm, from the land-sea terrain model and ellipsoidal height grid file of the land-sea surface, compute the land-sea unified complete Bouguer effect on the gravity (mGal) on the geoid or in near-Earth space.

** Input the land-sea terrain model and the ellipsoidal height grid files of the land-sea surface with the same grid specifications...

>> Open the land-sea terrain model file C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dtm5m.dat.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.

>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.

>> Compute the land-sea unified complete Bouguer effects using 2D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/TerCompleteBougure/IndseaFFT2.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:14:13

>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!

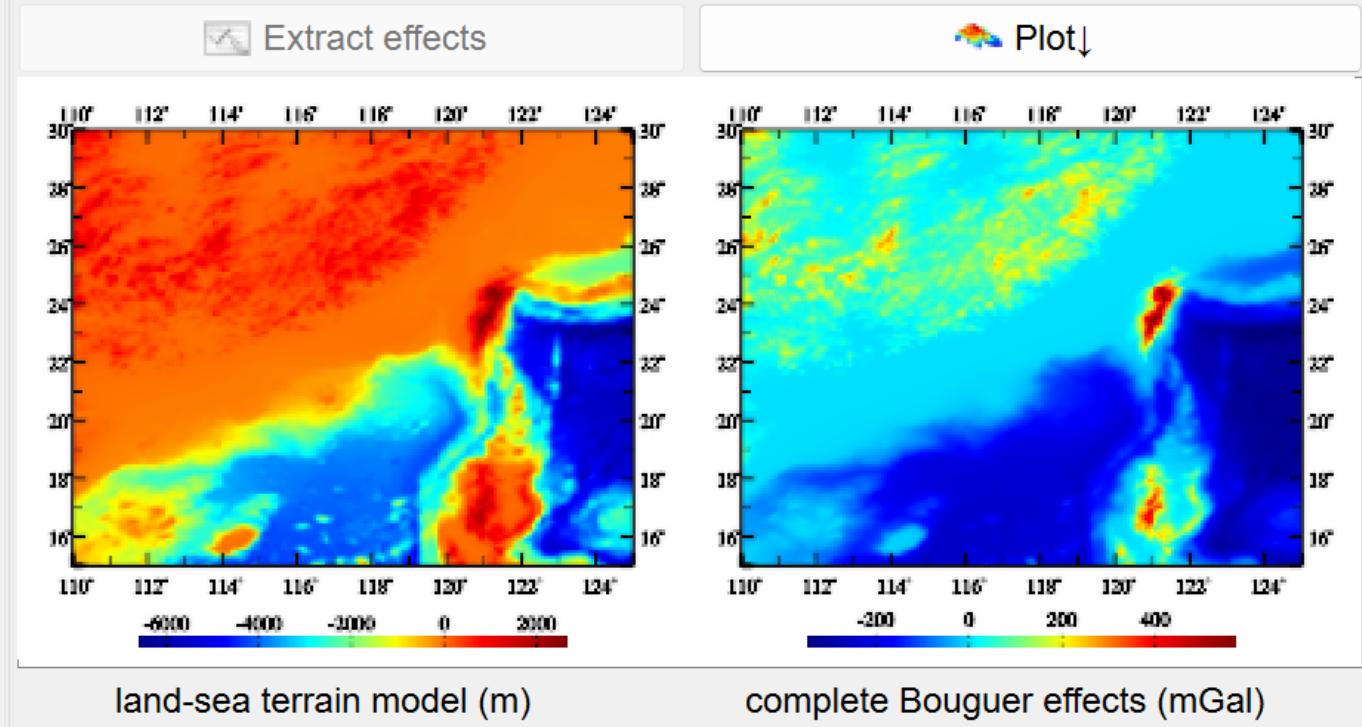
>> Computation end time: 2024-09-22 09:14:19

Save computation process as

Land integral radius 90 km Sea integral radius 300 km

Save the results as Import setting parameters Start Computation

110.000000	125.000000	15.000000	30.000000	0.08333333	0.08333333	
-8.3840	-8.4310	-9.7492	-14.6251	-17.9147	-19.4227	-21.6795
-46.0804	-47.7576	-49.3916	-50.7882	-51.3851	-53.8891	-59.9925
-125.7561	-133.7616	-144.0685	-157.5015	-165.2193	-167.7783	-166.8387
-196.6335	-199.8166	-201.3186	-202.6456	-204.0432	-205.8578	-208.1285
-206.3994	-211.4598	-212.6164	-212.0782	-210.6699	-209.1409	-208.8170
-183.9449	-154.6824	-133.6509	-128.7657	-154.2202	-177.0351	-196.9064
-177.6384	-157.0008	-136.9625	-122.9076	-140.2510	-160.7115	-182.6198
-211.3937	-218.8423	-224.2816	-227.0769	-221.9265	-205.9211	-175.6084
-3.9094	36.0852	49.2404	103.5004	110.1038	67.2428	8.8891
107.7201	80.4641	76.8699	-4.1631	-5.4744	-6.7966	-6.8071
-58.3003	-63.0309	-71.0464	-83.7201	-85.6414	-82.8324	-72.1778
-83.4268	-112.8950	-135.9738	-163.8406	-182.2737	-199.3464	-224.3924
-10.2471	-9.9652	-10.5049	-14.6940	-18.6774	-20.3997	-22.3998
-46.1861	-47.8194	-49.4312	-51.6749	-50.9006	-51.7915	-50.7816
-138.4751	-143.8311	-150.9153	-164.7942	-177.1894	-182.9933	-182.9549
-198.9392	-204.1574	-208.1467	-212.6239	-216.5529	-219.5346	-221.9885
-228.5733	-232.2644	-232.7040	-230.8908	-229.3755	-229.2764	-230.5019



- The program is suitable for the unified computation of the complete Bouguer effect on gravity, gravity anomaly and gravity disturbance in land, land-sea junction and sea area. The calculation point may be on the geoid or in near-Earth space.
- If the ocean water depth in the land-sea terrain model is set to zero, the program automatically computes the land complete Bouguer effect in the near-Earth space. If the terrain height in the land-sea terrain model is set to zero, the program automatically computes the seawater complete Bouguer effect in the near-Earth space.
- The complete Bouguer effect here is defined as the variation of Earth gravity field because of the terrain masses above the geoid removed and the seawater density compensated to the terrain density. There is the sea water Bouguer effect in the offshore land area, while there is the local terrain effect in the coastal sea area.

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid - FFT integral

Open DTM Import parameters Save as Start Computation Save process Follow example

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Formulas of land-sea unified complete Bouguer effect

Open the land-sea terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select integral algorithm
1D FFT algorithm

>> Computation Process ** Operation Prompts

>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!
>> Computation end time: 2024-09-22 09:14:19
>> [Function] Using the rigorous numerical integral method or FFT algorithm, from the land-sea terrain model and ellipsoidal height grid file of the land-sea surface, compute the land-sea unified complete Bouguer effect on the gravity (mGal) on the geoid or in near-Earth space.
** Input the land-sea terrain model and the ellipsoidal height grid files of the land-sea surface with the same grid specifications...

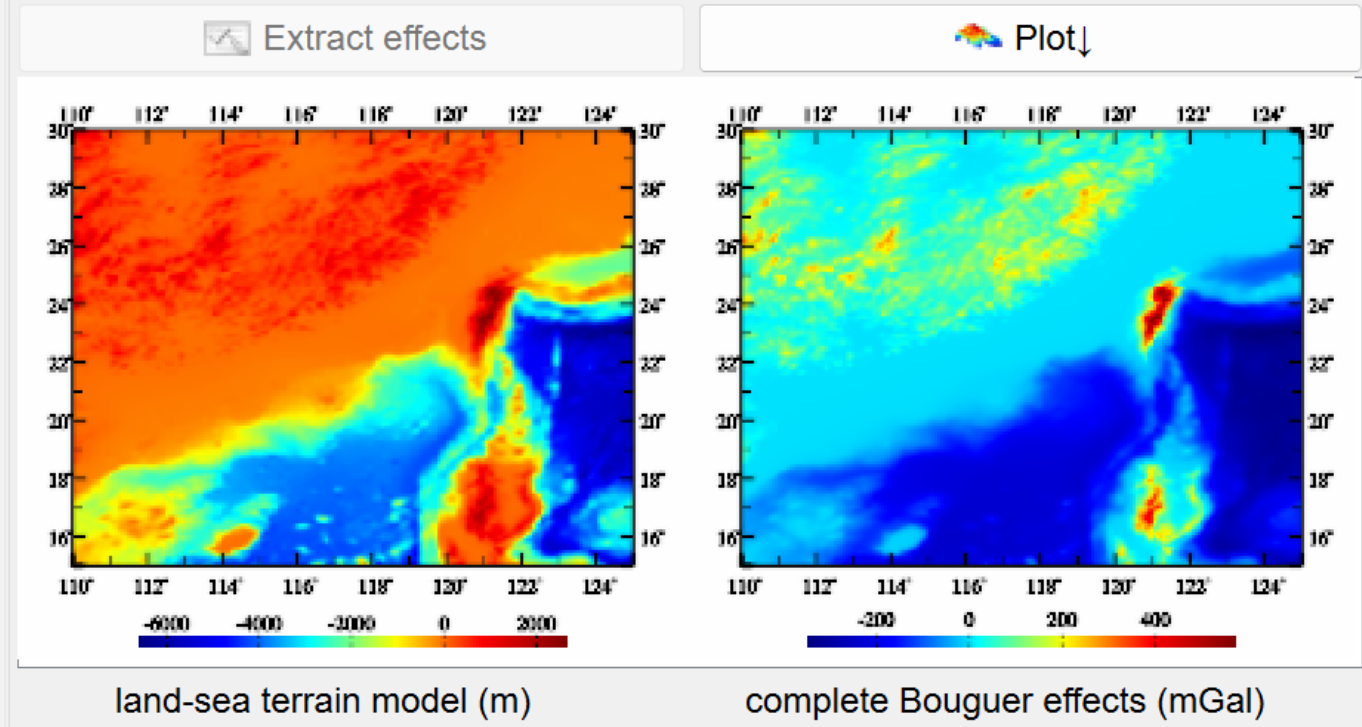
>> Open the land-sea terrain model file C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dtm5m.dat.
>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.
>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerCompleteBougure/dbmhgt5m.dat.
>> Compute the land-sea unified complete Bouguer effects using 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/TerCompleteBougure/IndseaFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-22 09:15:21
>> Complete computation of the land-sea unified complete Bouguer effect outside the geoid!
>> Computation end time: 2024-09-22 09:15:35

Save computation process as

Land integral radius 90 km Sea integral radius 300 km

Save the results as Import setting parameters Start Computation

110.000000	125.000000	15.000000	30.000000	0.08333333	0.08333333	
-8.2859	-8.2979	-9.5859	-14.4386	-17.6973	-19.1729	-21.4192
-45.5102	-47.1726	-48.7790	-50.1541	-50.7128	-53.1583	-59.2286
-123.6301	-131.4323	-141.4338	-154.6832	-162.1845	-164.6695	-163.6497
-192.5911	-195.6108	-197.0458	-198.3330	-199.6909	-201.4540	-203.7060
-202.1460	-207.0358	-208.1123	-207.5622	-206.1675	-204.6629	-204.3039
-180.3762	-151.5508	-130.9900	-125.9695	-151.2787	-173.5002	-193.1195
-174.2465	-153.8247	-134.2208	-120.1139	-137.5049	-157.4718	-179.0607
-206.9287	-214.2794	-219.6096	-222.4735	-217.4892	-202.0047	-172.0155
-3.4159	36.5032	49.6341	103.8896	110.4780	67.5950	9.2229
108.0989	80.8370	77.2701	-3.7790	-5.1007	-6.4139	-6.4107
-57.4799	-62.1677	-70.0703	-82.7109	-84.5577	-81.8098	-71.1878
-82.0921	-111.1265	-133.5695	-161.0260	-178.8618	-195.2426	-219.8860
-10.1361	-9.8124	-10.3213	-14.4839	-18.4358	-20.1202	-22.1095
-45.5731	-47.1780	-48.7561	-50.9909	-50.1816	-51.0756	-50.0823
-136.0776	-141.1197	-147.9200	-161.5592	-173.7014	-179.3393	-179.1977
-194.5959	-199.6421	-203.4520	-207.8225	-211.6475	-214.5354	-216.9526
-223.4237	-227.0499	-227.4504	-225.6176	-224.1094	-224.0079	-225.2122



- The program is suitable for the unified computation of the complete Bouguer effect on gravity, gravity anomaly and gravity disturbance in land, land-sea junction and sea area. The calculation point may be on the geoid or in near-Earth space.
- If the ocean water depth in the land-sea terrain model is set to zero, the program automatically computes the land complete Bouguer effect in the near-Earth space. If the terrain height in the land-sea terrain model is set to zero, the program automatically computes the seawater complete Bouguer effect in the near-Earth space.
- The complete Bouguer effect here is defined as the variation of Earth gravity field because of the terrain masses above the geoid removed and the seawater density compensated to the terrain density. There is the sea water Bouguer effect in the offshore land area, while there is the local terrain effect in the coastal sea area.

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Open DTM Import parameters Save as Start Computation Save process Follow example

Computation of the land-sea unified complete Bouguer effect on gravity outside geoid

Numerical integral computation of the lake-water complete Bouguer effect on gravity

Precise Approach of Earth Gravity Field and Geoid
PAGrav4.5
 Formulas of land-sea unified complete Bouguer effect
 Save computation process as
 Chinese Academy of Surveying & Mapping
 October 2024, Beijing, China

Open the lake water-depth grid file

Open the ellipsoidal height grid file of the lake surface

Open the calculation point location file

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

>> Computation Process ** Operation Prompts

>> Computation end time: 2024-09-22 09:15:35

>> [Function] Using the rigorous numerical integral algorithm, from the lake water-depth grid (value on land is zero) and ellipsoidal height grid file of the lake surface, compute the lake-water complete Bouguer effect on the gravity (mGal).

>> Open the lake water-depth grid file C:/PAGrav4.5_win64en/examples/TerCompleteBougure/TerLakeseabouginflu/lakedepth.dat.

>> Open the ellipsoidal height grid file of the lake surface C:/PAGrav4.5_win64en/examples/TerCompleteBougure/TerLakeseabouginflu/lakehgt.dat.

>> Open the calculation point location file C:/PAGrav4.5_win64en/examples/TerCompleteBougure/TerLakeseabouginflu/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/TerCompleteBougure/TerLakeseabouginflu/rstlake.txt.

>> Behind the source calculation point file record, appends the lake water complete Bouguer effect, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 09:17:49

>> Complete computation of the lake-water complete Bouguer effect outside the geoid!

>> Computation end time: 2024-09-22 09:18:08

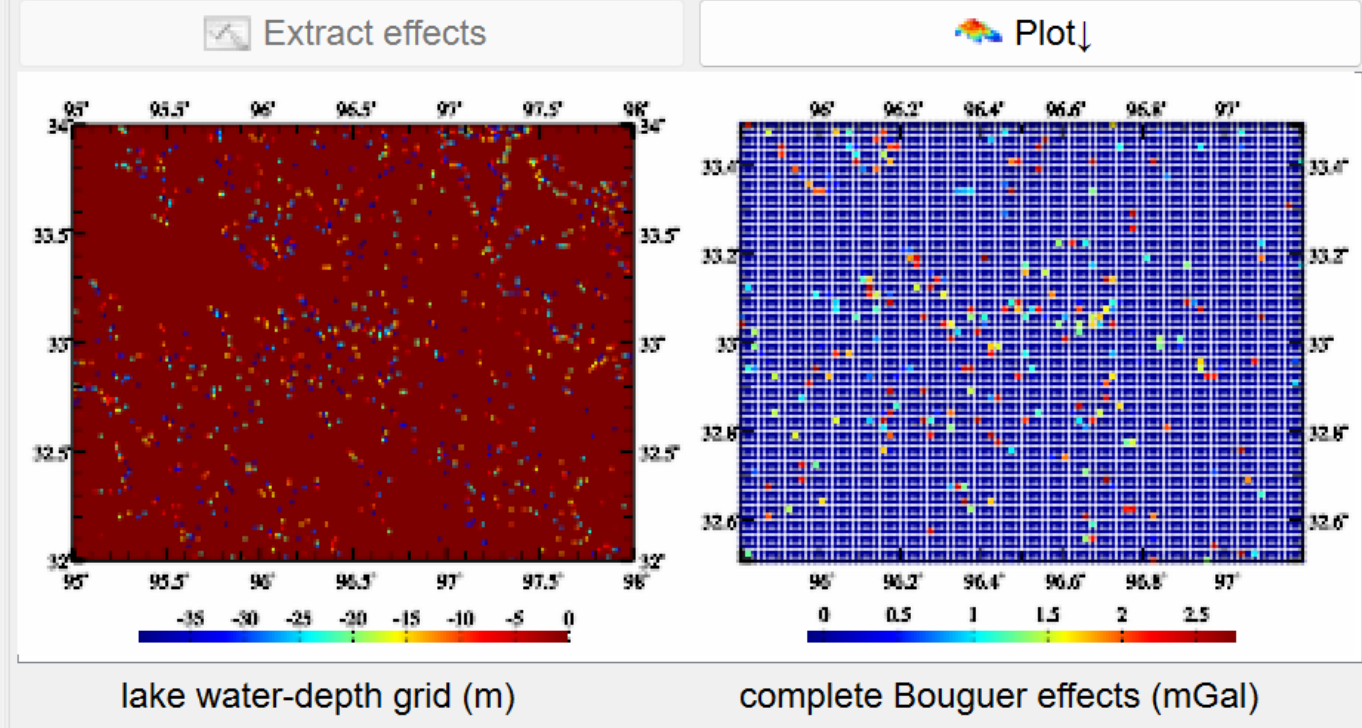
Land integral radius 90 km

Save the results as

Import setting parameters

Start Computation

no	lon	lat	hgt		
1	95.808333	32.508333	4287.928	0.0074	
2	95.825000	32.508333	4393.299	0.0071	
3	95.841667	32.508333	4472.533	-0.0030	
4	95.858333	32.508333	4455.904	-0.0016	
5	95.875000	32.508333	4449.265	-0.0024	
6	95.891667	32.508333	4381.011	-0.0010	
7	95.908333	32.508333	4330.999	-0.0008	
8	95.925000	32.508333	4388.620	-0.0024	
9	95.941667	32.508333	4361.609	-0.0021	
10	95.958333	32.508333	4261.231	-0.0004	
11	95.975000	32.508333	4152.346	0.0012	
12	95.991667	32.508333	4138.344	0.0008	
13	96.008333	32.508333	4174.044	-0.0005	
14	96.025000	32.508333	4193.084	-0.0013	
15	96.041667	32.508333	4078.828	-0.0009	
16	96.058333	32.508333	3984.327	-0.0007	
17	96.075000	32.508333	4052.948	-0.0015	
18	96.091667	32.508333	4094.322	-0.0019	



- The program is suitable for the unified computation of the complete Bouguer effect on gravity, gravity anomaly and gravity disturbance in land, land-sea junction and sea area. The calculation point may be on the geoid or in near-Earth space.
- If the ocean water depth in the land-sea terrain model is set to zero, the program automatically computes the land complete Bouguer effect in the near-Earth space. If the terrain height in the land-sea terrain model is set to zero, the program automatically computes the seawater complete Bouguer effect in the near-Earth space.
- The complete Bouguer effect here is defined as the variation of Earth gravity field because of the terrain masses above the geoid removed and the seawater density compensated to the terrain density. There is the sea water Bouguer effect in the offshore land area, while there is the local terrain effect in the coastal sea area.

Numerical integral of terrain Helmert condensation effects on various field elements

Numerical integral of terrain Helmert condensation on various field elements

FFT algorithm of terrain Helmert condensation on various field elements

Calculator of terrain Helmert condensation effects on various field elements

Algorithm form PAggrav4.5

Precise Approach of Earth Gravity Field and Geoid

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
Number of rows of file header 1
Column ordinal number of ellipsoidal height in the record 4

- Select gravity field elements
- height anomaly (m)
 - gravity (anomaly/disturbance, mGal)
 - vertical deflection (" , SW)
 - disturbing gravity gradient (E, radial)

Integral radius 90 km

Extract effects

Plot↓

>> Computation Process ** Operation Prompts

>> [Function] Using the rigorous numerical integral algorithm, from the ground digital elevation model and ground ellipsoidal height grid, compute the terrain Helmert condensation effects on the height anomaly (m), gravity (anomaly/disturbance, mGal), vertical deflection (" , to south, to west) or (disturbing) gravity gradient (E, radial) on or outside the geoid.

** Input the ground digital elevation model and ground ellipsoidal height grid file with the same grid specifications...

>> Open the ground digital elevation model file C:/PAGrav4.5_win64en/examples/TerHelmertcondensat/landtm1m.dat.

>> Open the ground ellipsoidal height grid file C:/PAGrav4.5_win64en/examples/TerHelmertcondensat/landbmsurfhgt.dat.

>> Open the calculation point location file C:/PAGrav4.5_win64en/examples/TerHelmertcondensat/surfhgt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/TerHelmertcondensat/result.txt.

** Record format: Behind the source calculation point file record, appends several columns of the terrain Helmert condensation effects on specified types of field elements, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

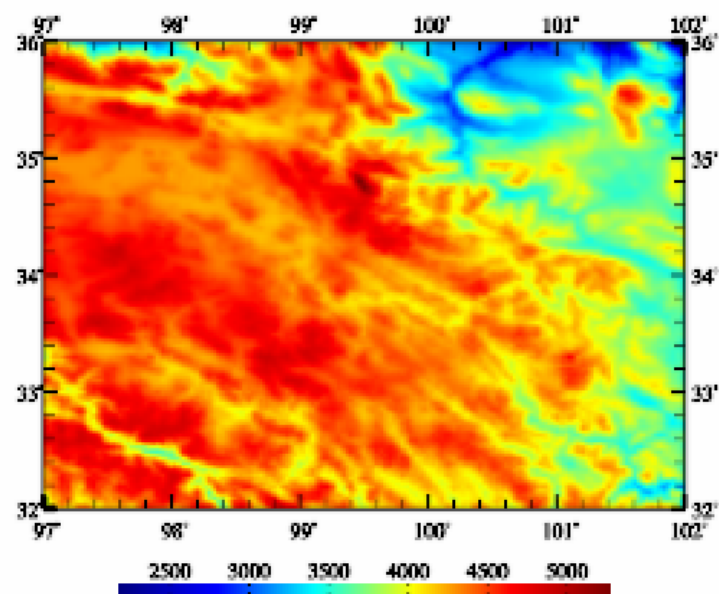
** Click the [Start Computation] control button or the [Start Computation] tool button

Save the results as

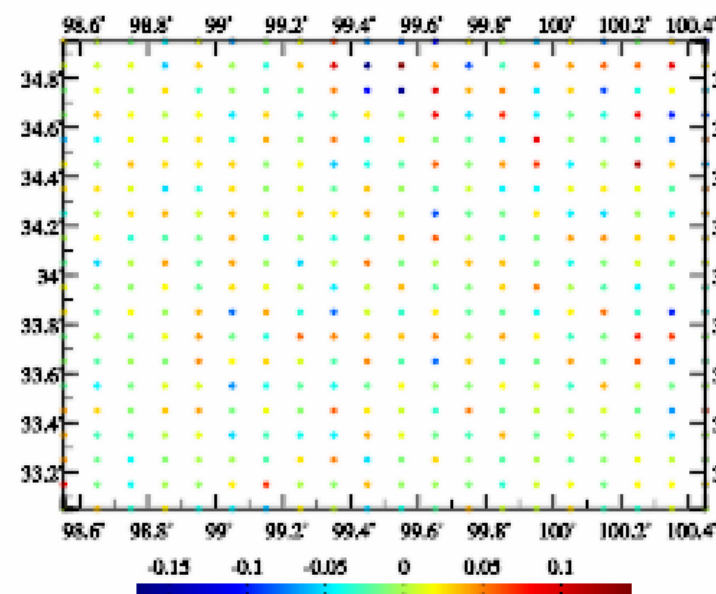
Import setting parameters

Start Computation

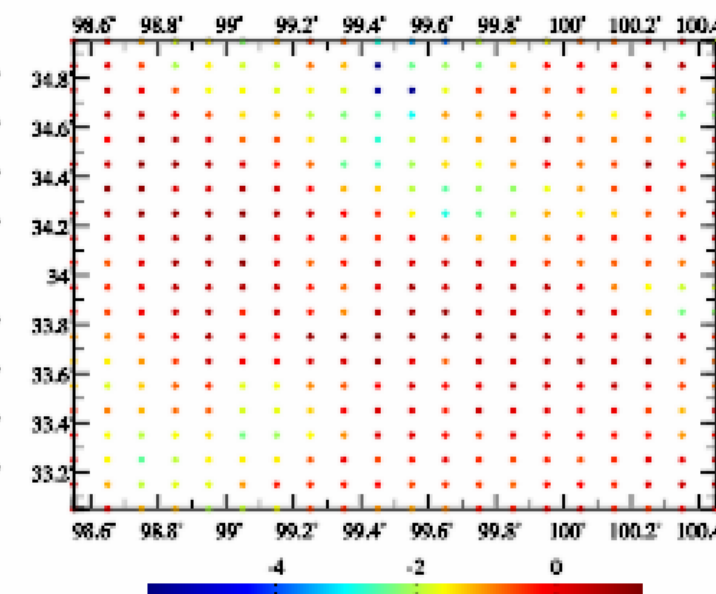
no	lon(deg/decimal)	lat	ellipHeight (m)						
1	98.550000	33.050000	4372.431	0.0056	-0.0969	-8.7481	0.5033	-1.2229	
2	98.650000	33.050000	4372.834	0.0347	0.0307	-10.9996	-6.5552	-5.9075	
3	98.750000	33.050000	4530.959	-0.0336	-1.1852	-13.1633	-9.3919	5.9238	
4	98.850000	33.050000	4567.407	0.0234	-1.1791	-14.0034	-2.3475	-4.6099	
5	98.950000	33.050000	4646.551	-0.0401	-2.0462	-15.1799	-4.9229	7.2632	
6	99.050000	33.050000	4672.380	-0.0463	-1.9176	-9.1527	2.1447	8.2814	
7	99.150000	33.050000	4611.765	-0.0611	-1.6366	-1.2470	5.5278	11.4664	
8	99.250000	33.050000	4475.199	0.0232	-0.5479	-1.0704	7.1169	-3.7881	



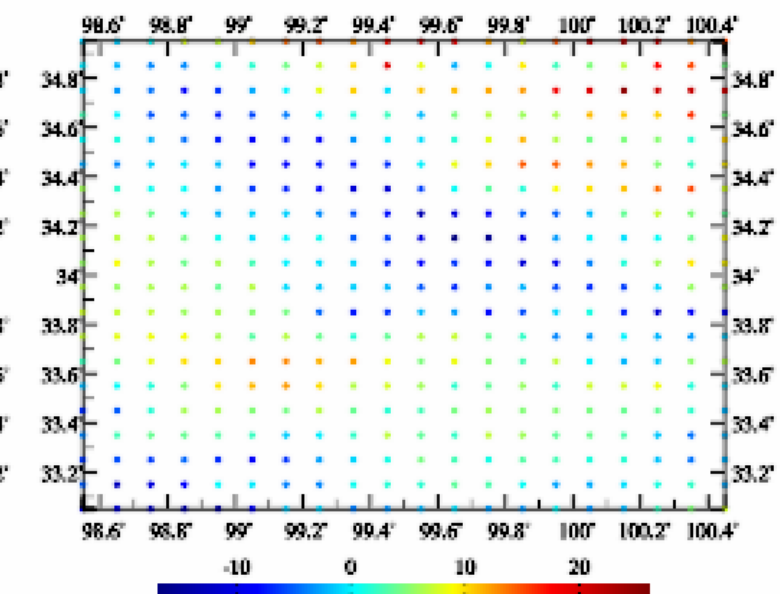
digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (" , S)

The calculation point may be on the geoid or in near-Earth space.

Compared with local terrain effects, terrain Helmert condensation has more ultrashort wave components. Affected by the continental topography, there is terrain Helmert condensation in the nearshore sea area, and the terrain Helmert condensation in the deep ocean area is equal to zero.

Numerical integral of terrain Helmert condensation effects on various field elements

Open DEM Import parameters Save as Start Computation Save process Follow example



Numerical integral of terrain Helmert condensation on various field elements

FFT algorithm of terrain Helmert condensation on various field elements

Calculator of terrain Helmert condensation effects on various field elements

Algorithm form PAGrav4.5

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

- Select gravity field elements
- height anomaly (m)
 - gravity (anomaly/disturbance, mGal)
 - vertical deflection (" , SW)
 - disturbing gravity gradient (E, radial)

Integral radius 90 km

>> Computation Process ** Operation Prompts

>> [Function] Using the rigorous numerical integral algorithm, from the ground digital elevation model and ground ellipsoidal height grid, compute the terrain Helmert condensation effects on the height anomaly (m), gravity (anomaly/disturbance, mGal), vertical deflection (" , to south, to west) or (disturbing) gravity gradient (E, radial) on or outside the geoid.

** Input the ground digital elevation model and ground ellipsoidal height grid file with the same grid specifications...

>> Open the ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landtm1m.dat.

>> Open the ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landbmsurfhgt.dat.

>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landbmsurfhgt.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/numitng.dat.

** At the same time, the program also outputs the terrain Helmert condensation effect grid files on height anomaly (*.ksi), gravity anomaly (*.gra), gravity disturbance (*.rga), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the terrain Helmert condensation effect grid file on the specified types of elements.

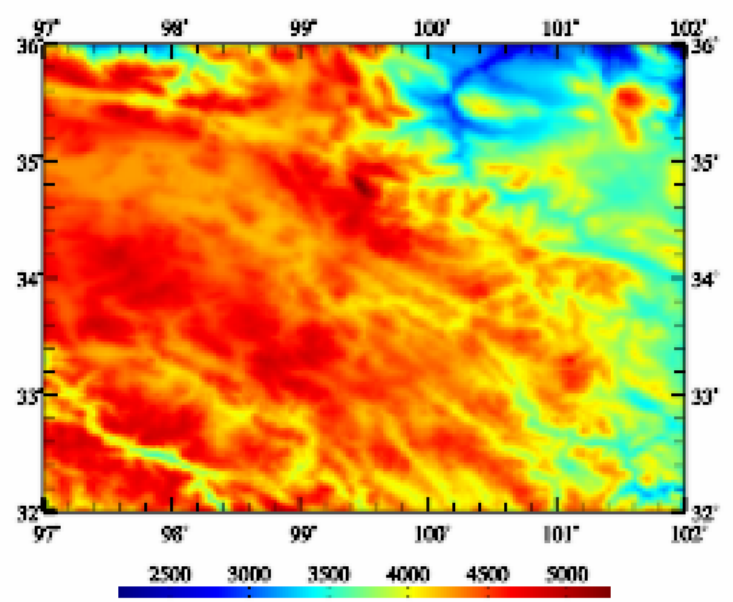
>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button or the [Start Computation] tool button

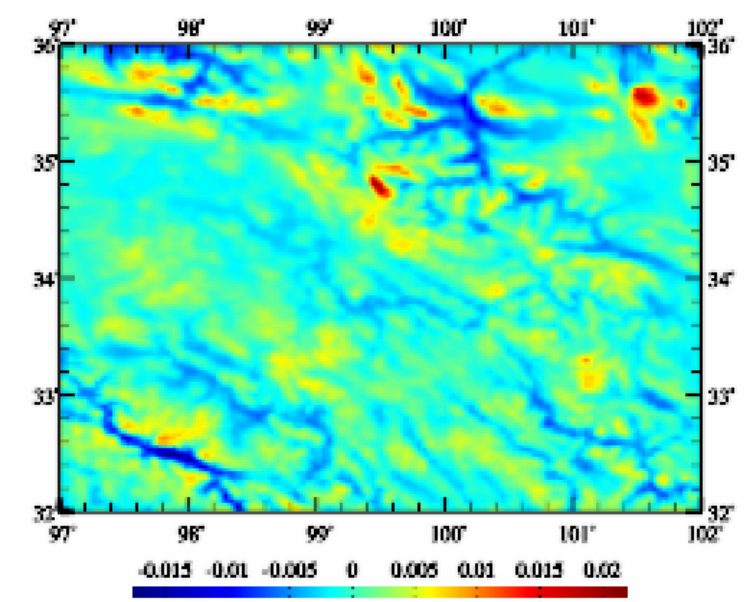
Save the results as Import setting parameters Start Computation

C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/numitng.ksi
C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/numitng.gra
C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/numitng.dft
C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/numitng.grr

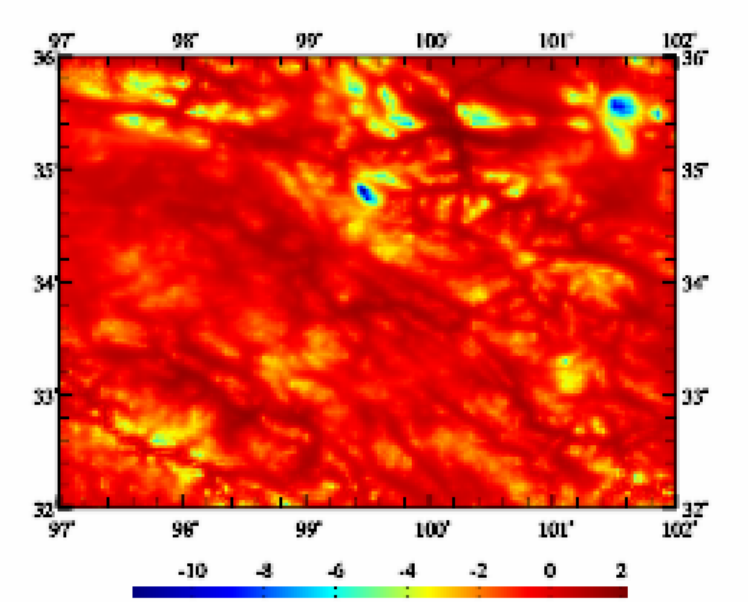
Extract effects Plot↓



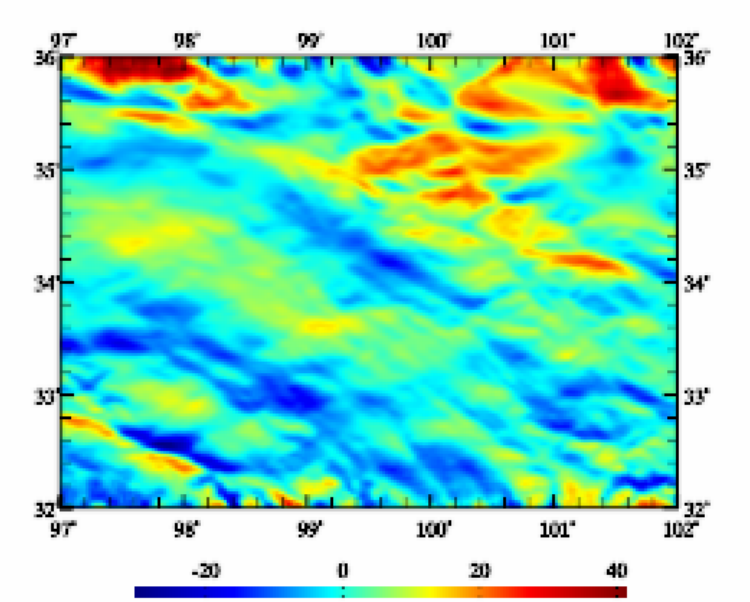
digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)

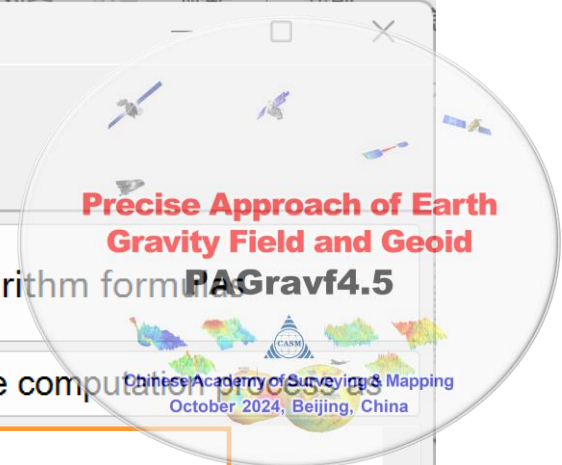


vertical deflection (" , S)

- The calculation point may be on the geoid or in near-Earth space.
- Compared with local terrain effects, terrain Helmert condensation has more ultrashort wave components. Affected by the continental topography, there is terrain Helmert condensation in the nearshore sea area, and the terrain Helmert condensation in the deep ocean area is equal to zero.

FFT algorithm of terrain Helmert condensation effects on various field elements

Open DEM Import parameters Save as Start Computation Save process Follow example



Numerical integral of terrain Helmert condensation on various field elements

FFT algorithm of terrain Helmert condensation on various field elements

Calculator of terrain Helmert condensation effects on various field elements

Algorithm form PAggrav4.5

Save computation process

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (" , SW)
- disturbing gravity gradient (E, radial)

Integral radius 90 km

>> Computation Process ** Operation Prompts

>> Open the ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landtm1m.dat.
 >> Open the ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landbmsurfhgt.dat.
 >> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landgeoidhgt.dat.

** Look at the file information in the window below, set the input file format parameters...
 >> Compute the terrain Helmert condensation effects using 2D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT2.txt.
 ** At the same time, the program also outputs the terrain Helmert condensation effect grid files on height anomaly (*.ksi), gravity anomaly (*.gra), gravity disturbance (*.rga), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the terrain Helmert condensation effect grid file on the specified types of elements.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-22 11:55:16

>> Complete the computation of terrain Helmert condensation effects!

Fast algorithm 2D FFT

Save the results as

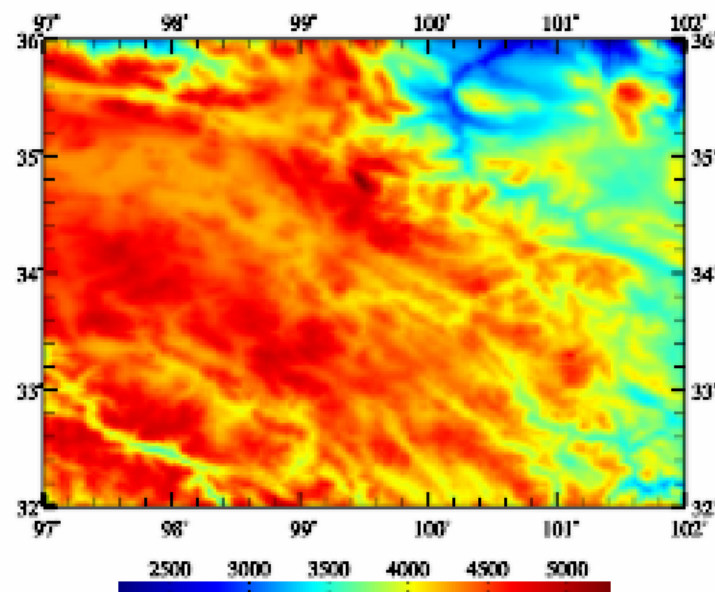
Import setting parameters

Start Computation

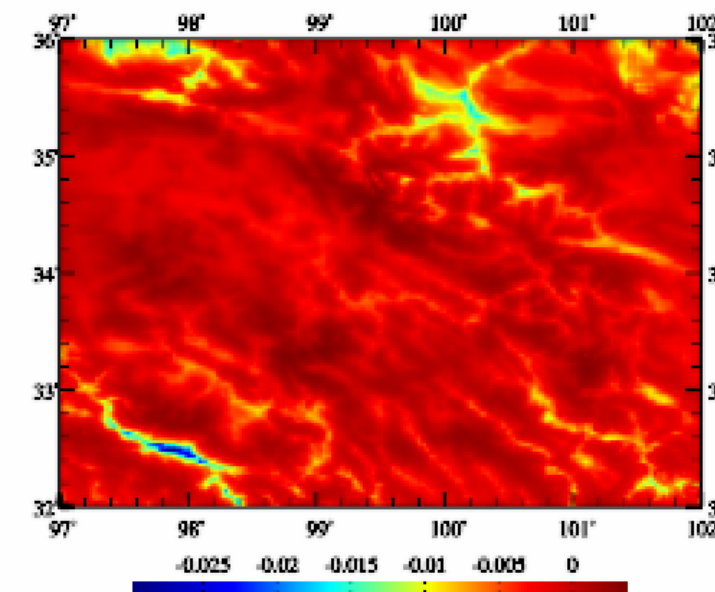
C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT2.ksi
 C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT2.gra
 C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT2.dft
 C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT2.grr

Extract effects

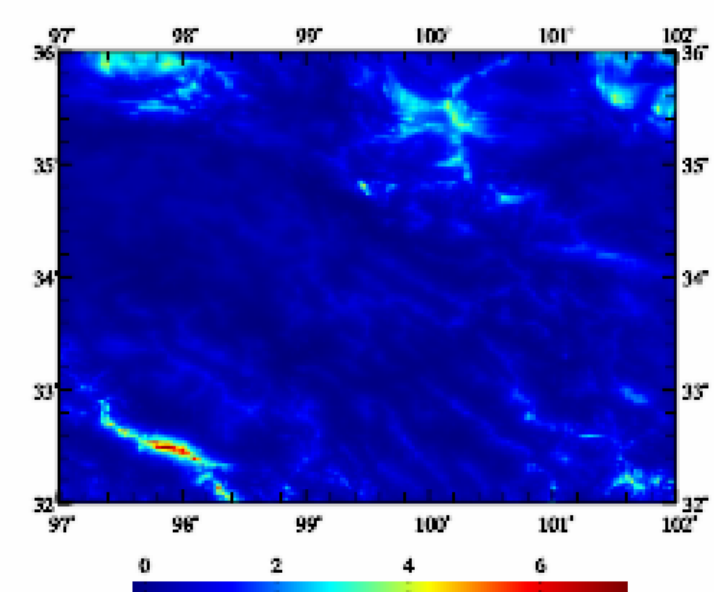
Plot↓



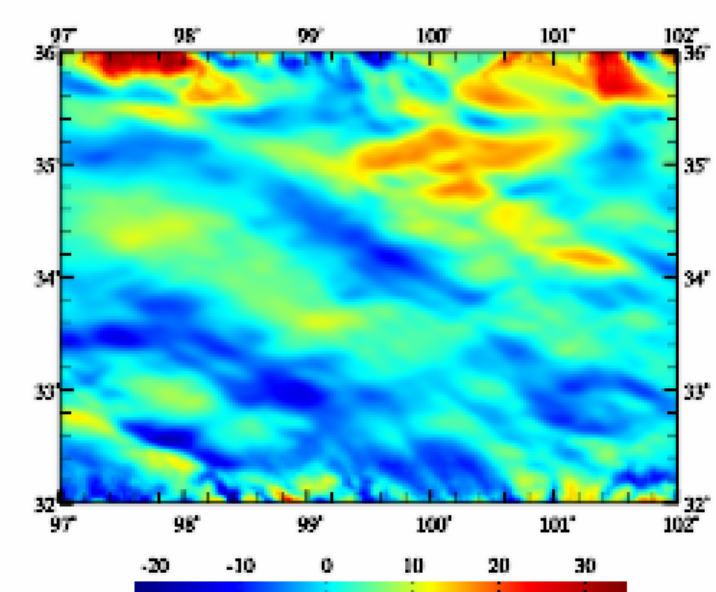
digital elevation model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (" , S)

The calculation point may be on the geoid or in near-Earth space.

Compared with local terrain effects, terrain Helmert condensation has more ultrashort wave components. Affected by the continental topography, there is terrain Helmert condensation in the nearshore sea area, and the terrain Helmert condensation in the deep ocean area is equal to zero.

FFT algorithm of terrain Helmert condensation effects on various field elements

Numerical integral of terrain Helmert condensation on various field elements

FFT algorithm of terrain Helmert condensation on various field elements

Calculator of terrain Helmert condensation effects on various field elements

Algorithm formulas

Save computation process as

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (" , SW)
- disturbing gravity gradient (E, radial)

Integral radius 90 km

>> Computation Process ** Operation Prompts

>> Open the ground digital elevation model file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landtm1m.dat.
 >> Open the ground ellipsoidal height grid file C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landbmsurfhgt.dat.
 >> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/landgeoidhgt.dat.

** Look at the file information in the window below, set the input file format parameters...
 >> Compute the terrain Helmert condensation effects using 1D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT1.txt.
 ** At the same time, the program also outputs the terrain Helmert condensation effect grid files on height anomaly (*.ksi), gravity anomaly (*.gra), gravity disturbance (*.rga), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory. Where * is the output file name entered from the interface. The program outputs the terrain Helmert condensation effect grid file on the specified types of elements.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

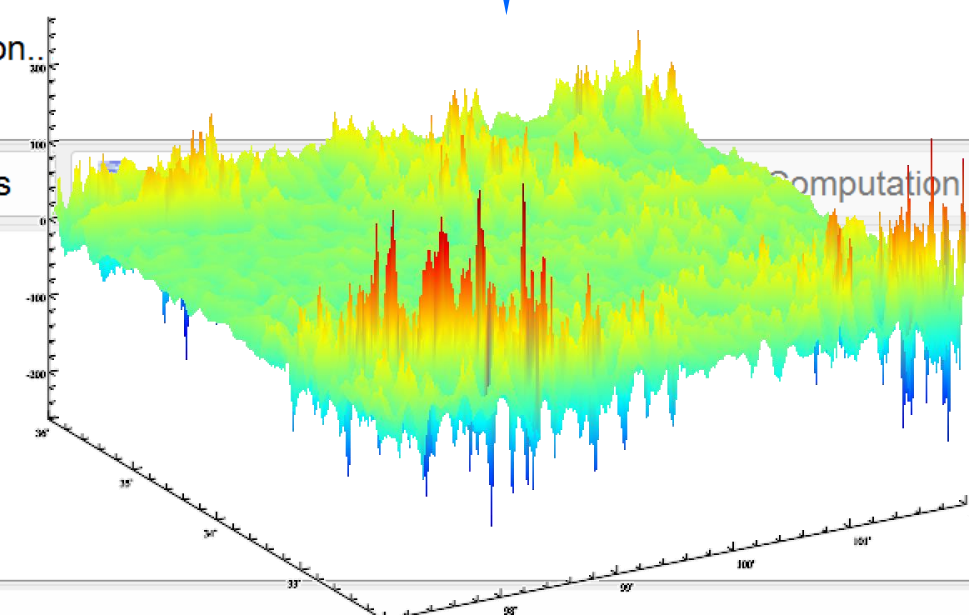
>> Computation start time: 2024-09-22 11:57:55

>> Complete the computation of terrain Helmert condensation effects!

Fast algorithm 1D FFT

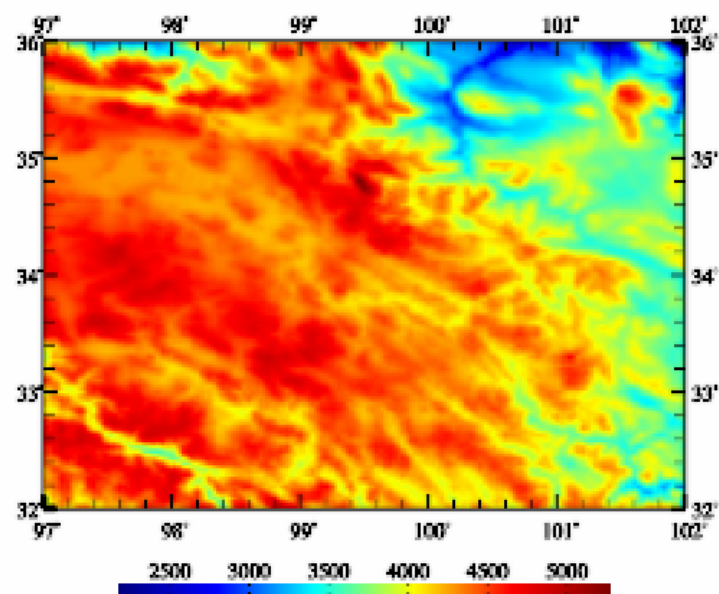
Save the results as

C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT1.ksi
 C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT1.dft
 C:/PAGravf4.5_win64en/examples/TerHelmertcondensat/surfFFT1.grr

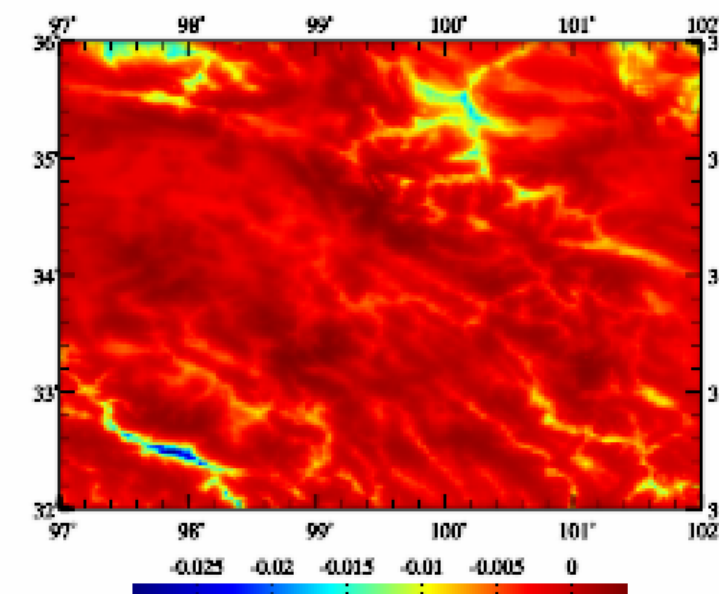


Extract effects

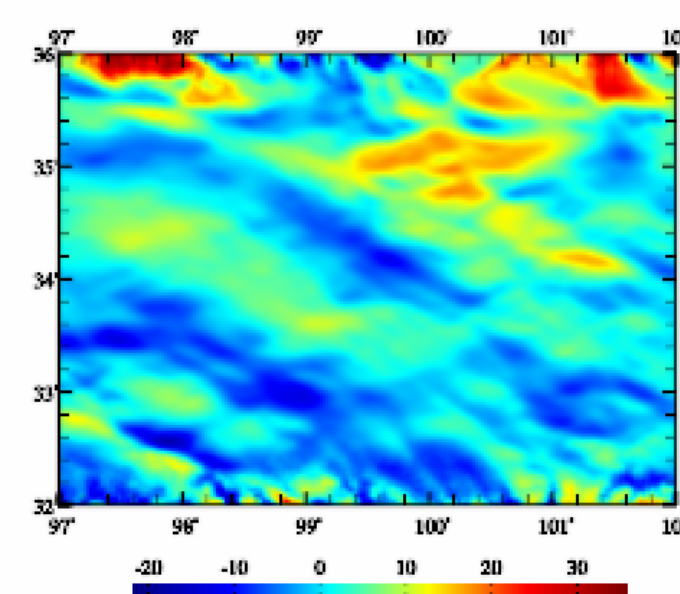
Plot↓



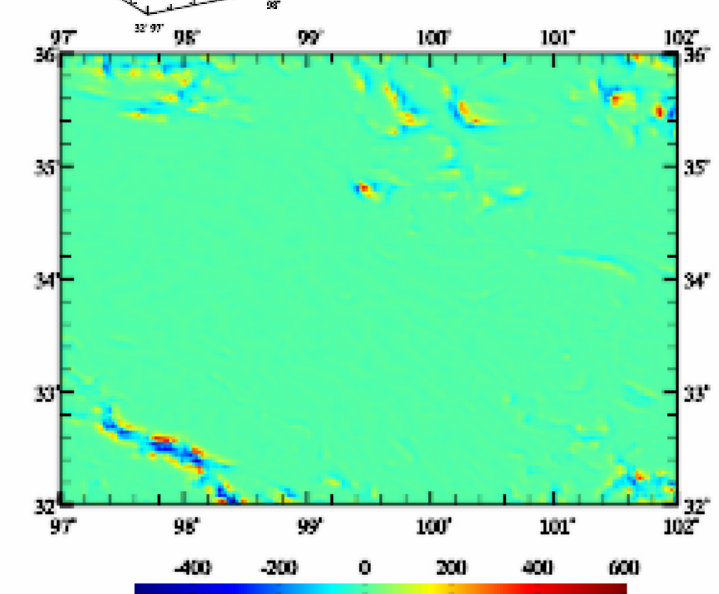
digital elevation model (m)



height anomaly (m)



vertical deflection (" , S)



disturbing gradient (E, R)

The calculation point may be on the geoid or in near-Earth space.

Compared with local terrain effects, terrain Helmert condensation has more ultrashort wave components. Affected by the continental topography, there is terrain Helmert condensation in the nearshore sea area, and the terrain Helmert condensation in the deep ocean area is equal to zero.

Calculator of terrain Helmert condensation effects on various field elements

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Input geodetic coordinates of calculation point

longitude 98.240000°

latitude 32.428000°

ellipsoidal height 2017.830m

Integral radius 90 km

Start calculation

Ground digital elevation model

97.000000	102.000000	32.000000	36.000000	0.01666667	0.01666667
3988.0003	4048.9987	4129.9921	4151.9956	4155.9995	4177.9961
4277.9980	4373.9953	4466.9865	4479.9911	4520.9918	4547.9825
4242.0005	4229.0008	4211.0001	4165.0004	4150.0047	4157.0059
4429.0008	4511.9959	4529.9991	4431.9991	4539.9993	4531.9988
4273.0028	4221.0056	4195.9991	4195.9991	4251.0050	4337.9987
4643.9962	4607.0004	4607.0004	4607.0004	457.0003	4379.9835
4500.0065	4593.9997	4593.9997	4593.9997	4593.9997	4473.0101
4272.0146	4409.9997	4409.9997	4409.9997	4409.9997	4729.0038
4530.9966	4450.9997	4450.9997	4450.9997	4450.9997	4071.0117
4371.0006	4429.9974	4429.9974	4429.9974	4429.9974	4520.9942
3868.0107	3964.9992	3964.9992	3964.9992	3964.9992	4124.0006
4243.0076	4270.0056	4350.9996	4350.9996	4350.9996	4347.9933
4161.9980	4189.9935	4160.9996	4160.9996	4143.9926	4040.0077
4050.9965	4023.0017	4012.0017	4012.0017	4171.9934	4235.0039
4051.0030	4022.0027	4077.0121	4023.9996	4032.9998	3996.0025
4299.0025	4415.9991	4516.9921	4514.9967	4458.0037	4431.9971
3672.0205	3912.9978	4073.9952	4150.0051	4313.9938	4374.9940

Terrain Helmert condensation effect calculation results

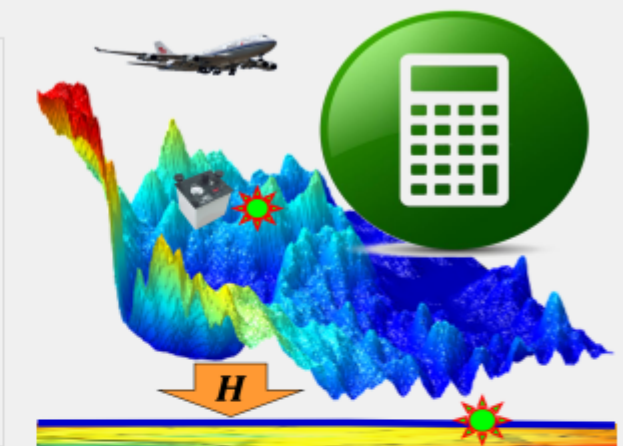
height anomaly (m) -0.0207

gravity (anomaly/disturbance, mGal) -0.6315

vertical deflection (" , S) -14.1486

vertical deflection (" , W) -1.2267

(disturbing) gradient (E, radial) 9.7229



Inputting the ground digital elevation model (standing for terrain relief) and ground geodetic ellipsoidal height grid (standing for the terrain surface location) files with the same grid specifications, the button [Start Calculation] becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the terrain Helmert condensation effects on various field elements at the calculation point can be computed and displayed in time.

The program allows to replace the ground digital elevation model and the ground ellipsoidal height grid file at any time from the interface, or to change the integral radius, and these user inputs will take effect at once. The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.

Calculator of terrain Helmert condensation effects on various field elements

Open the ground digital elevation model file

Open the ground ellipsoidal height grid file

Input geodetic coordinates of calculation point

longitude 99.640000°

latitude 34.428000°

ellipsoidal height 317.830m

Integral radius 90 km

Start calculation

Ground digital elevation model

97.000000	102.000000	32.000000	36.000000	0.01666667	0.01666667
3988.0003	4048.9987	4129.9921	4151.9956	4155.9995	4177.9961
4277.9980	4373.9953	4466.9865	4479.9931	4520.9918	4547.9825
4242.0005	4229.0008	4211.0001	4165.0054	4150.0047	4157.0059
4429.0008	4511.9959	4529.9991	4531.9999	4539.9993	4531.9988
4273.0028	4221.0056	4196.0075	4196.0075	4251.0050	4337.9987
4643.9962	4607.0004	4605.9966	4605.9966	4457.0003	4379.9835
4500.0065	4593.9999	4650.9999	4650.9999	4585.9976	4473.0101
4272.0146	4409.9999	4409.9999	4409.9999	4647.0046	4729.0038
4530.9966	4456.9999	4456.9999	4456.9999	40042.9999	4071.0117
4371.0006	4429.9999	4429.9999	4429.9999	40094.9999	4520.9942
3868.0107	3964.9999	3964.9999	3964.9999	40006.9999	4124.0006
4243.0076	4270.0000	4270.0000	4270.0000	40034.9999	4347.9933
4161.9980	4189.9937	4189.9937	4189.9937	40077.9999	4040.0077
4050.9965	4023.0017	4023.0017	4023.0017	40034.9999	4235.0039
4051.0030	4022.0027	3977.9999	3977.9999	40032.9988	3996.0025
4299.0025	4415.9991	4514.9999	4514.9999	4458.0037	4431.9971
3672.0205	3912.9978	4073.9952	4159.0051	4313.9938	4374.9940

Terrain Helmert condensation effect calculation results

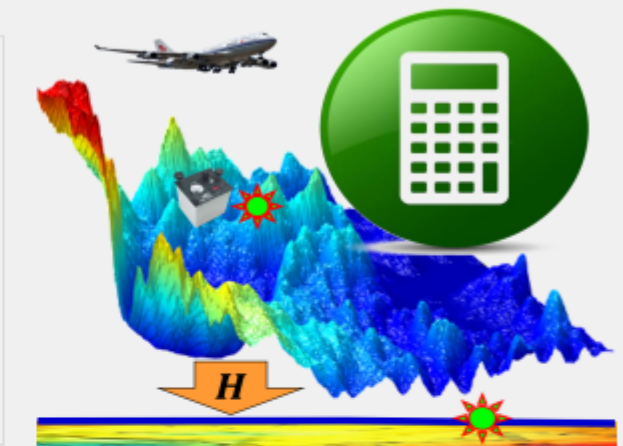
height anomaly (m) 0.0015

gravity (anomaly/disturbance, mGal) -1.5825

vertical deflection (" , S) 2.9665

vertical deflection (" , W) 7.6491

(disturbing) gradient (E, radial) 1.1203



Inputting the ground digital elevation model (standing for terrain relief) and ground geodetic ellipsoidal height grid (standing for the terrain surface location) files with the same grid specifications, the button [Start Calculation] becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the terrain Helmert condensation effects on various field elements at the calculation point can be computed and displayed in time.

The program allows to replace the ground digital elevation model and the ground ellipsoidal height grid file at any time from the interface, or to change the integral radius, and these user inputs will take effect at once. The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.

Numerical integral of land-sea residual terrain effects on various gravity field elements

Precise Approach of Earth Gravity Field and Geoid
PAGrav4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Numerical integral of land-sea residual terrain effects on various gravity field elements

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Calculator of land-sea unified residual terrain effect or complete Bouguer effect

Open high-resolution land-sea terrain model file

Open the land-sea low-pass terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format

discrete calculation point file

Open the calculation point position file

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

Select gravity field elements

height anomaly (m)

gravity (anomaly/disturbance, mGal)

vertical deflection (" , SW)

disturbing gravity gradient (E, radial)

Integral radius 90 km

Extract effects Plot

>> Computation Process ** Operation Prompts

residual terrain model (RTM) before integral.

>> Open the high-resolution land-sea terrain model file C:/PAGrav4.5_win64en/examples/Renterrianeffect/landtm1m.dat.

>> Open the land-sea low-pass terrain model file C:/PAGrav4.5_win64en/examples/Renterrianeffect/landtm1mlvb.dat.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGrav4.5_win64en/examples/Renterrianeffect/landbmsurfhgt.dat.

>> Open the calculation point location file C:/PAGrav4.5_win64en/examples/Renterrianeffect/surfhgt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/Renterrianeffect/result.txt.

** Record format: Behind the source calculation point file record, appends several columns of residual terrain effects on specified types of field elements, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

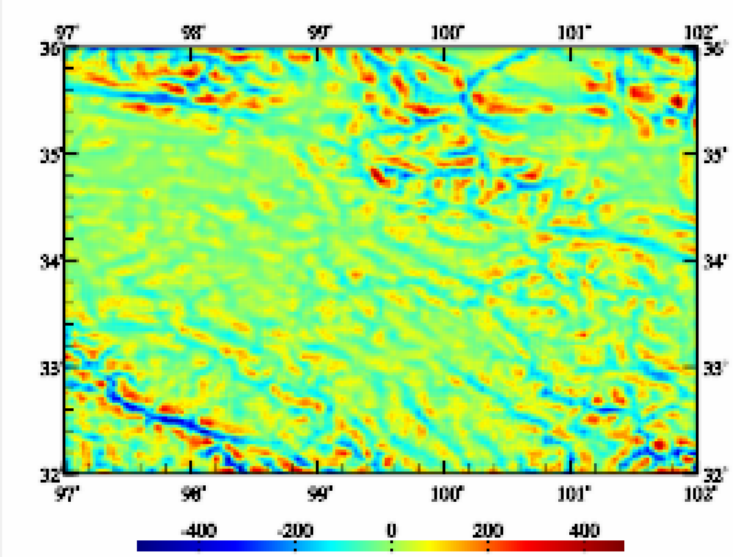
>> Computation start time: 2024-09-22 12:50:02

>> Complete the computation of land-sea unified residual terrain effects!

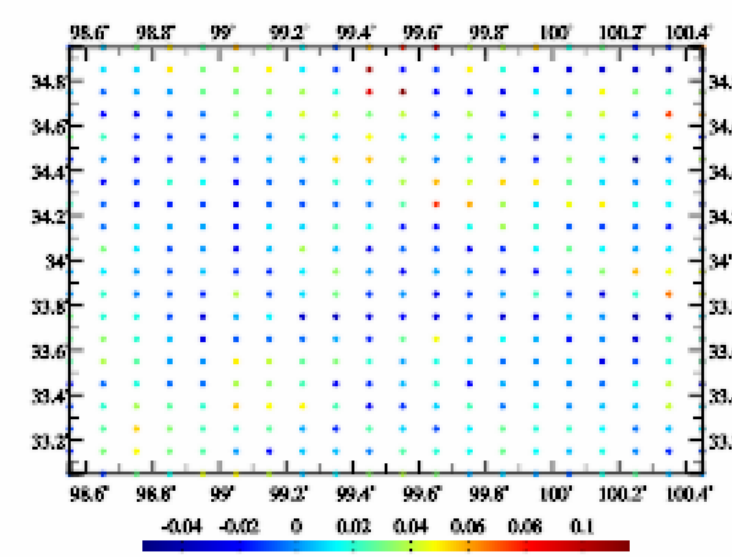
>> Computation end time: 2024-09-22 12:50:04

Save the results as Import setting parameters Start Computation

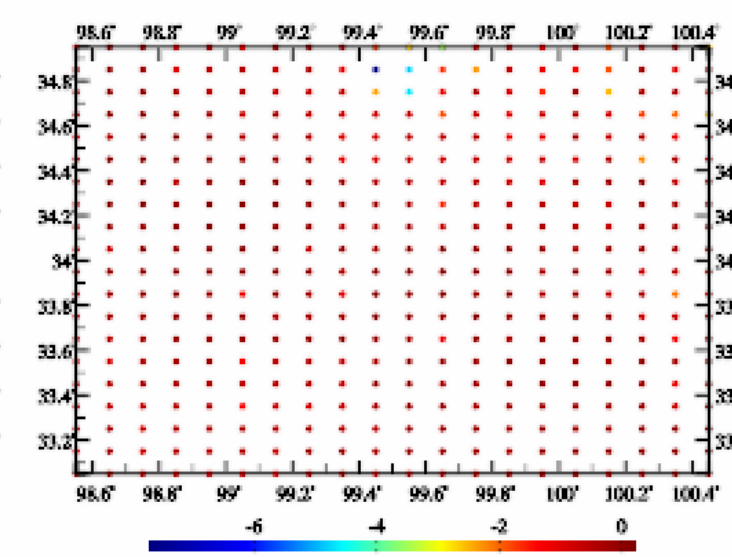
number	long(deg/decimal)	lat	ellipHeight(m)					
1	98.550000	33.050000	4372.431	-0.0064	-0.0821	-0.4948	1.6642	9.6285
2	98.650000	33.050000	4372.834	-0.0128	-0.0748	-0.1234	0.1747	53.4893
3	98.750000	33.050000	4530.959	0.0292	-0.3837	-0.3162	-1.3952	-50.7005
4	98.850000	33.050000	4567.407	0.0166	-0.5441	-0.6622	0.5086	66.8856
5	98.950000	33.050000	4646.551	0.0452	-0.7076	-1.6590	-1.6979	-60.9009
6	99.050000	33.050000	4672.380	0.0490	-0.6732	-0.4186	0.3348	-75.5007
7	99.150000	33.050000	4611.765	0.0407	-1.0746	1.6103	0.5141	-111.7206



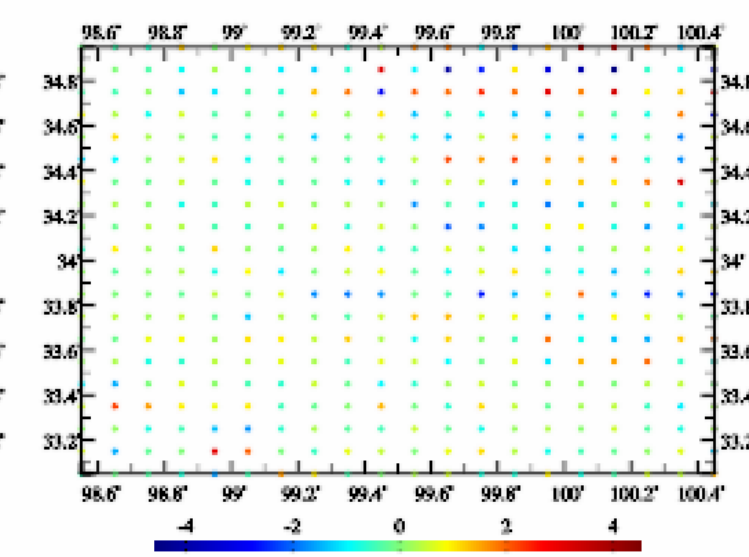
residual terrain model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (" , S)

- The land-sea residual terrain effect here is defined as the short-wave and ultra-short-wave components of the land-sea complete Bouguer effect. Since the normal gravity field keeps unchanged, the residual terrain effect on the gravity disturbance and gravity anomaly is always equal to the residual terrain effect on gravity.
- The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also employed to separate land and sea areas. Since the finite radius integral cannot deal with terrain zero-degree term, the program removes the average of the residual terrain model (RTM) before integral.

Numerical integral of land-sea residual terrain effects on various gravity field elements

Precise Approach of Earth Gravity Field and Geoid
PAGravf4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Numerical integral of land-sea residual terrain effects on various gravity field elements

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Calculator of land-sea unified residual terrain effect or complete Bouguer effect

Open high-resolution land-sea terrain model file

Open the land-sea low-pass terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format

ellipsoidal height grid file

Open the ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (" , SW)
- disturbing gravity gradient (E, radial)

Integral radius 90 km

Extract effects

Plot

>> Computation Process ** Operation Prompts

residual terrain model (RTM) before integral.

>> Open the high-resolution land-sea terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1m.dat.

>> Open the land-sea low-pass terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1mlvb.dat.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landbmsurfhgt.dat.

>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landgeoidhgt.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/Renterrianeffect/numintg.dat.

** At the same time, the program also outputs the residual terrain effect grid files on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory, where * is the output file name entered from the interface. The program outputs residual terrain effect grid file on the specified types of elements.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

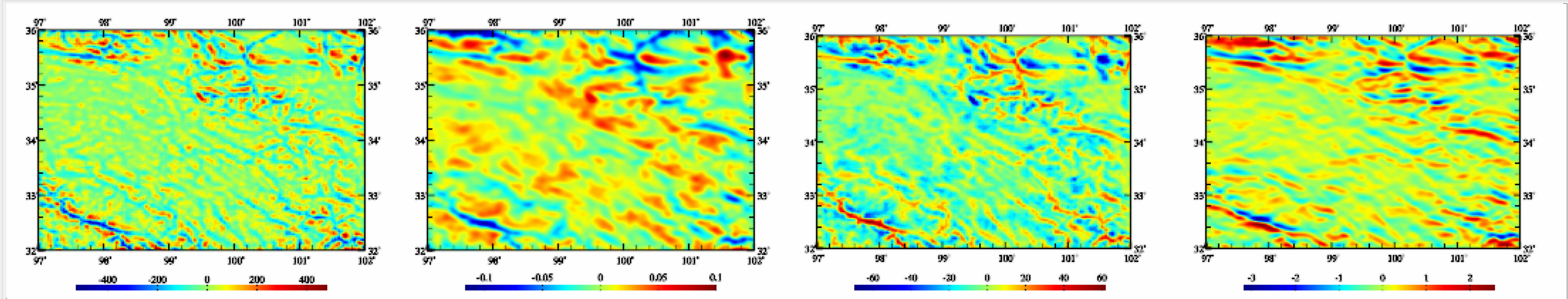
>> Computation start time: 2024-09-22 12:52:09

>> Complete the computation of land-sea unified residual terrain effects!

>> Computation end time: 2024-09-22 12:58:33

Save the results as Import setting parameters Start Computation

C:/PAGravf4.5_win64en/examples/Renterrianeffect/numintg.ksi
C:/PAGravf4.5_win64en/examples/Renterrianeffect/numintg.gra
C:/PAGravf4.5_win64en/examples/Renterrianeffect/numintg.dft
C:/PAGravf4.5_win64en/examples/Renterrianeffect/numintg.grr



residual terrain model (m)

height anomaly (m)

gravity (anomaly, mGal)

vertical deflection (" , S)

- The land-sea residual terrain effect here is defined as the short-wave and ultra-short-wave components of the land-sea complete Bouguer effect. Since the normal gravity field keeps unchanged, the residual terrain effect on the gravity disturbance and gravity anomaly is always equal to the residual terrain effect on gravity.
- The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also employed to separate land and sea areas. Since the finite radius integral cannot deal with terrain zero-degree term, the program removes the average of the residual terrain model (RTM) before integral.

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Numerical integral of land-sea residual terrain effects on various gravity field elements

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Calculator of land-sea unified residual terrain effect or complete Bouguer effect

Open high-resolution land-sea terrain model file

Open the land-sea low-pass terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Open the ellipsoidal height grid file of calculation surface

Select gravity field elements

- height anomaly (m)
- gravity (anomaly/disturbance, mGal)
- vertical deflection (" , SW)
- disturbing gravity gradient (E, radial)

Integral radius 90 km

>> Computation Process ** Operation Prompts

```
>> Open the high-resolution land-sea terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1m.dat.
>> Open the land-sea low-pass terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1mlvb.dat.
>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landbmsurfhgt.dat.
>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landgeoidhgt.dat.
>> Compute the land-sea unified residual terrain effects using 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT2.txt.
```

** At the same time, the program also outputs the residual terrain effect grid files on height anomaly (*.ks), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory, where * is the output file name entered from the interface. The program outputs residual terrain effect grid file on the specified types of elements.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] control button.

>> Computation start time: 2024-09-22 13:00:34

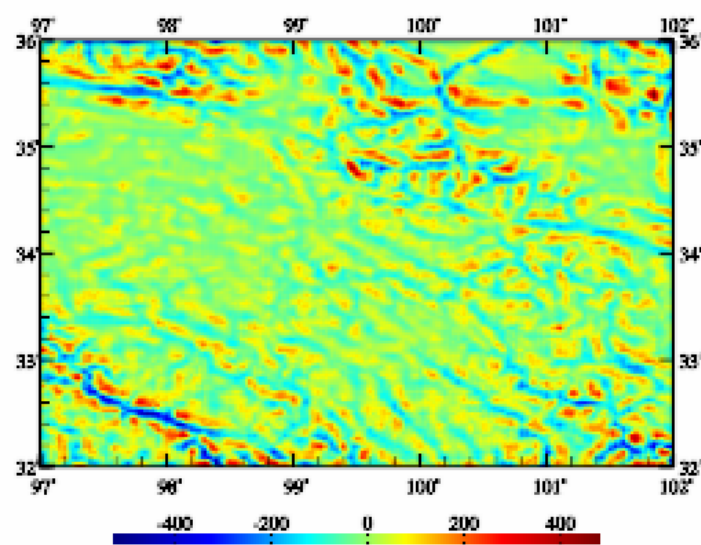
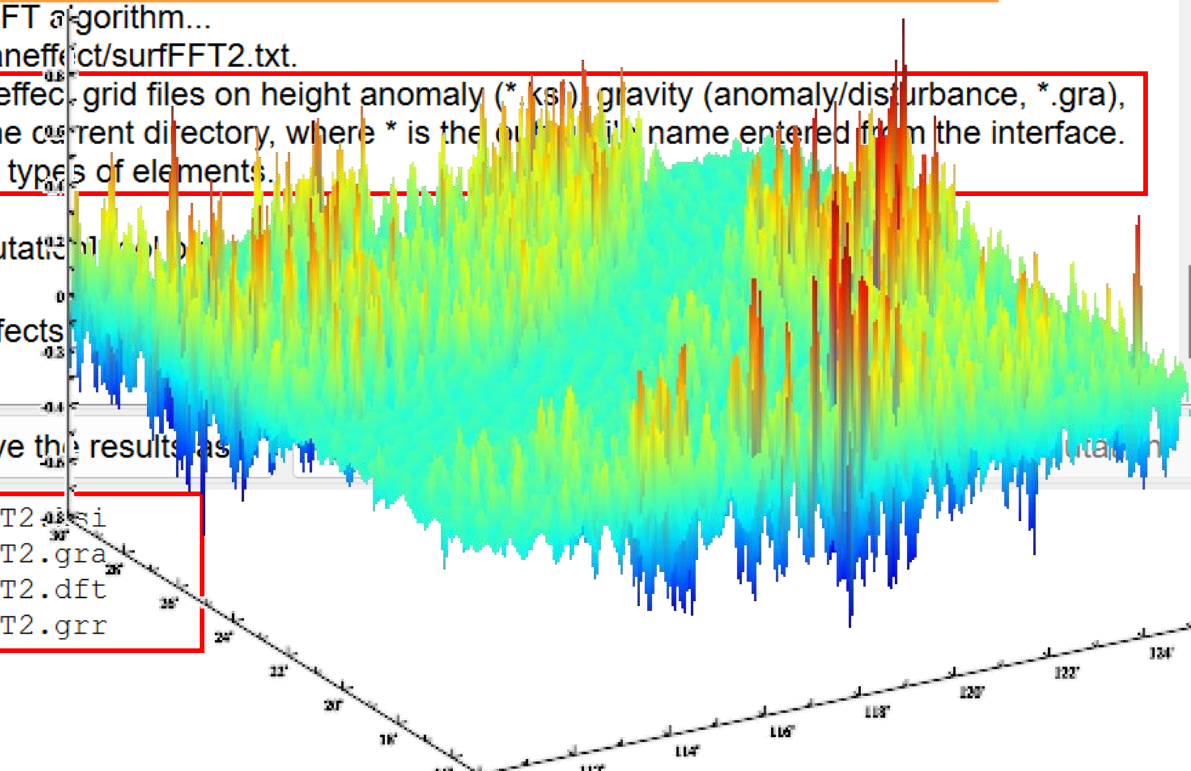
>> Complete the computation of land-sea unified residual terrain effects

>> Computation end time: 2024-09-22 13:00:37

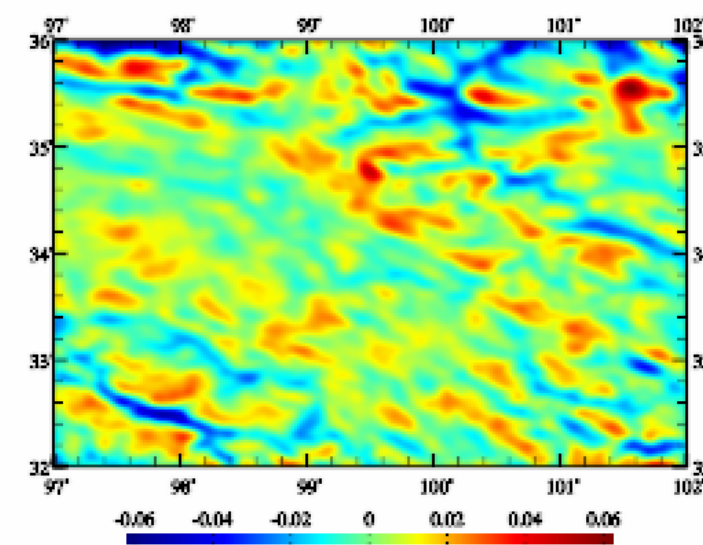
Fast algorithm 2D FFT

Save the results as

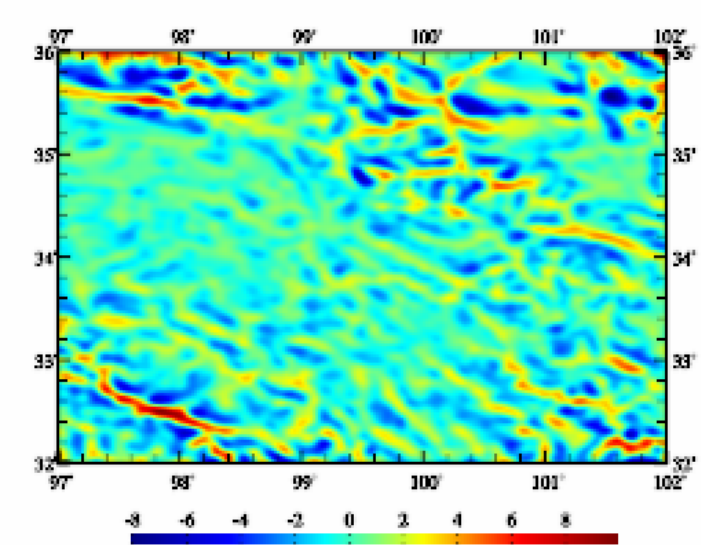
```
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT2.ks
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT2.gra
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT2.dft
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT2.grr
```



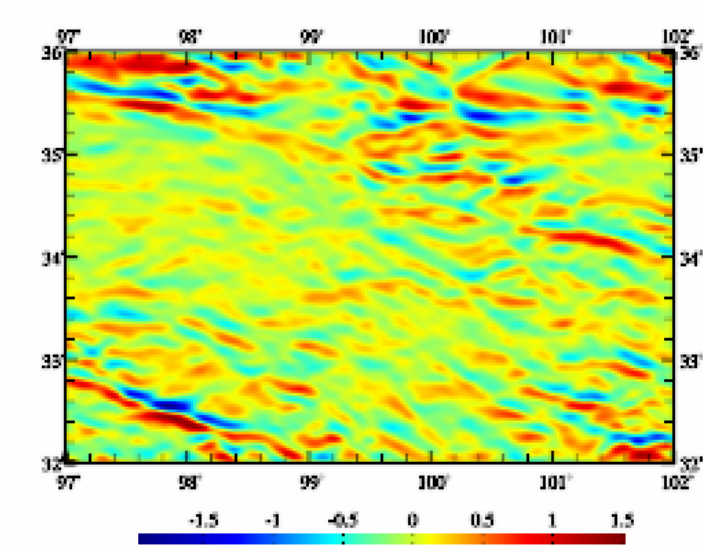
residual terrain model (m)



height anomaly (m)



gravity (anomaly, mGal)



vertical deflection (" , S)

The land-sea residual terrain effect here is defined as the short-wave and ultra-short-wave components of the land-sea complete Bouguer effect. Since the normal gravity field keeps unchanged, the residual terrain effect on the gravity disturbance and gravity anomaly is always equal to the residual terrain effect on gravity.

The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also employed to separate land and sea areas. Since the finite radius integral cannot deal with terrain zero-degree term, the program removes the average of the residual terrain model (RTM) before integral.

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Numerical integral of land-sea residual terrain effects on various gravity field elements
 FFT algorithm of land-sea residual terrain effects on various gravity field elements
 Calculator of land-sea unified residual terrain effect or complete Bouguer effect

Select gravity field elements

height anomaly (m)
 gravity (anomaly/disturbance, mGal)
 vertical deflection (" , SW)
 disturbing gravity gradient (E, radial)

Integral radius

>> Computation Process ** Operation Prompts

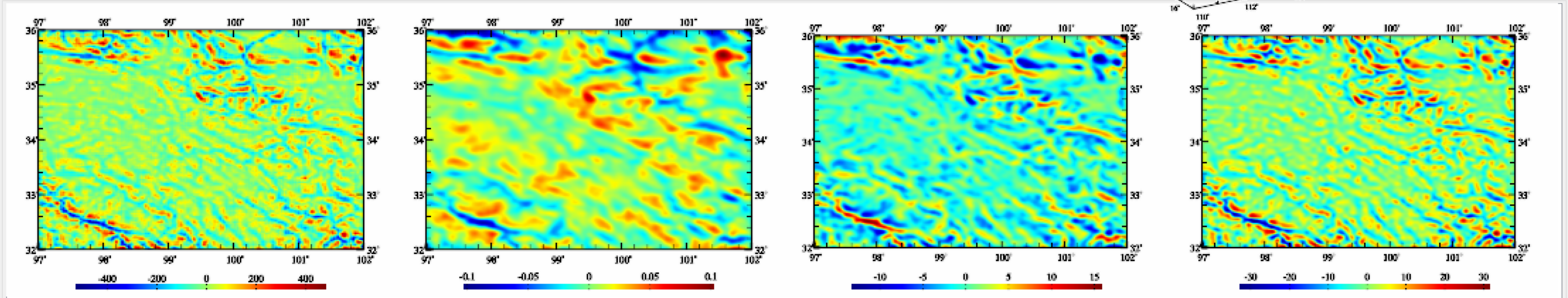
```

>> Open the high-resolution land-sea terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1m.dat.
>> Open the land-sea low-pass terrain model file C:/PAGravf4.5_win64en/examples/Renterrianeffect/landtm1mlvb.dat.
>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landbmsurfhgt.dat.
>> Open the ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/Renterrianeffect/landgeoidhgt.dat.
>> Compute the land-sea unified residual terrain effects using 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT1.txt.
** At the same time, the program also outputs the residual terrain effect grid files on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection (*.dft) or (disturbing) gravity gradient (*.grr) into the current directory, where * is the output file name entered from the interface.
The program outputs residual terrain effect grid file on the specified type of elements
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] button
>> Computation start time: 2024-09-22 13:02:25
>> Complete the computation of land-sea unified residual terrain effects!
>> Computation end time: 2024-09-22 13:02:51
    
```

Fast algorithm

```

C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT1.ksi
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT1.gra
C:/PAGravf4.5_win64en/examples/Renterrianeffect/surfFFT1.grr
    
```






residual terrain model (m)
 height anomaly (m)
 gravity (anomaly, mGal)
 disturbing gradient (E, R)

● The land-sea residual terrain effect here is defined as the short-wave and ultra-short-wave components of the land-sea complete Bouguer effect. Since the normal gravity field keeps unchanged, the residual terrain effect on the gravity disturbance and gravity anomaly is always equal to the residual terrain effect on gravity.

● The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also employed to separate land and sea areas. Since the finite radius integral cannot deal with terrain zero-degree term, the program removes the average of the residual terrain model (RTM) before integral.


Calculator of land-sea unified residual terrain effect

-  Open high-resolution land-sea terrain model file
-  Open the land-sea low-pass terrain model file
-  Open the ellipsoidal height grid file of the land-sea surface

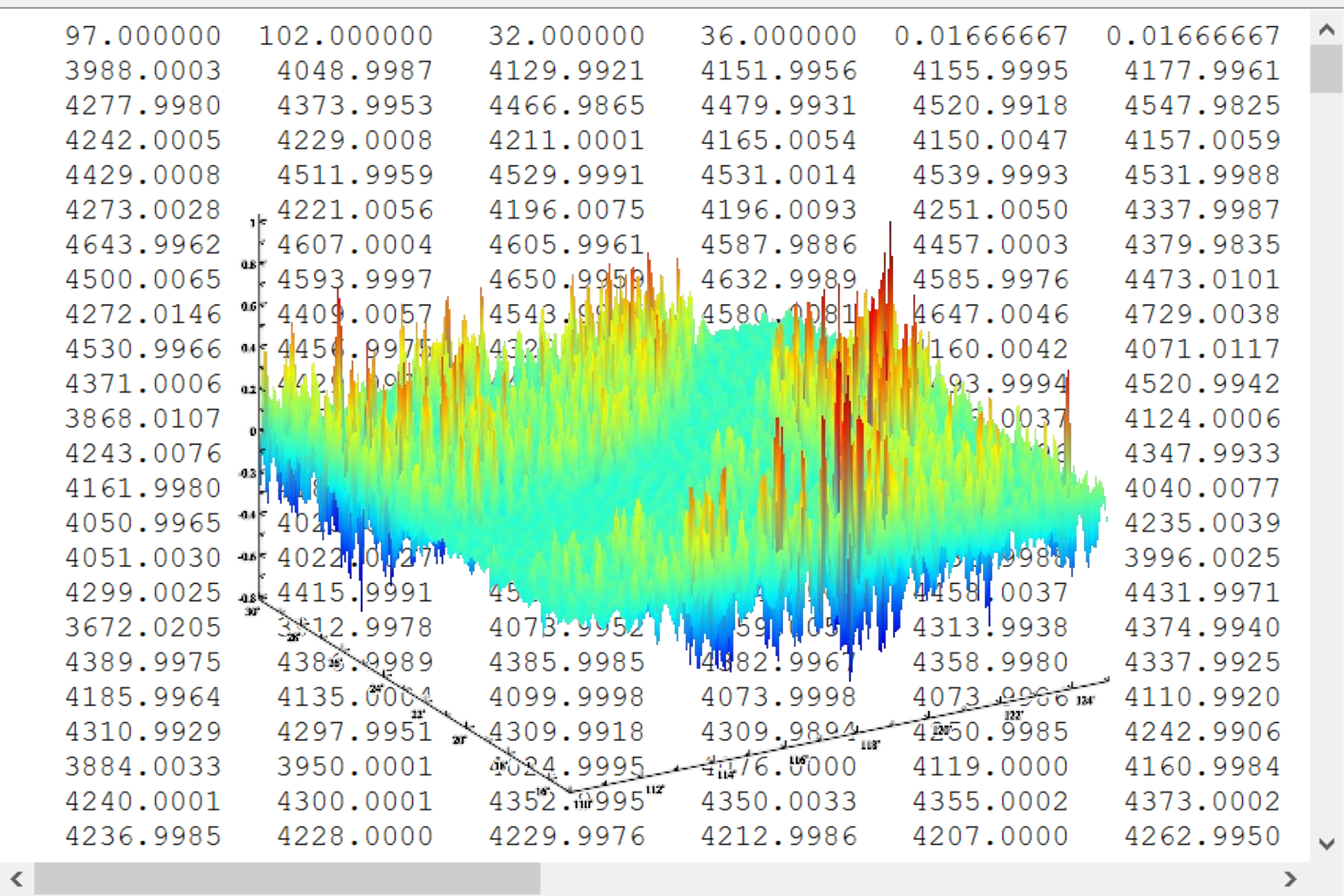
Input geodetic coordinates of calculation point

longitude	<input type="text" value="98.240000°"/>
latitude	<input type="text" value="32.428000°"/>
ellipsoidal height	<input type="text" value="2017.830m"/>

Integral radius

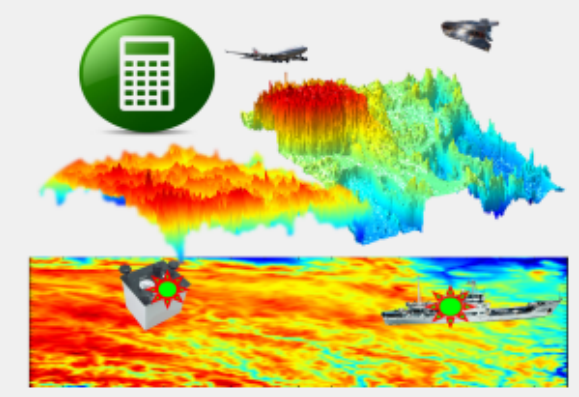
 Start calculation



High-resolution land-sea terrain model



Residual terrain / complete Bouguer effect calculation results

height anomaly (m)	<input type="text" value="0.0094"/>	gravity (anomaly/disturbance, mGal)	<input type="text" value="-7.1398"/>
vertical deflection (" , S)	<input type="text" value="-2.3612"/>	vertical deflection (" , W)	<input type="text" value="-0.9987"/>
(disturbing) gradient (E, radial)	<input type="text" value="13.2737"/>		



-  Inputting the high-resolution land-sea terrain model, low-pass land-sea terrain model and ellipsoidal height grid file of the land-sea surface with the same grid specifications, the button [Start Calculation] becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the residual terrain / complete Bouguer effects on various field elements can be computed and displayed in time.
-  The program allows to replace the three grid files above at any time from the interface, or to change the integral radius, and these user inputs will take effect at once. The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.

Calculator of land-sea unified residual terrain effect

Open high-resolution land-sea terrain model file

Open the land-sea low-pass terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Input geodetic coordinates of calculation point

longitude 100.450000°

latitude 34.428000°

ellipsoidal height 417.830m

Integral radius 90 km

Start calculation

High-resolution land-sea terrain model

97.000000	102.000000	32.000000	36.000000	0.01666667	0.01666667
3988.0003	4048.9987	4129.9921	4151.9956	4155.9995	4177.9961
4277.9980	4373.9953	4466.9865	4479.9931	4520.9918	4547.9825
4242.0005	4229.0008	4211.0001	4165.0054	4150.0047	4157.0059
4429.0008	4511.9959	4529.9991	4531.0014	4539.9993	4531.9988
4273.0028	4221.0056	4196.0075	4196.0093	4251.0050	4337.9987
4643.9962	4607.0004	4605.9961	4587.9886	4457.0003	4379.9835
4500.0065	4593.9997	4650.9999	4632.9999	4585.9976	4473.0101
4272.0146	4409.0057	4431.0057	4431.0057	4407.0046	4729.0038
4530.9966	4411.0075	4431.0075	4431.0075	4407.0042	4071.0117
4371.0006	4411.0075	4431.0075	4431.0075	4407.0042	4520.9942
3868.0107	4411.0075	4431.0075	4431.0075	4407.0042	4124.0006
4243.0076	4411.0075	4431.0075	4431.0075	4407.0042	4347.9933
4161.9980	4411.0075	4431.0075	4431.0075	4407.0042	4040.0077
4050.9965	4411.0075	4431.0075	4431.0075	4407.0042	4235.0039
4051.0030	4411.0075	4431.0075	4431.0075	4407.0042	3996.0025
4299.0025	4411.0075	4431.0075	4431.0075	4407.0042	4431.9971
3672.0205	3912.9978	4073.9952	4159.0051	4313.9938	4374.9940
4389.9975	4386.9999	4385.9985	4382.9967	4358.9980	4337.9925
4185.9964	4135.0004	4099.9998	4073.9998	4073.9998	4110.9920
4310.9929	4297.9951	4309.9918	4309.9918	4250.9985	4242.9906
3884.0033	3950.0001	4024.9995	4076.0000	4119.0000	4160.9984
4240.0001	4300.0001	4352.9995	4350.0033	4355.0002	4373.0002
4236.9985	4228.0000	4229.9976	4212.9986	4207.0000	4262.9950

Residual terrain / complete Bouguer effect calculation results

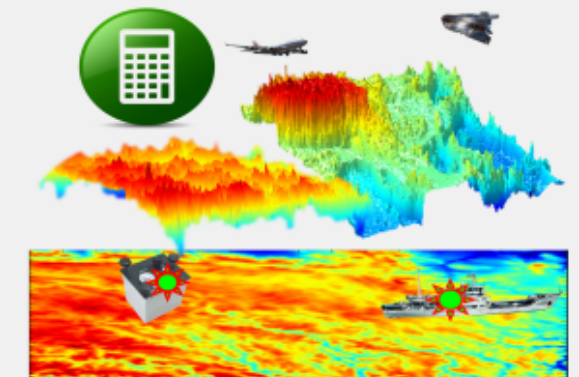
height anomaly (m) 0.0206

gravity (anomaly/disturbance, mGal) -9.2450

vertical deflection (" , S) -0.3546

vertical deflection (" , W) -0.2634

(disturbing) gradient (E, radial) 7.7494



Inputting the high-resolution land-sea terrain model, low-pass land-sea terrain model and ellipsoidal height grid file of the land-sea surface with the same grid specifications, the button [Start Calculation] becomes available. After that, the geodetic coordinates of the calculation point can be input repeatedly, and the residual terrain / complete Bouguer effects on various field elements can be computed and displayed in time.

The program allows to replace the three grid files above at any time from the interface, or to change the integral radius, and these user inputs will take effect at once. The calculation point may be on the geoid or in near-Earth space, that is, from the geoid to the aviation altitude.

Integral of land-sea unified classical gravity Bouguer / equilibrium effect

Open DTM Import parameters Save as Start Computation Save process Follow example



Integral of land-sea unified classical gravity Bouguer / equilibrium effect

Calculator of land-sea unified classical gravity Bouguer / equilibrium effect

Algorithms land-sea unified classic Bouguer and equilibrium effects

Open the land-sea terrain model file

Open the ellipsoidal height grid file of land-sea surface

Select calculation point file format
discrete calculation point file

Open the calculation point location file on land-sea surface

Number of rows of file header 1

Integral radius for local terrain effect 90 km

Integral radius for seawater Bouguer / equilibrium effect 300 km

Equilibrium compensation depth 30 km

>> Computation Process ** Operation Prompts

>> Open the land-sea terrain model file C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dtm5m.dat.
>> Open the ellipsoidal height grid file of land-sea surface C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dbmhgt5m.dat.
>> Open the calculation point location file on land-sea surface C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dbmhgt.txt.

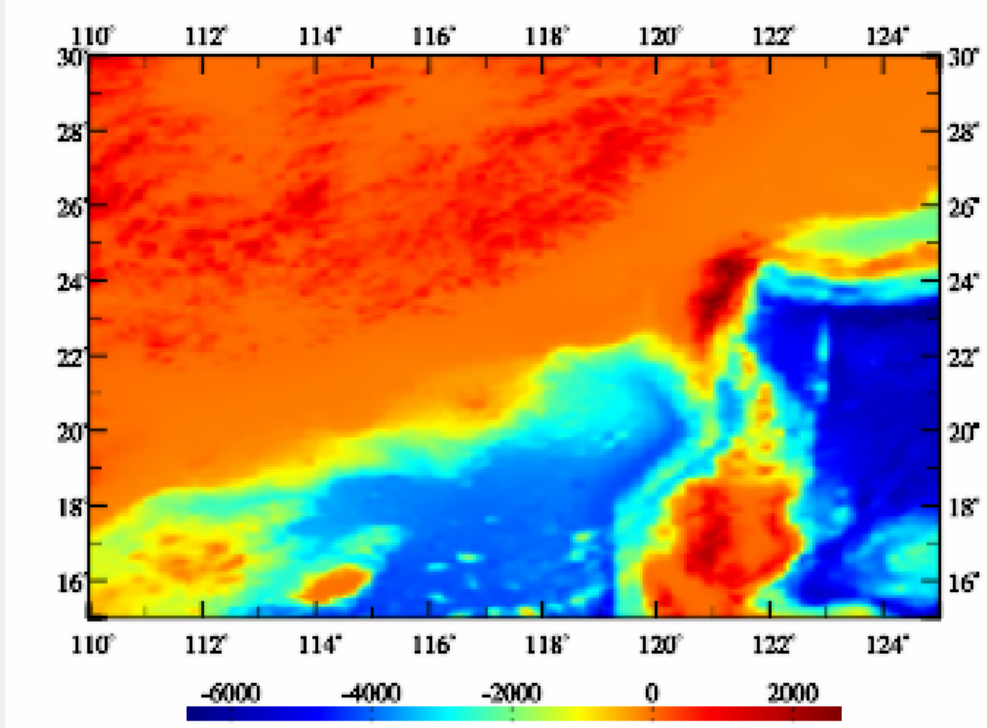
** Look at the file information in the window below, set the input file format parameters...
>> Save the results as C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/rstpnt.txt.
** Behind the source calculation point file record, appends the terrain height/sea depth, local terrain effect, plane layer effect, seawater Bouguer effect, land equilibrium effect, ocean equilibrium effect, total Bouguer effect and total equilibrium effect, a total of 8 attribute values, keeps 4 significant figures.

>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024.09.22 18:31:54

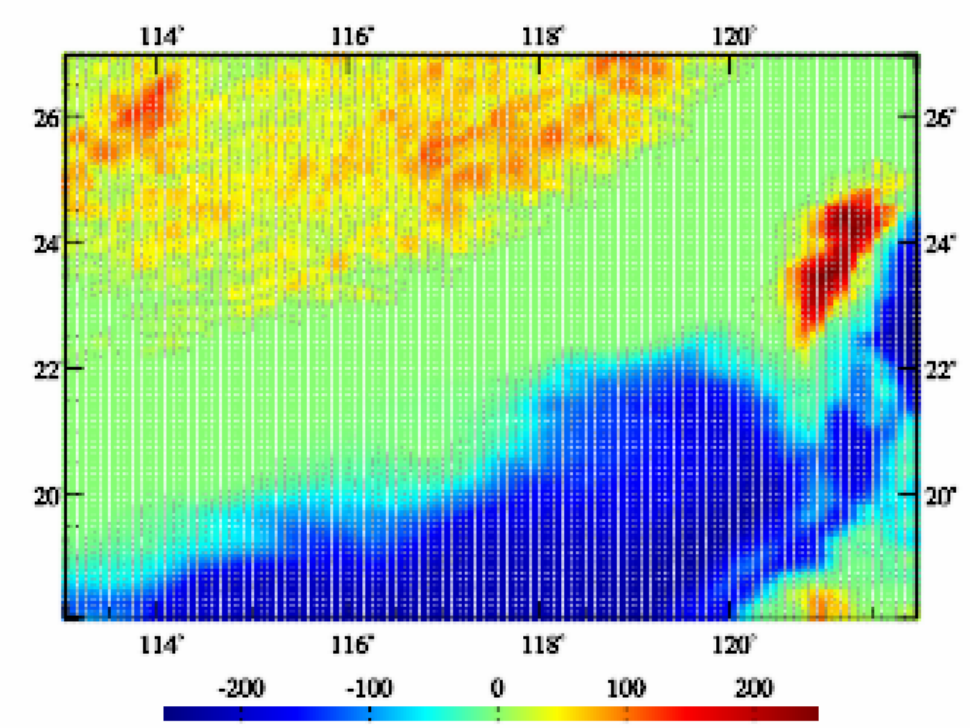
Save the results as Import setting parameters Start Computation

terrian	plane layer	sea-water Bouguer	land equilibrium...						
18.041667	1.4605	-2191.889	0.0000	0.0000	-109.5704	-0.0009	122.0600	-109.5704	12.4887
18.041667	1.7831	-2072.111	0.0000	0.0000	-103.9803	-0.0003	122.3674	-103.9803	18.3868
18.041667	2.1041	-1926.889	0.0000	0.0000	-97.4649	-0.0000	122.9345	-97.4649	25.4695
18.041667	2.4240	-1638.222	0.0000	0.0000	-89.4900	0.0000	124.4235	-89.4900	34.9336

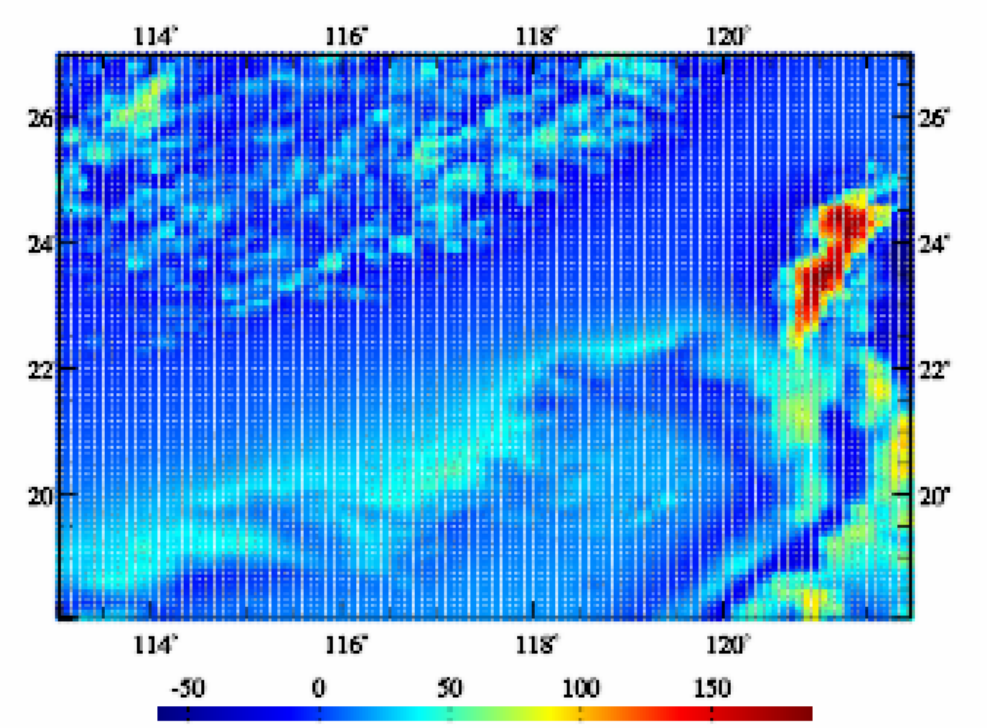
Extract effects Plot



land-sea terrain model (m)



total Bouguer effect (mGal)



total equilibrium effect (mGal)

● Classic Bouguer gravity anomaly on geoid = gravity anomaly at the observed point – total Bouguer effect – analytical continuation of gravity anomaly from the observed point to geoid. Classic Bouguer gravity disturbance on geoid = gravity disturbance at the observed point – total Bouguer effect – analytical continuation of gravity disturbance from the observed point to geoid.
● Classic equilibrium gravity anomaly on geoid = gravity anomaly at the observed point – total equilibrium effect – analytical continuation of gravity anomaly from the observed point to geoid. Classic equilibrium gravity disturbance on geoid = gravity disturbance at the observed point – total equilibrium effect – analytical continuation of gravity disturbance from the observed point to geoid.

Integral of land-sea unified classical gravity Bouguer / equilibrium effect

Open DTM Import parameters Save as Start Computation Save process Follow example

Precise Approach of Earth Gravity Field and Geoid
PAGrav4.5

Algorithms land-sea unified classic Bouguer and equilibrium effects
Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Integral of land-sea unified classical gravity Bouguer / equilibrium effect

Calculator of land-sea unified classical gravity Bouguer / equilibrium effect

Algorithms land-sea unified classic Bouguer and equilibrium effects

Save computation process as

Open the land-sea terrain model file

>> Computation Process ** Operation Prompts

Open the ellipsoidal height grid file of land-sea surface

>> Open the land-sea terrain model file C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dtm5m.dat.

>> Open the ellipsoidal height grid file of land-sea surface C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dbmhgt5m.dat.

>> Open the ellipsoidal height grid file on land-sea calculation surface C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/dbmhgt5m.dat.

>> Save the results as C:/PAGrav4.5_win64en/examples/TerSurfacegravinfl/result.txt.

Select calculation point file format

ellipsoidal height grid file

Open the ellipsoidal height grid file on land-sea calculation surface

** Record format: Point no, longitude, latitude, terrain height/sea depth, local terrain effect, plane layer effect, seawater Bouguer effect, land equilibrium effect, ocean equilibrium effect, total Bouguer effect and total equilibrium effect.

** At the same time, the program also outputs the land-sea total Bouguer effect (*.bgr) and land-sea total equilibrium effect (*.ist) grid files into the current directory, where * is the output file name entered from the interface.

Integral radius for local terrain effect 90 km

Integral radius for seawater Bouguer / equilibrium effect 300 km

Equilibrium compensation depth 30 km

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024.09.22 18:35:45

Save the results as

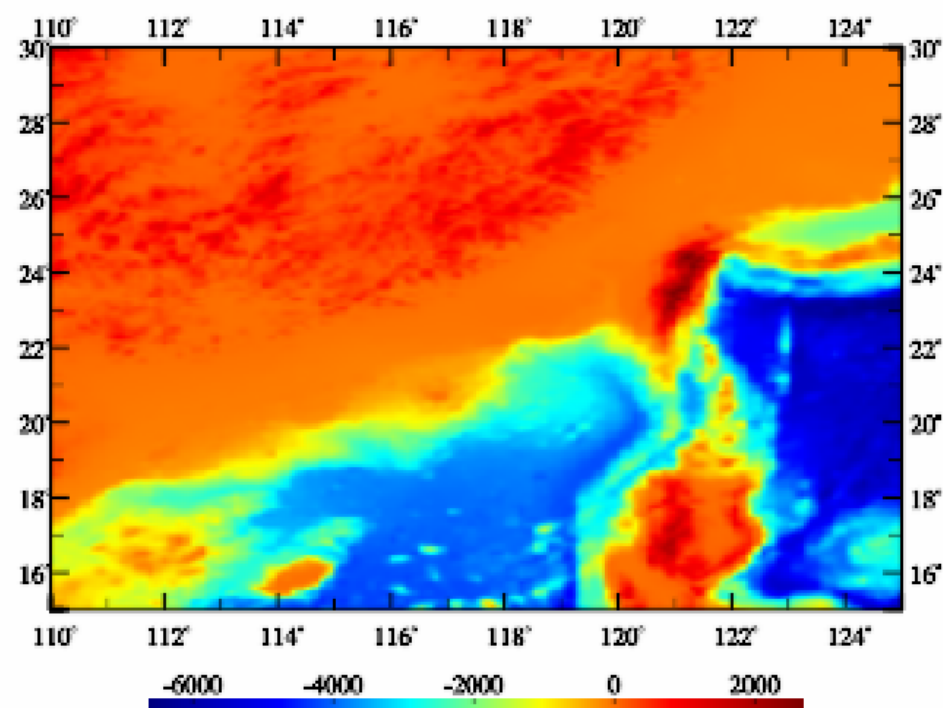
Import setting parameters

Start Computation

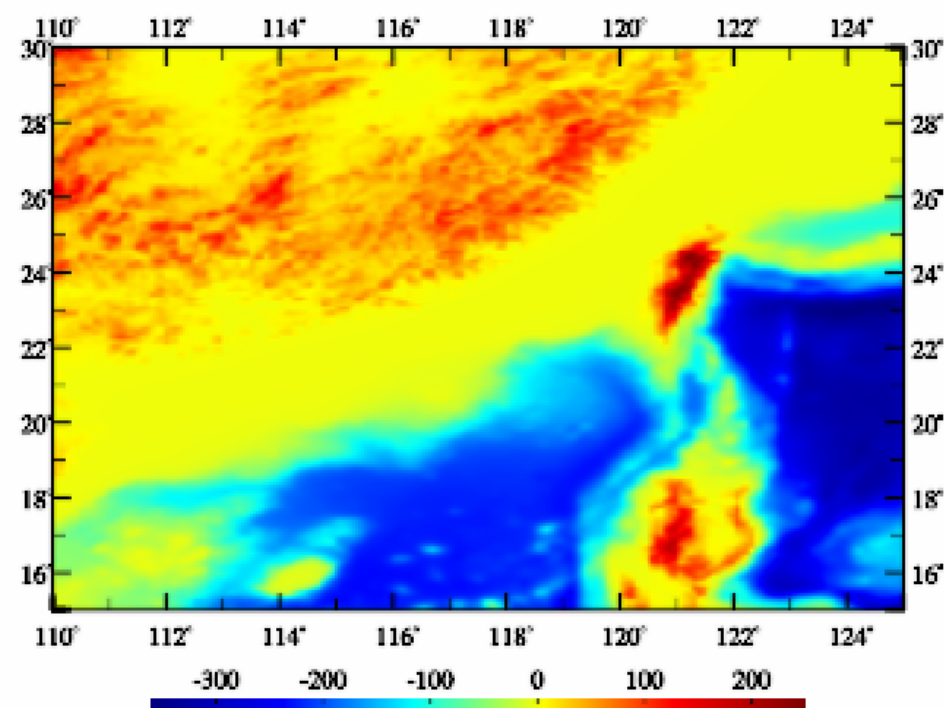
no	lon(deg/decimal)	lat	height/depth	local terrian	plane layer	sea-water Bouguer effect	...
1	110.04167	15.04167	-456.500	0.0000	0.0000	-7.8971	0.0000 12.2480 -7.8971 4
2	110.12500	15.04167	-434.667	0.0000	0.0000	-7.8766	0.0000 14.7200 -7.8766 6
3	110.20833	15.04167	-465.667	0.0000	0.0000	-9.1329	0.0000 17.0115 -9.1329 7
4	110.29167	15.04167	-638.167	0.0000	0.0000	-13.9564	0.0000 19.0292 -13.9564 5

Extract effects

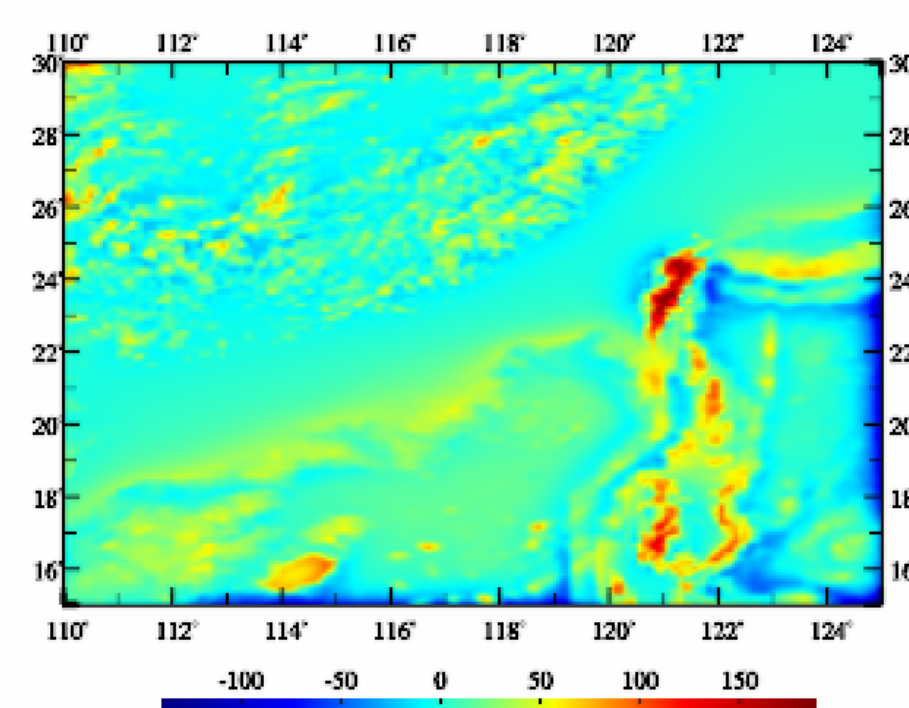
Plot↓



land-sea terrain model (m)



total Bouguer effect (mGal)

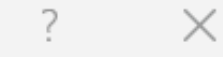


total equilibrium effect (mGal)

● Classic Bouguer gravity anomaly on geoid = gravity anomaly at the observed point – total Bouguer effect – analytical continuation of gravity anomaly from the observed point to geoid. Classic Bouguer gravity disturbance on geoid = gravity disturbance at the observed point – total Bouguer effect – analytical continuation of gravity disturbance from the observed point to geoid.
● Classic equilibrium gravity anomaly on geoid = gravity anomaly at the observed point – total equilibrium effect – analytical continuation of gravity anomaly from the observed point to geoid. Classic equilibrium gravity disturbance on geoid = gravity disturbance at the observed point – total equilibrium effect – analytical continuation of gravity disturbance from the observed point to geoid.

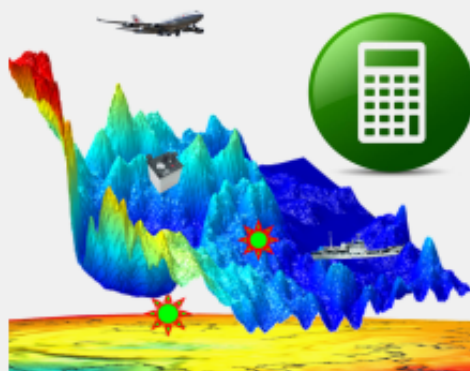


Calculator of land-sea unified classical gravity Bouguer / equilibrium effect



Open the land-sea terrain model file

Open the ellipsoidal height grid file of land-sea surface



Integral radius for local terrain effect

Integral radius for seawater Bouguer /equilibrium effect

Equilibrium compensation depth

Input geodetic coordinates of calculation point on land-sea surface

longitude latitude

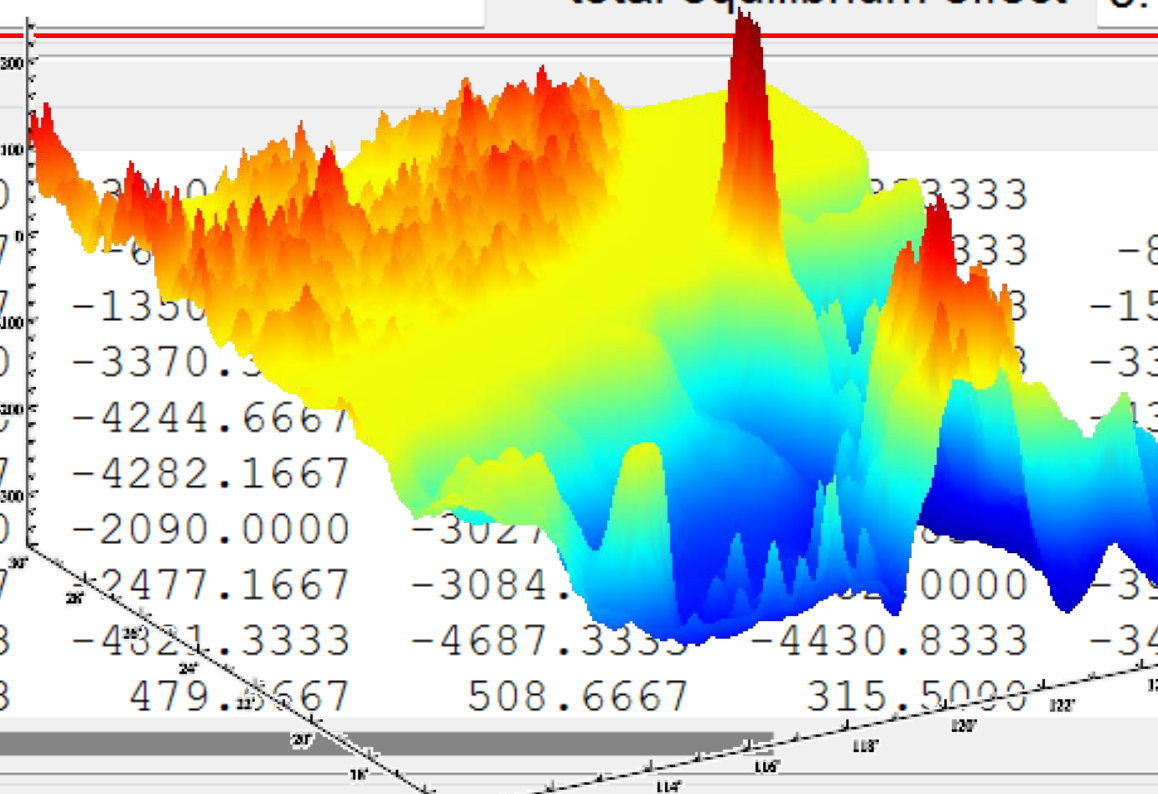
Start calculation

Terrain effects (mGal) at the calculation point on

land height/sea depth	400.3811 m	local terrain effect	-0.4405
plane layer effect	44.8300	seawater Bouguer effect	-0.0000
land equilibrium effect	-39.2525	ocean equilibrium effect	0.0000
total Bouguer effect	44.3896	total equilibrium effect	5.1370

Land-sea terrain model

110.000000	125.000000	15.000000	20.000000	25.000000	30.000000	35.000000	40.000000	45.000000	50.000000
-456.5000	-434.6667	-465.6667	-465.6667	-465.6667	-465.6667	-465.6667	-465.6667	-465.6667	-465.6667
-1253.8333	-1290.3333	-1321.6667	-1350.0000	-1375.0000	-1400.0000	-1425.0000	-1450.0000	-1475.0000	-1500.0000
-2604.3333	-2767.5000	-2971.5000	-3370.3333	-3869.1667	-4468.0000	-5166.8333	-5965.6667	-6864.5000	-7863.3333
-4315.0000	-4281.8333	-4269.0000	-4244.6667	-4222.3333	-4200.0000	-4177.6667	-4155.3333	-4133.0000	-4110.6667
-4158.6667	-4285.5000	-4289.1667	-4282.1667	-4275.1667	-4268.1667	-4261.1667	-4254.1667	-4247.1667	-4240.1667
-3536.6667	-2641.6667	-2227.0000	-2090.0000	-3027.1667	-3864.3333	-4701.5000	-5538.6667	-6375.8333	-7213.0000
-4036.8333	-3508.1667	-3080.6667	-2477.1667	-3084.1667	-3691.1667	-4298.1667	-4905.1667	-5512.1667	-6119.1667
-4273.1667	-4475.5000	-4593.3333	-4821.3333	-4687.3333	-4430.8333	-3924.3333	-3417.8333	-2911.3333	-2404.8333
7.1667	180.3333	237.8333	479.1667	508.6667	315.5000	122.3333	-70.8333	-163.9667	-257.1000

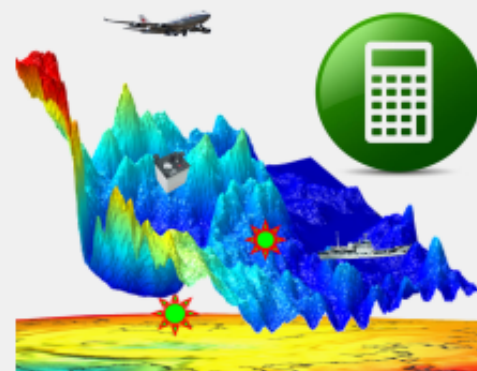


- Using + to indicate greater than zero, and - to indicate less than zero, there are always: plane layer effect (+), seawater Bouguer effect (-), land equilibrium effect (-), ocean equilibrium effect (+).
- In the coastal sea area, there are local terrain effects and land equilibrium effects. In the offshore land area, there are also seawater Bouguer effects and ocean equilibrium effects.

Calculator of land-sea unified classical gravity Bouguer / equilibrium effect

Open the land-sea terrain model file

Open the ellipsoidal height grid file of land-sea surface



Integral radius for local terrain effect

Integral radius for seawater Bouguer /equilibrium effect

Equilibrium compensation depth

Input geodetic coordinates of calculation point on land-sea surface

longitude latitude

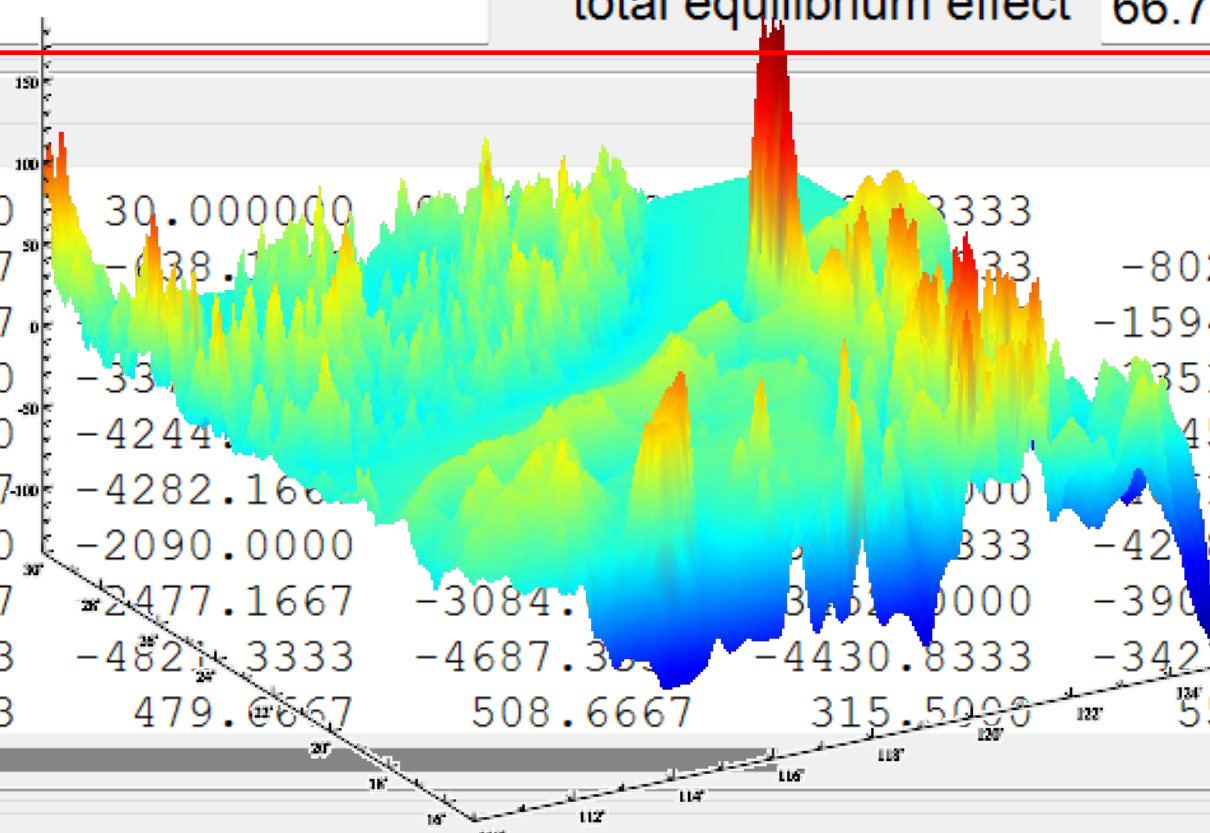
Start calculation

Terrain effects (mGal) at the calculation point on

land height/sea depth	-2187.1242 m	local terrain effect	0.0017
plane layer effect	0.0000	seawater Bouguer effect	-61.3520
land equilibrium effect	-1.2635	ocean equilibrium effect	129.3990
total Bouguer effect	-61.3503	total equilibrium effect	66.7853

Land-sea terrain model

110.000000	125.000000	15.000000	30.000000	3333				
-456.5000	-434.6667	-465.6667	-438.1667	333	-802.6667	-775.3333	-763.833	
-1253.8333	-1290.3333	-1321.6667	-33	3333	-1594.5000	-1622.6667	-1623.833	
-2604.3333	-2767.5000	-2971.5000	-4244.1667	3333	-351.0000	-3388.0000	-3409.833	
-4315.0000	-4281.8333	-4269.0000	-4282.1667	3333	45.0000	-4336.3333	-4305.666	
-4158.6667	-4285.5000	-4289.1667	-2090.0000	3333	-4218.8333	-4260.8333	-4299.000	
-3536.6667	-2641.6667	-2227.0000	-2477.1667	-3084.1667	-3901.3333	-4096.3333	-4237.166	
-4036.8333	-3508.1667	-3080.6667	-4821.3333	-4687.3333	-4430.8333	-3423.5000	-3013.0000	-2808.000
-4273.1667	-4475.5000	-4593.3333	479.6667	508.6667	315.5000	55.0000	23.8333	13.833



Using + to indicate greater than zero, and - to indicate less than zero, there are always: plane layer effect (+), seawater Bouguer effect (-), land equilibrium effect (-), ocean equilibrium effect (+).

In the coastal sea area, there are local terrain effects and land equilibrium effects. In the offshore land area, there are also seawater Bouguer effects and ocean equilibrium effects.

Ultrahigh degree spherical harmonic analysis of global land-sea terrain model

Open file Save as Import parameters Start computation Save process Follow example

Construction of global surface data grid in spherical coordinates

Ultrahigh degree spherical harmonic analysis of global land-sea terrain model

Algorithm of spherical harmonic analysis and synthesis of land-sea terrain masses

Open global land-sea terrain model grid in spherical coordinate system

Set iteration termination condition

Residual standard deviation threshold (a) 1.0 ‰

Termination condition of residual decrease (b) 1.0 ‰

Simultaneously output terrain geopotential coefficient model

>> Computation Process ** Operation Prompts

** 16th iteration. the residual standard deviation = 7.243e+04
 ** 17th iteration. the residual standard deviation = 7.169e+04
 ** 18th iteration. the residual standard deviation = 7.103e+04
 ** 19th iteration. the residual standard deviation = 7.045e+04
 ** 20th iteration. the residual standard deviation = 6.993e+04
 ** 21th iteration. the residual standard deviation = 6.947e+04
 ** standard deviation of global land-sea terrain = 41.76m.

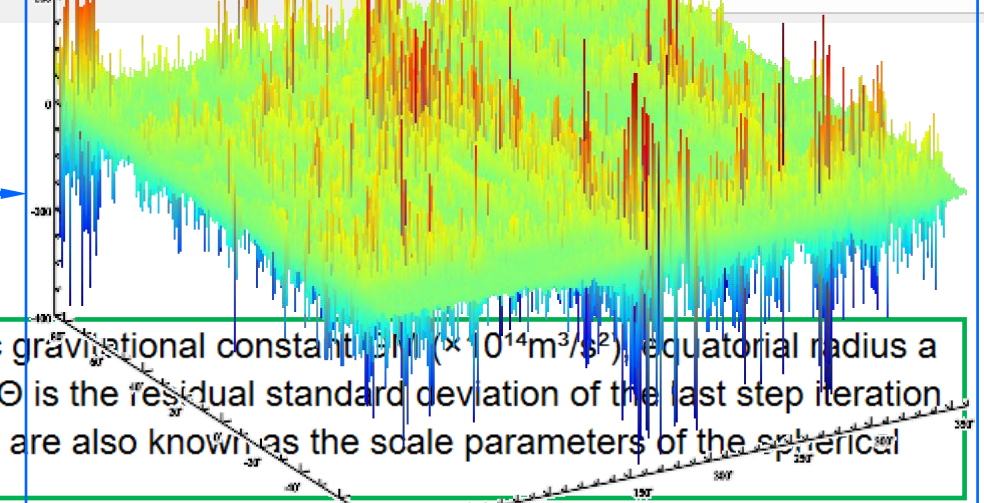
>> The file header of the spherical harmonic coefficient model: the geocentric gravitational constant μ ($\times 10^{14} \text{m}^3/\text{s}^2$), equatorial radius a (m) of the Earth, zero-degree term $a\Delta C_{00}$ (kg/m^2), relative error Θ (%), where Θ is the residual standard deviation of the last step iteration as a percentage of the standard deviation of the source grid values, and μ, a are also known as the scale parameters of the spherical harmonic coefficient model.

>> The program also outputs the global land-sea terrain geopotential coefficient model file *geop.dat into the current directory, where * is the file name of the global land-sea terrain mass spherical harmonic coefficient model.

>> Complete the ultrahigh degree spherical harmonic analysis of global land-sea terrain model!

>> Computation end time: 2024-09-22 19:30:22

Computation process as



Save the results as

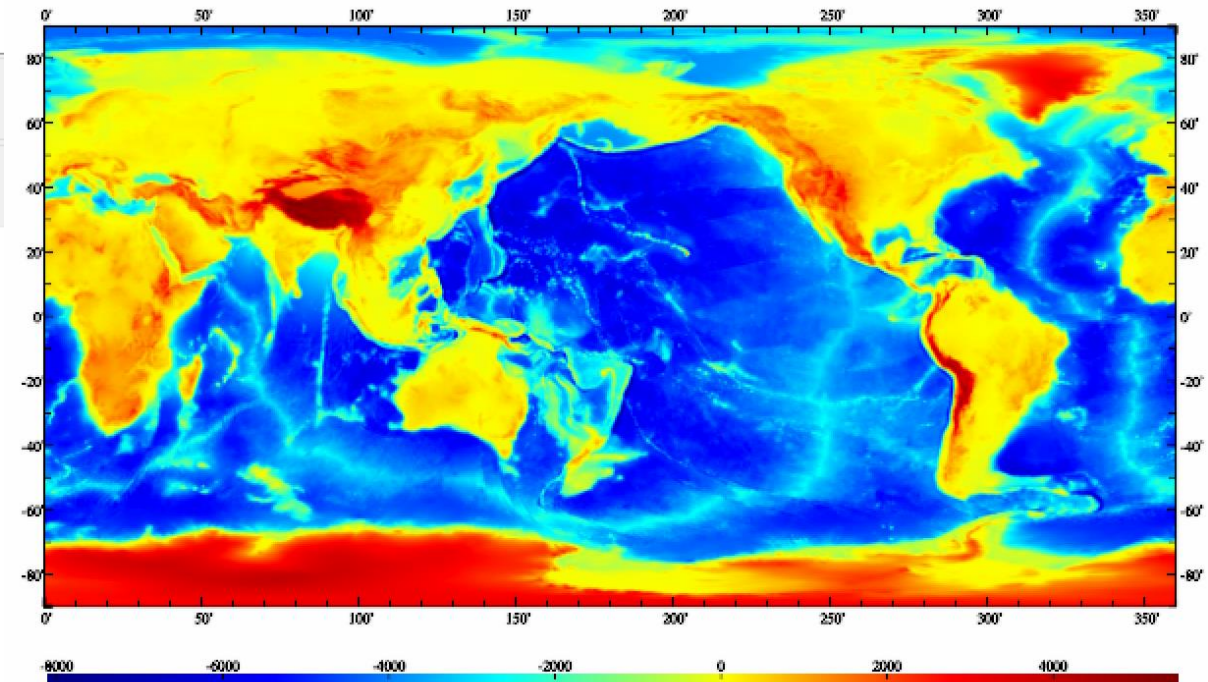
Save residual DTM as

Import setting parameters

Display of the input-output file ↓

```

3.986004415 6378136.30 -3667855.301 2.521
1 0 1.7136617466283444E-01 0.0000000000000000E+00
1 1 1.6662830460947373E-01 1.1455495760110544E-01
2 0 1.6336327492305205E-01 0.0000000000000000E+00
2 1 8.4790436862281993E-02 9.1248955791892794E-02
2 2 -1.1820159432578198E-01 -1.6730453760116247E-02
3 0 -6.4915287439358635E-02 0.0000000000000000E+00
3 1 -4.4601487637124751E-02 4.0150215900756667E-02
3 2 -1.3058410613568169E-01 1.2619038828971818E-01
3 3 3.7363651282940558E-02 1.5252641909794926E-01
4 0 1.0060940799382276E-01 0.0000000000000000E+00
4 1 -5.9865766035864118E-02 -8.3251300057076774E-02
4 2 -1.1442732934894125E-01 1.9235264166930027E-02
4 3 1.0098478651494894E-01 -4.2950380278059655E-02
4 4 -1.1646562236291021E-02 1.2919605986189289E-01
5 0 -1.6569492084399357E-01 0.0000000000000000E+00
5 1 -7.2051327049100396E-03 -1.9203743552770599E-02
    
```



0.0	360.0	-90.0	90.0	0.50000000	0.50000000
2734.91	2735.40	2735.93	2736.53	2737.08	2737.61
2743.65	2744.20	2744.92	2745.57	2746.21	2746.86
2753.34	2754.16	2754.80	2755.49	2756.19	2756.79
2764.09	2764.85	2765.68	2766.57	2767.32	2768.02
2776.18	2776.96	2777.86	2778.81	2779.69	2780.46
2789.14	2790.07	2791.04	2791.81	2792.59	2793.41
2801.59	2802.21	2802.88	2803.60	2804.26	2804.90
2811.06	2811.66	2812.18	2812.57	2813.07	2813.50
2817.19	2817.38	2817.57	2817.83	2818.18	2818.39
2819.57	2819.61	2819.63	2819.63	2819.68	2819.74
2819.26	2819.25	2819.13	2819.09	2819.18	2819.03

- The degree n of the spherical harmonic coefficients model is equal to the number of grids in the SN direction of the $0.25^\circ \times 0.25^\circ$ land-sea terrain model.
- The land terrain areal density, always greater than zero, represents the topographic mass per unit area, which is equal to the land terrain density multiplied by the grid area.
- The ocean terrain areal density, always less than zero, represents the compensation masses of the sea water per unit area, which is equal to the seawater density multiplied by the grid area minus the land terrain density multiplied by the grid area.

Calculation of model value for complete Bouguer or residual terrain effects

Open calculation file Save as Import parameters Start Computation Save process Follow example

Precise Approach of Earth Gravity Field and Geoid
PAGravf4.5

Save computation process as
Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Calculation of model value for complete Bouguer or residual terrain effects

Calculator of global land-sea terrain effects model

Calculation and analysis of spectral character of global terrain effects model

Open global land-sea terrain mass spherical harmonic coefficient model file

Select calculation file format
Discrete calculation point file

Open space calculation point file

Set input point file format
Number of rows of file header 1
Column ordinal number of ellipsoidal height in the record 4

Select elements to be calculated

- terrain height/sea depth (m)
- height anomaly (m)
- gravity anomaly/disturbance (mGal)
- vertical deflection (" , SW)
- disturbing gradient (E, radial)
- tangential gradient (E, NW)
- disturbing potential/geopotential (m²/s²)

Minimum degree 361
Maximum degree 720

Extract effects Plot

>> Computation Process ** Operation Prompts

>> [Function] From global land-sea terrain mass spherical harmonic coefficient model (kg/m²), calculate the model value of terrain height/sea depth, as well as the land-sea unified complete Bouguer or residual terrain effects on the height anomaly (m), gravity (anomaly/disturbance, mGal), vertical deflection vector (" , south, west), (disturbing) gravity gradient (E, radial), tangential gravity gradient vector (E, north, west), or (disturbing) geopotential (m²/s²) on the geoid or in whole outer Earth space.

** Click the [Open global land-sea terrain mass spherical harmonic coefficient model file] control button or [Open terrain model] tool button...

>> Open global land-sea terrain mass spherical harmonic coefficient model file C:/PAGravf4.5_win64en/data/ETOPOCs1800.dat.

** The window below only shows the spherical harmonic coefficients data with no more than 2000 rows in it.

>> Open space calculation point file C:/PAGravf4.5_win64en/examples/TerHarmrntinfluence/calcpnt.txt.

** Look at the file information in the window below and set the discrete point file format...

>> Save the results as C:/PAGravf4.5_win64en/examples/TerHarmrntinfluence/rstpnt.txt.

** Behind the record of the calculation point file, appends one or more columns of model values of complete Bouguer or residual terrain effects, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

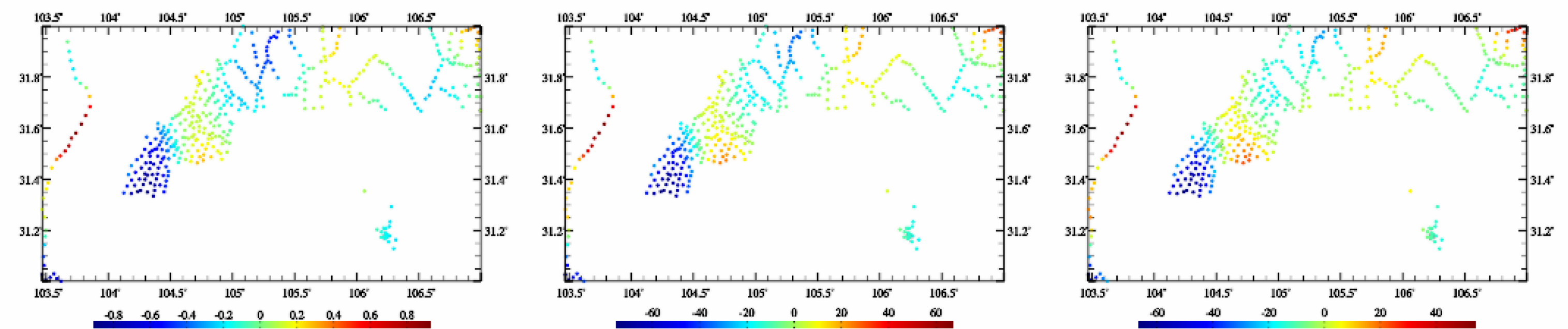
** Click the [Start Computation] control button, or the [Start Computation] tool button...

** The calculation process need wait, during which you can open the output file to look at the calculation progress...

>> Computation start time: 2024.09.22 19:42:27

Save the results as Import setting parameters Start Computation

number (value or st)	long (degree/decimal)	lat (degree/decimal)	ellipHeight (m)
3248	103.671939	31.938051	2743.9394
3249	103.696944	31.864721	2501.2449
3250	103.718330	31.831114	2435.4206
3251	103.735559	31.795280	2366.5700
3252	103.777216	31.776390	2294.0304
3253	103.822773	31.758333	2233.2317
3254	103.849717	31.724168	2215.6606



height anomaly (m) gravity effect (mGal) disturbing gradient (E, R)

The program is suitable for the unified computation of the complete Bouguer and residual terrain effects on various gravity field elements in land, land-sea junction and sea area. The calculation point may be on the geoid or in whole outer Earth space.

Calculation of model value for complete Bouguer or residual terrain effects

Open calculation file Save as Import parameters Start Computation Save process Follow example

Calculation of model value for complete Bouguer or residual terrain effects

Calculator of global land-sea terrain effects model

Calculation and analysis of spectral character of global terrain effects model

Open global land-sea terrain mass spherical harmonic coefficient model file

Select calculation file format
Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

- Select elements to be calculated
- terrain height/sea depth (m)
 - height anomaly (m)
 - gravity (anomaly/disturbance, mGal)
 - vertical deflection (" SW)
 - (disturbing) gradient (E, radial)
 - tangential gradient (E, NW)
 - disturbing potential/geopotential (m²/s²)

Minimum degree 361
Maximum degree 720

Extract effects Plot

>> Computation Process ** Operation Prompts

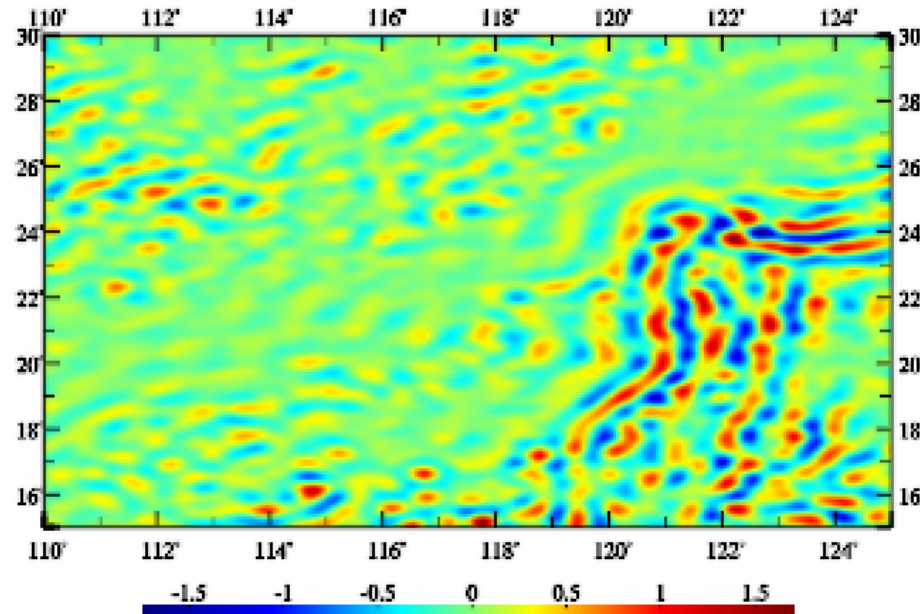
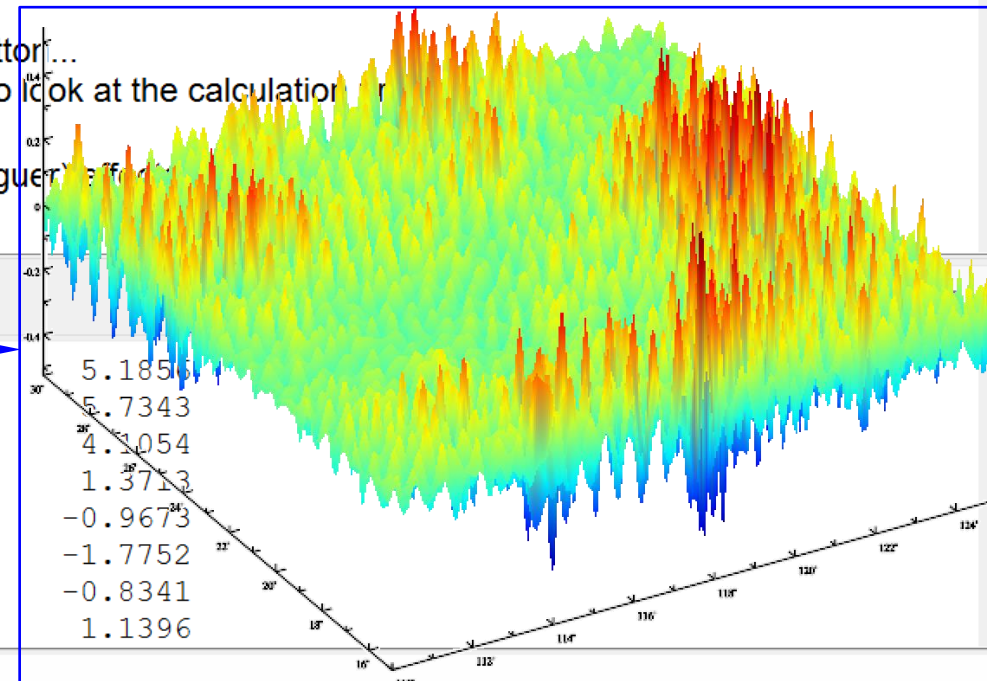
>> Complete the calculation of the model value for residual terrain (complete Bouguer) effects!
>> Computation end time: 2024-09-22 19:57:51
>> Open ellipsoidal height grid file of calculation surface C:/PAGravf4.5_win64en/examples/TerHarmrntinfluence/dbmhgt5m.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/TerHarmrntinfluence/result.txt.
** The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of complete Bouguer or residual terrain effects.
** The program also outputs the model value grid files for the terrain height/sea depth (m), complete Bouguer or residual terrain effects on height anomaly (*.ksi), gravity (anomaly/disturbance, *.gra), vertical deflection vector (*.dft), (disturbing) gravity gradient (*.grr), tangential gravity gradient vector (*.hgd) or (disturbing) geopotential (*.get) into the current directory. Where * is the output file name entered from the interface.

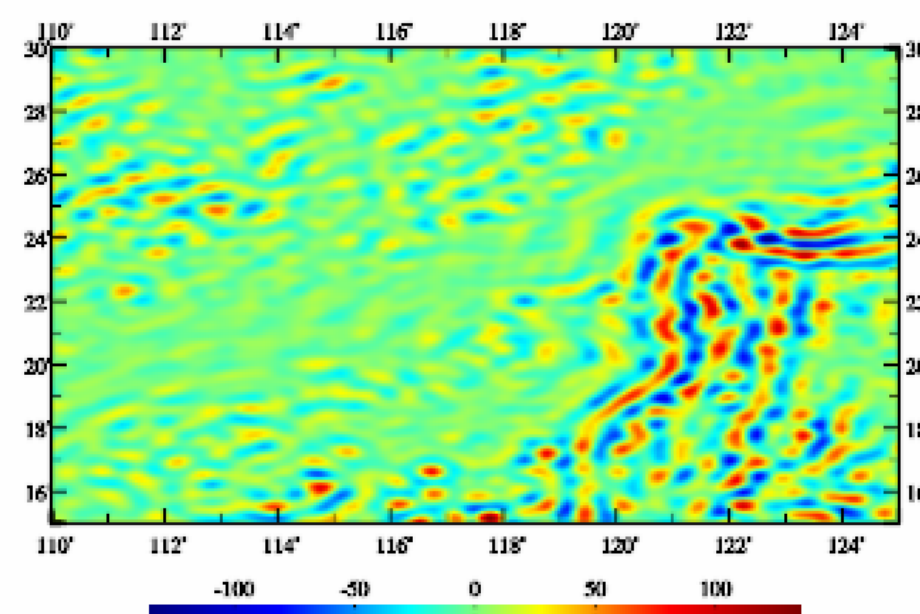
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
** The calculation process need wait, during which you can open the output file to look at the calculation
>> Computation start time: 2024-09-22 19:59:42
>> Complete the calculation of the model value for residual terrain (complete Bouguer) effects!
>> Computation end time: 2024-09-22 20:12:32

Save the results as Import setting parameters

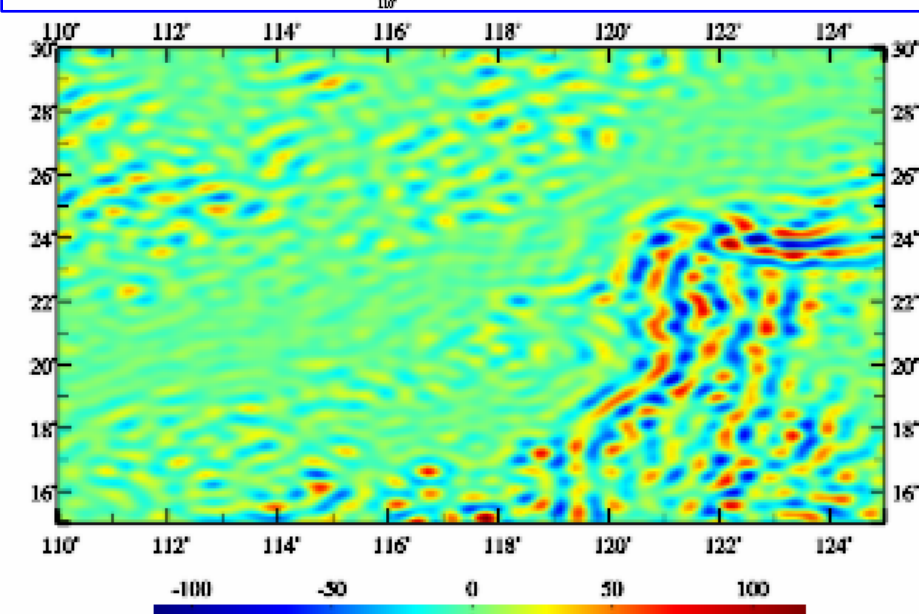
1	110.04167	15.04167	-1.947	0.1195	7.4827
2	110.12500	15.04167	-1.724	0.1476	8.8020
3	110.20833	15.04167	-1.484	0.1315	7.1302
4	110.29167	15.04167	-1.222	0.0825	3.5905
5	110.37500	15.04167	-0.937	0.0231	-0.0144
6	110.45833	15.04167	-0.628	-0.0245	-2.1472
7	110.54167	15.04167	-0.295	-0.0484	-2.2535
8	110.62500	15.04167	0.061	-0.0499	-0.8811



height anomaly (m)



gravity effect (mGal)



disturbing gradient (E, R)

The program is suitable for the unified computation of the complete Bouguer and residual terrain effects on various gravity field elements in land, land-sea junction and sea area. The calculation point may be on the geoid or in whole outer Earth space.

Calculator of global land-sea terrain effects model



Open global land-sea terrain mass spherical harmonic coefficient model file

When opening an ultrahigh degree global land-sea terrain mass spherical harmonic model file, the program need read and initialize, please wait...

Minimum degree 361

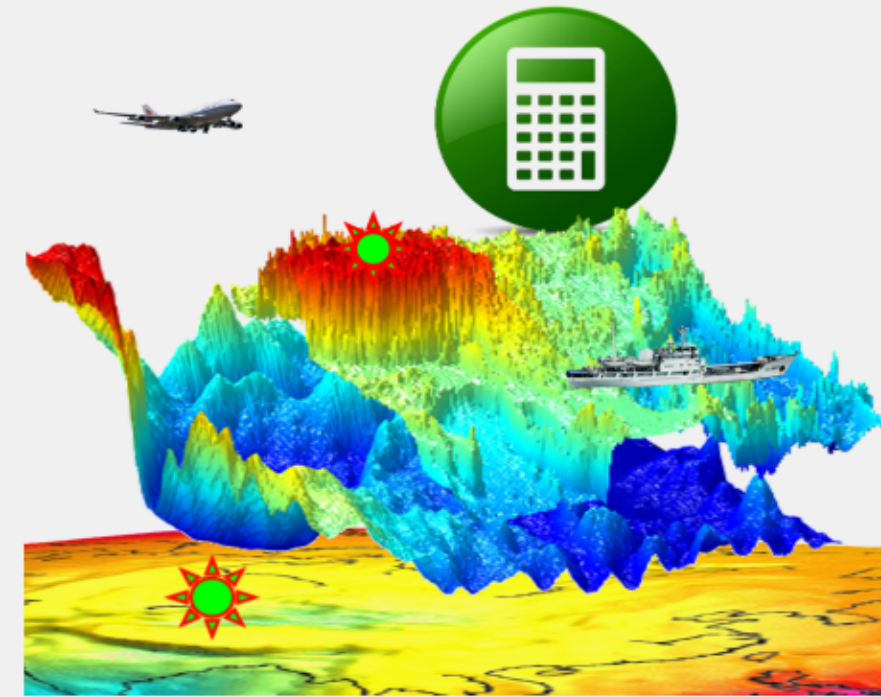
Maximum degree 1800

Input the geodetic coordinates of calculation point

longitude 121.240000°

latitude 29.428100°

ellipsoidal height 17.830m



Start Calculation

Model values of land-sea unified complete Bouguer or residual terrain effects

terrain height/sea depth (m) 520.04

gravity (anomaly/disturbance, mGal) 57.9119

height anomaly (m) 0.4661

vertical deflection (" , S) 0.2286

vertical deflection (" , W) 1.3582

(disturbing) gradient (E, radial) 94.2959

tangential gradient (E, N) -16.2491

tangential gradient (E, W) -77.8878

(disturbing) geopotential (m²/s²) 4.5643

Global land-sea terrain mass spherical harmonic coefficient model

```

3.986004415  6378136.30  -3666611.637  1.478
1  0  1.7073567878991658E-01  0.0000000000000000E+00
1  1  1.6633036628733813E-01  1.1479210613310797E-01
2  0  1.6429313329998932E-01  0.0000000000000000E+00
2  1  8.5035152210278894E-02  9.1333502848550255E-02
2  2  -1.1793912586067470E-01  -1.7411465069800628E-02
3  0  -6.5349154204352972E-02  0.0000000000000000E+00
3  1  -4.4184211923815692E-02  4.0618031845130055E-02
3  2  -1.3069109856940694E-01  1.2578589265181686E-01
3  3  3.6582125575328230E-02  1.5294533153047263E-01
4  0  1.0192376884714217E-01  0.0000000000000000E+00
4  1  -5.9905008831126150E-02  -8.3292685493168567E-02
4  2  -1.1471261607043508E-01  1.9460308775542352E-02
    
```

The relative error Θ (%) of the model

Calculator of global land-sea terrain effects model



Open global land-sea terrain mass spherical harmonic coefficient model file

When opening an ultrahigh degree global land-sea terrain mass spherical harmonic model file, the program need read and initialize, please wait...

Minimum degree 361

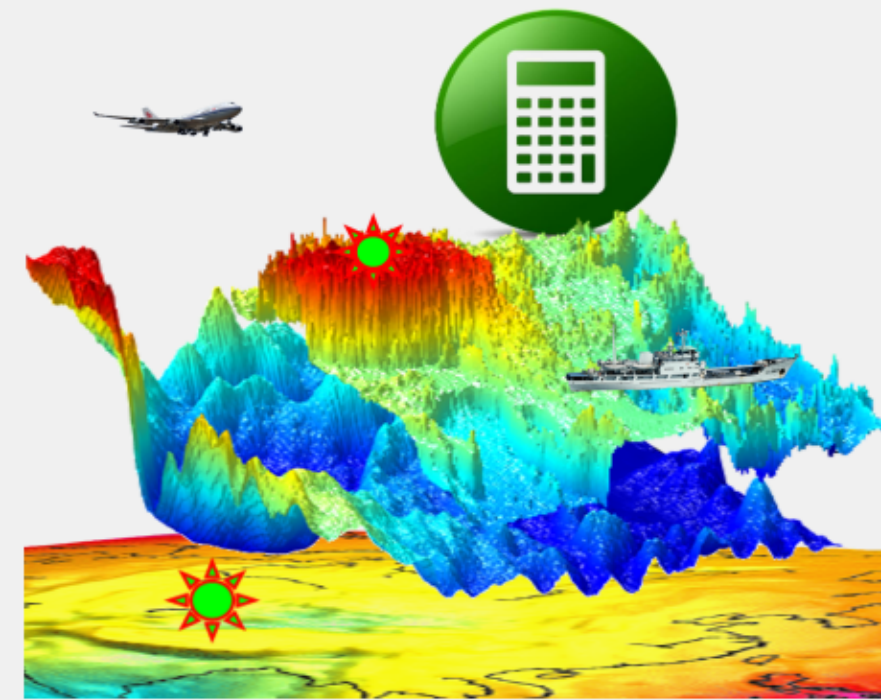
Maximum degree 1800

Input the geodetic coordinates of calculation point

longitude 132.240000°

latitude 21.428100°

ellipsoidal height 1.830m



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PAGravf4.5

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Start Calculation

Model values of land-sea unified complete Bouguer or residual terrain effects

terrain height/sea depth (m) -5950.95

gravity (anomaly/disturbance, mGal) -40.4123

height anomaly (m) -0.2083

vertical deflection (" , S) -5.2269

vertical deflection (" , W) -0.7046

(disturbing) gradient (E, radial) -91.6757

tangential gradient (E, N) 67.2680

tangential gradient (E, W) 24.2020

(disturbing) geopotential (m²/s²) -2.0384


Global land-sea terrain mass spherical harmonic coefficient model


```


3.986004415  6378136.30  -3666611.637  1.478
1  0  1.7073567878991658E-01  0.0000000000000000E+00
1  1  1.6633036628733813E-01  1.1479210613310797E-01
2  0  1.6429313329998932E-01  0.0000000000000000E+00
2  1  8.5035152210278894E-02  9.1333502848550255E-02
2  2  -1.1793912586067470E-01  -1.7411465069800628E-02
3  0  -6.5349154204352972E-02  0.0000000000000000E+00
3  1  -4.4184211923815692E-02  4.0618031845130055E-02
3  2  -1.3069109856940694E-01  1.2578589265181686E-01
3  3  3.6582125575328230E-02  1.5294533153047263E-01
4  0  1.0192376884714217E-01  0.0000000000000000E+00
4  1  -5.9905008831126150E-02  -8.3292685493168567E-02
4  2  -1.1471261607043508E-01  1.9460308775542352E-02
    
```


The relative error Θ (%) of the model

Calculation and analysis of spectral character of global terrain effects model

 Open global land-sea terrain mass spherical harmonic coefficient model file

 Open high-degree geopotential model file

 Save the results as

 Start Calculation

Display of the input-output file

2	3.125000E-01	6.715451E+00	7.911381E-02
3	8.641975E-02	3.952913E+00	8.823035E-02
4	3.515625E-02	2.312997E+00	2.289217E-02
5	1.760000E-02	1.416801E+00	1.366044E-02
6	1.003086E-02	4.389914E-01	8.191773E-03
7	6.247397E-03	2.654210E-01	5.675256E-03
8	4.150391E-03	9.823847E-02	2.379274E-03
9	2.895900E-03	1.038844E-01	1.819157E-03
10	2.100000E-03	7.850419E-02	1.264171E-03
11	1.570931E-03	3.775911E-02	6.892058E-04
12	1.205633E-03	2.646725E-02	2.284380E-04
13	9.453451E-04	2.874715E-02	5.736342E-04
14	7.548938E-04	2.222554E-02	2.158315E-04
15	6.123457E-04	1.544843E-02	1.950448E-04
16	5.035400E-04	1.479913E-02	1.898962E-04
17	4.190563E-04	1.517999E-02	1.308700E-04
18	3.524615E-04	8.631766E-03	1.393244E-04

Precise Approach of Earth Gravity Field and Geoid
PAGravf4.5



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Start end row number 150

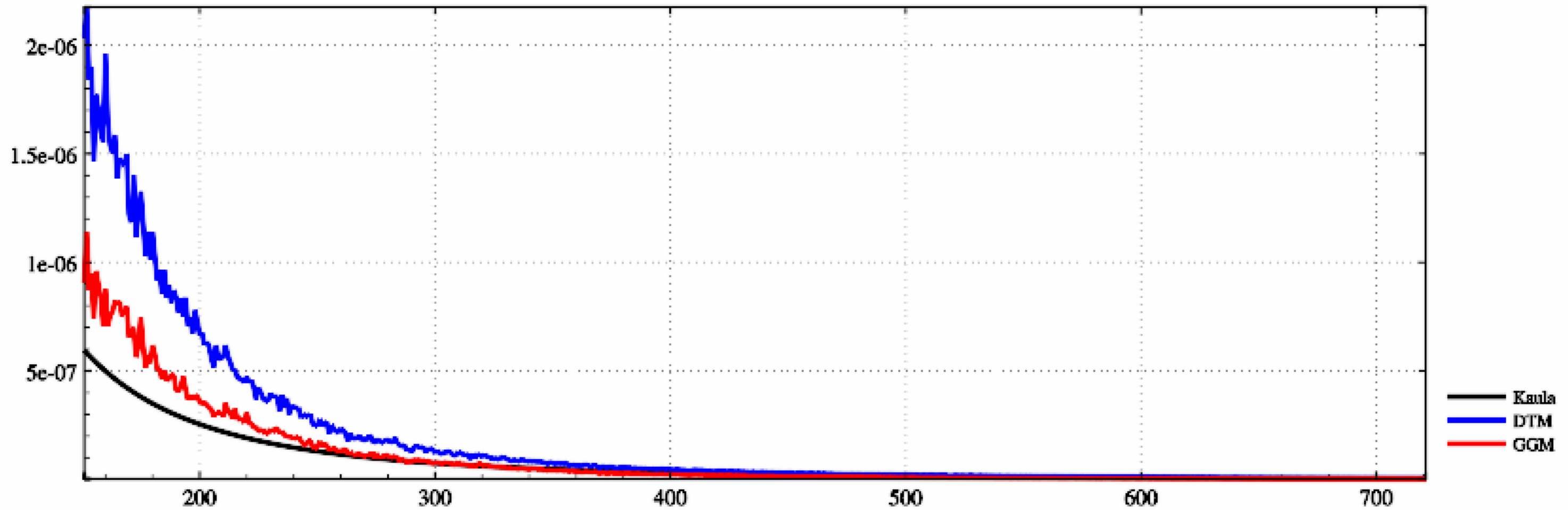
720

Line thickness 3

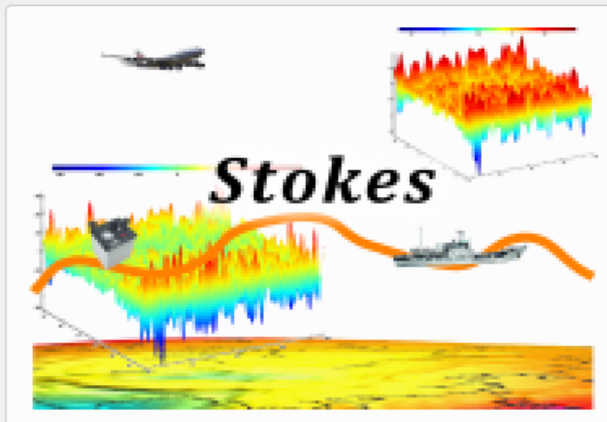
Chart plot↓

 Save current plot as

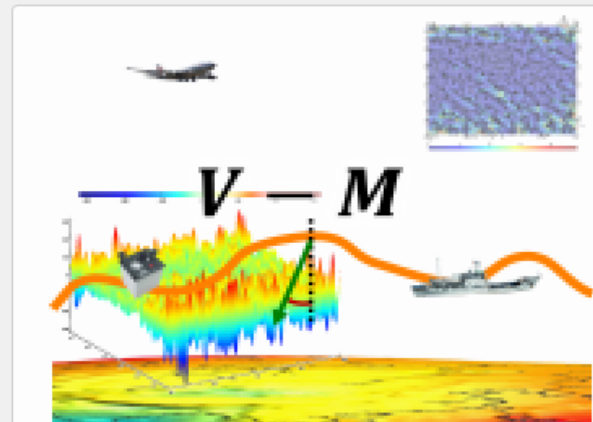
Degree variance curves



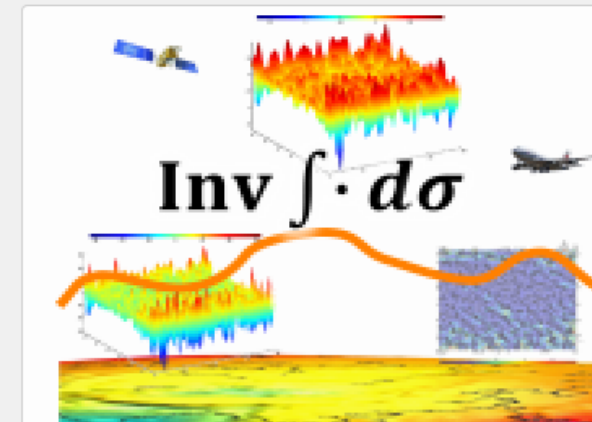
Precise approach and all-element modeling on Earth gravity field



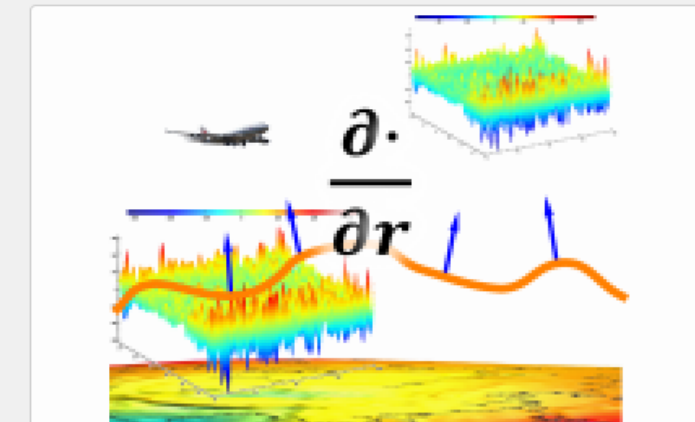
External height anomaly computation using Stokes/Hotine integral



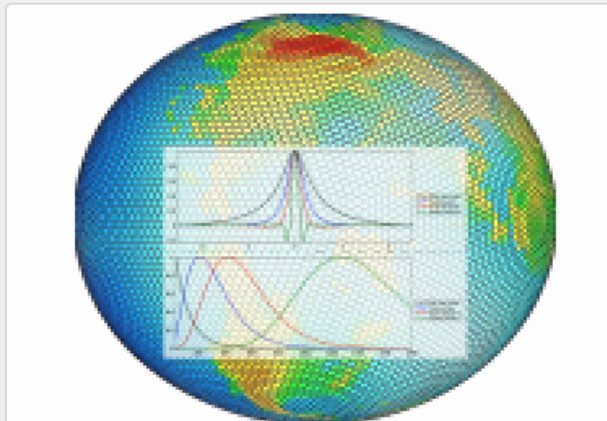
External vertical deflection computation using Vening-Meinesz integral



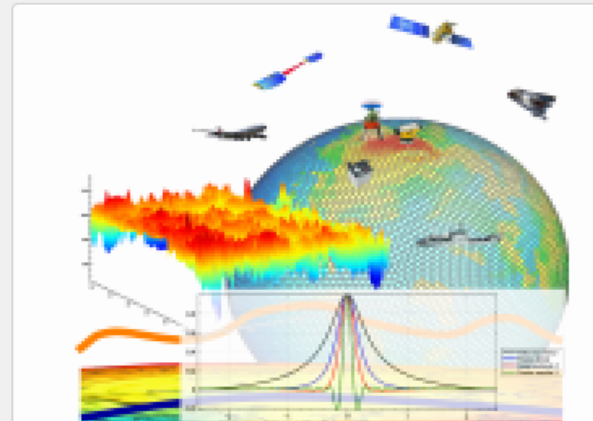
Inverse integral and integral of inverse operation on anomalous field element



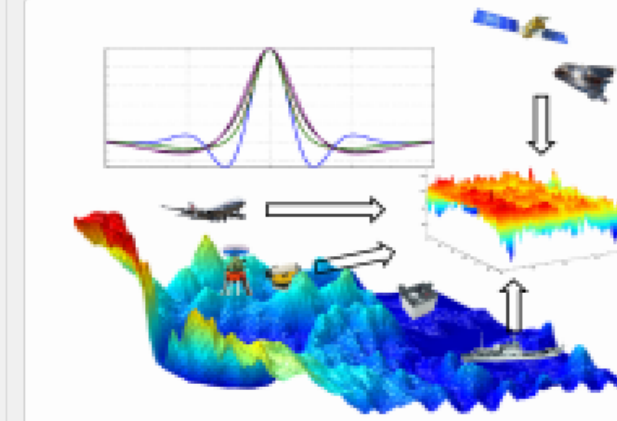
Gradient and Poisson integral computation of external gravity field element



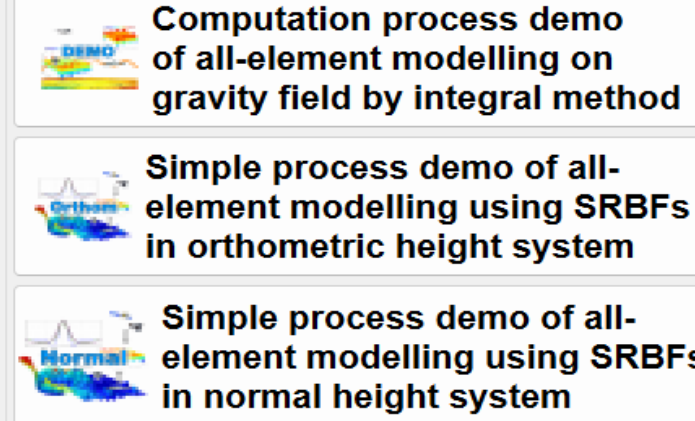
Feature and performance analysis of spherical radial basis functions



Gravity field approach using SRBFs in spectral domain and performance test



All-element modelling on gravity field using SRBFs from heterogeneous observations



Computation process demo of all-element modelling on gravity field by integral method

Simple process demo of all-element modelling using SRBFs in orthometric height system

Simple process demo of all-element modelling using SRBFs in normal height system

Modeling process exercise of regional gravity field and geoid

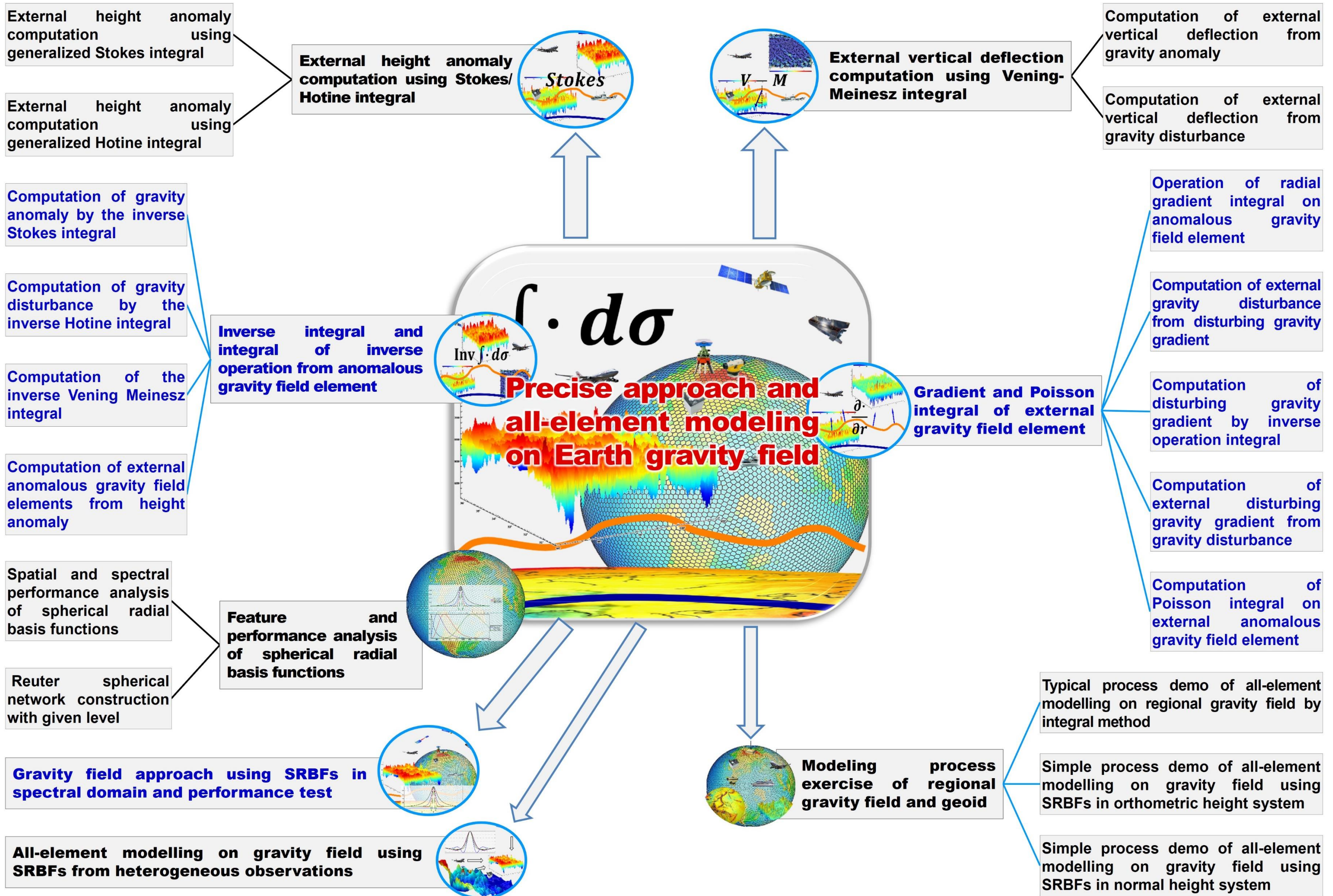
- Cross aliasing of heterogeneous observations in land-sea-space
- All-element modeling on Earth gravity field in whole outer space

- Loop closed analytical operations on outer gravity field elements
- Index measurement of observation errors and computation control

Programs and functions structure of the subsystem

● PAGravf4.5 sets up the scientific gravity field approach system with the spatial domain integration algorithms based on boundary value theory and spectral domain radial basis function approach algorithms to realize the all-element analytical modelling on gravity field in whole space outside the geoid from various heterogeneous observations in the different altitudes, cross-distribution and land-sea coexisting cases.

● The typical complex gravity field feature area selected where residual gravity disturbance variation exceeds 300mGal after the 540-degree reference model value removed, you can verify and analyze the performance of various gravity field approach algorithms in this group of programs to facilitate and quickly grasp the characteristics and usage of these algorithms.



External height anomaly computation using generalized Stokes integral - Numerical



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
number of rows of file header: 1
column ordinal number of ellipsoidal height in the record: 4

>> Computation Process ** Operation Prompts

** Input the ellipsoidal height grid file of the equipotential surface and the gravity anomaly/disturbance grid file on the surface with the same grid specification...

>> [Function] From the ellipsoidal height grid of the equipotential surface and gravity anomaly (mGal) grid on the surface, compute the external residual height anomaly (m) by the Stokes integral.

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landgeoidhgt.dat.

>> Open residual gravity anomaly grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/resGMlgeoid541_1800.gra.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/rststk.txt.

** Record format: Behind the source calculation point file record, appends a column of residual height anomaly calculated, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 10:57:07

>> Complete the computation of the height anomaly outside the geoid!

>> Computation end time: 2024-09-23 10:58:45

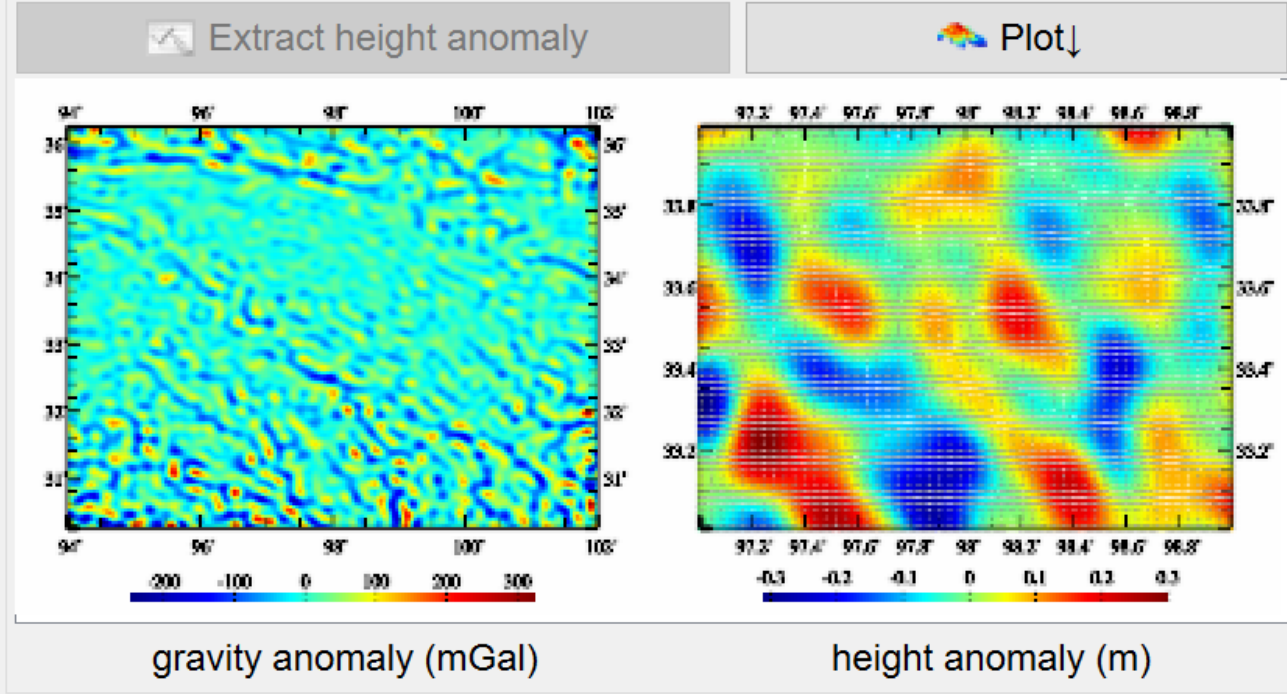
Integral radius: 180 km

Save the results as

Import setting parameters

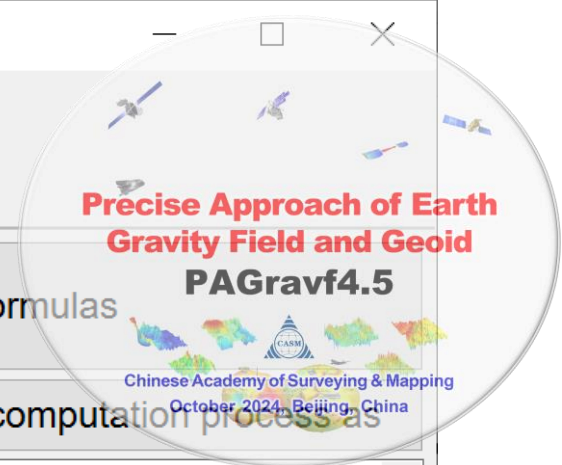
Start Computation

no	lon(degree/decimal)	lat	ellipHeight(m)	
1	97.008333	33.008333	3942.764	-0.0294
2	97.025000	33.008333	3989.787	-0.0340
3	97.041667	33.008333	4034.817	-0.0404
4	97.058333	33.008333	4070.847	-0.0485
5	97.075000	33.008333	4106.877	-0.0582
6	97.091667	33.008333	4119.913	-0.0693
7	97.108333	33.008333	4115.946	-0.0817
8	97.125000	33.008333	4090.977	-0.0952
9	97.141667	33.008333	4070.007	-0.1090
10	97.158333	33.008333	3991.047	-0.1235
11	97.175000	33.008333	3985.070	-0.1362
12	97.191667	33.008333	3956.107	-0.1475
13	97.208333	33.008333	3965.137	-0.1552
14	97.225000	33.008333	3964.173	-0.1592
15	97.241667	33.008333	3983.205	-0.1581
16	97.258333	33.008333	3953.251	-0.1526



- Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Stokes integral - Numerical



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Save computation process as

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm

numerical integral

>> Computation Process ** Operation Prompts

```
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:03:17
>> [Function] From the ellipsoidal height grid of the equipotential surface and gravity anomaly (mGal) grid on the surface, compute the external residual height anomaly (m) by the Stokes integral.
>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landgeoidhgt.dat.
>> Open residual gravity anomaly grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/resGMlgeoid541_1800.gra.
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landbmsurfhgt.dat.
>> Compute external residual height anomaly by numerical integral...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/stokesnintg.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:04:56
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:34:09
```

Integral radius 180 km

Save the results as

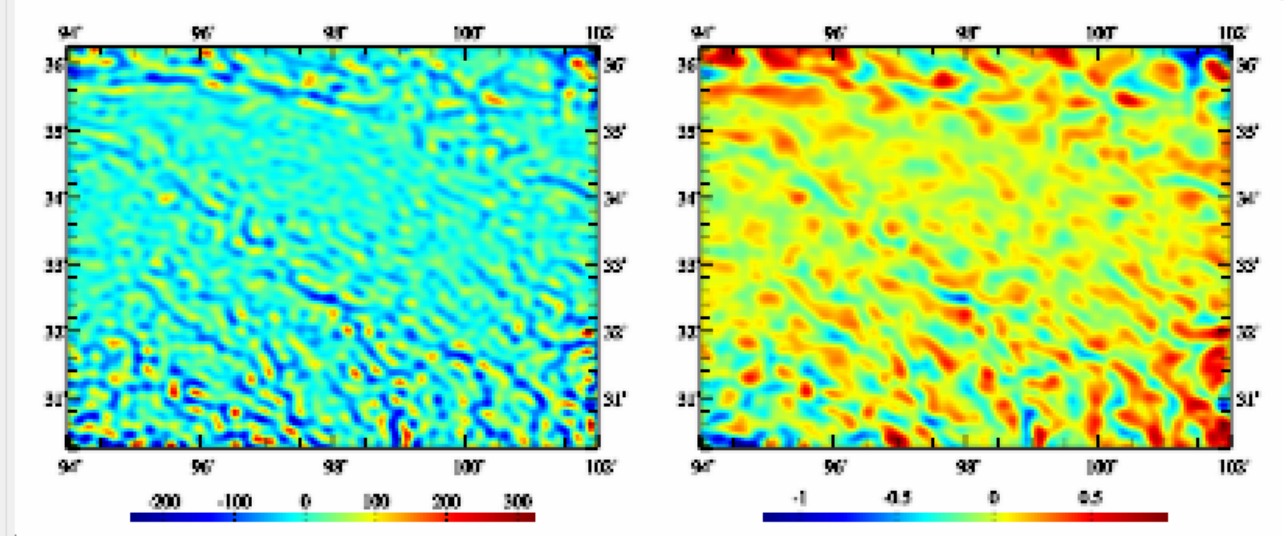
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0985	-0.0918	-0.0929	-0.1025	-0.1184	-0.1397	-0.1641
-0.3691	-0.3790	-0.3864	-0.3924	-0.3988	-0.4062	-0.4160
-0.7265	-0.7631	-0.8020	-0.8354	-0.8626	-0.8929	-0.9039
-1.0120	-1.0246	-1.0271	-1.0019	-0.9528	-0.8930	-0.8092
0.1001	0.1635	0.2066	0.2352	0.2495	0.2417	0.2169
-0.2854	-0.3400	-0.3918	-0.4330	-0.4706	-0.4958	-0.5033
0.1690	0.2420	0.2994	0.3331	0.3416	0.3352	0.3029
-0.2588	-0.2453	-0.2122	-0.1673	-0.1158	-0.0692	-0.0300
-0.0422	-0.0655	-0.0880	-0.1094	-0.1292	-0.1468	-0.1629
-0.2292	-0.2297	-0.2287	-0.2252	-0.2187	-0.2084	-0.1941
0.0855	0.0932	0.0876	0.0708	0.0422	0.0045	-0.0408
-0.2274	-0.1866	-0.1405	-0.0918	-0.0407	0.0079	0.0533
0.4118	0.4248	0.4271	0.4192	0.3997	0.3698	0.3315
0.0589	0.0536	0.0500	0.0468	0.0435	0.0399	0.0360
0.1401	0.1539	0.1599	0.1580	0.1466	0.1258	0.0957

Extract height anomaly

Plot



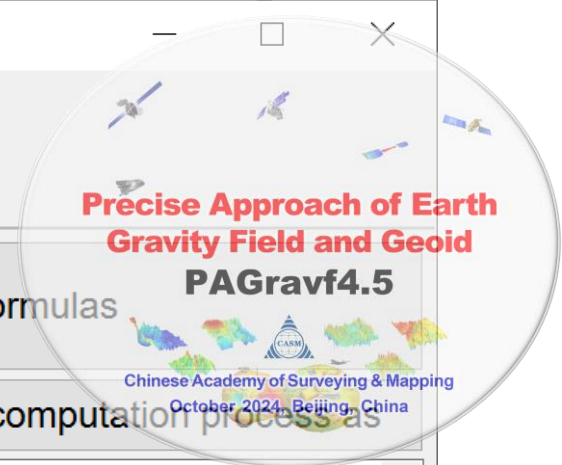
gravity anomaly (mGal)

height anomaly (m)

- Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Stokes integral - FFT

Import parameters Save as Start Computation Save process Follow example



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
2D FFT algorithm

>> Computation Process ** Operation Prompts

```

resGMlgeoid541_1800.gra.
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landbmsurfhgt.dat.
>> Compute external residual height anomaly by numerical integral...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/stokesnintg.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:04:56
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:34:09
>> Compute external residual height anomaly by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/stokesFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:39:25
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:39:27
    
```

Save computation process

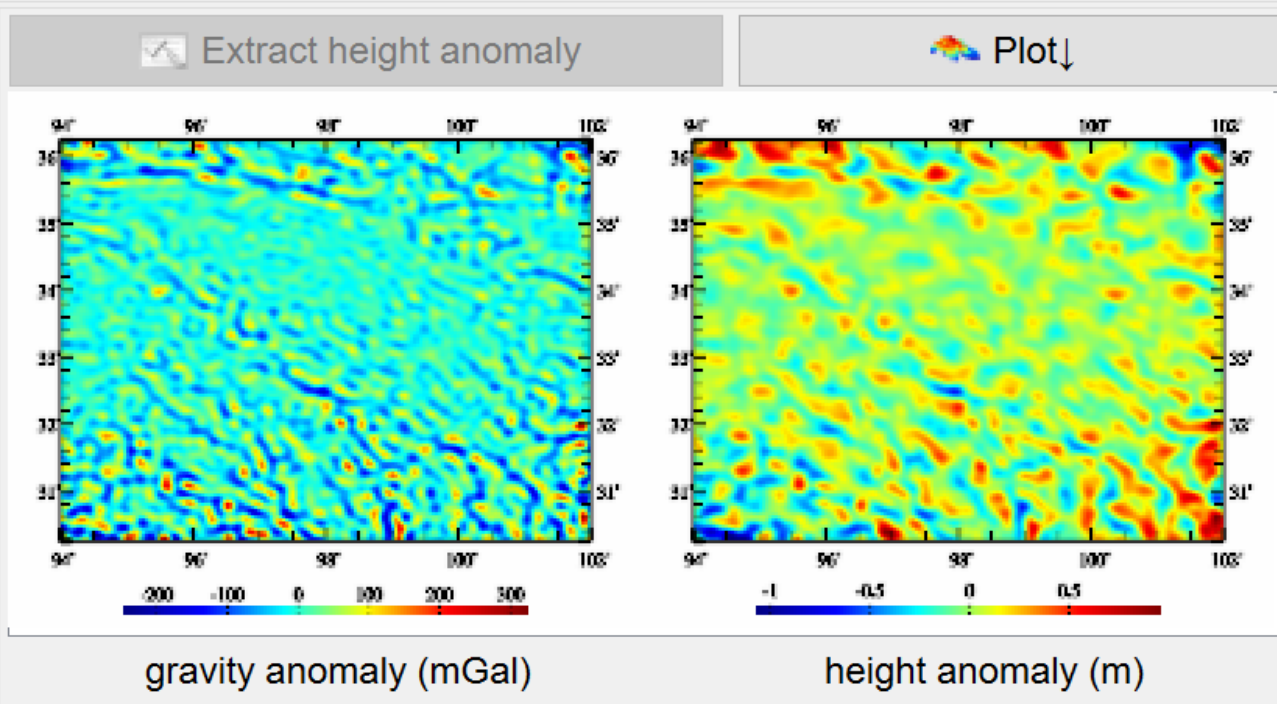
Integral radius 180 km

Save the results as

Import setting parameters

Start Computation

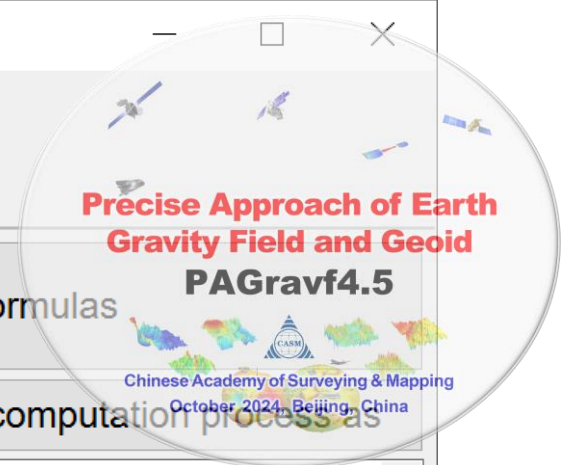
94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0801	-0.0775	-0.0825	-0.0952	-0.1146	-0.1390	-0.1667
-0.3914	-0.4036	-0.4126	-0.4191	-0.4241	-0.4292	-0.4362
-0.7545	-0.7992	-0.8366	-0.8651	-0.8842	-0.8944	-0.8971
-0.8988	-0.8960	-0.8837	-0.8596	-0.8213	-0.7679	-0.7000
0.0897	0.1378	0.1713	0.1904	0.1958	0.1884	0.1697
-0.2694	-0.3182	-0.3601	-0.3932	-0.4158	-0.4257	-0.4217
0.1558	0.2243	0.2769	0.3098	0.3208	0.3092	0.2763
-0.2183	-0.2149	-0.1962	-0.1656	-0.1276	-0.0868	-0.0479
-0.0505	-0.0730	-0.0945	-0.1144	-0.1326	-0.1492	-0.1642
-0.2305	-0.2288	-0.2252	-0.2196	-0.2115	-0.2005	-0.1861
0.0563	0.0686	0.0703	0.0607	0.0397	0.0086	-0.0306
-0.2157	-0.1802	-0.1347	-0.0816	-0.0234	0.0371	0.0978
0.3944	0.3889	0.3769	0.3592	0.3374	0.3126	0.2862
0.0878	0.0701	0.0532	0.0379	0.0251	0.0160	0.0116
0.1639	0.1731	0.1734	0.1640	0.1448	0.1166	0.0807



Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
 The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Stokes integral - FFT

Import parameters Save as Start Computation Save process Follow example



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
1D FFT algorithm

>> Computation Process ** Operation Prompts

```
>> Computation start time: 2024-09-23 11:04:56
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:34:09
>> Compute external residual height anomaly by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/stokesFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:39:25
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:39:27
>> Compute external residual height anomaly by 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/stokesFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:48:22
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 11:48:49
```

Save computation process as

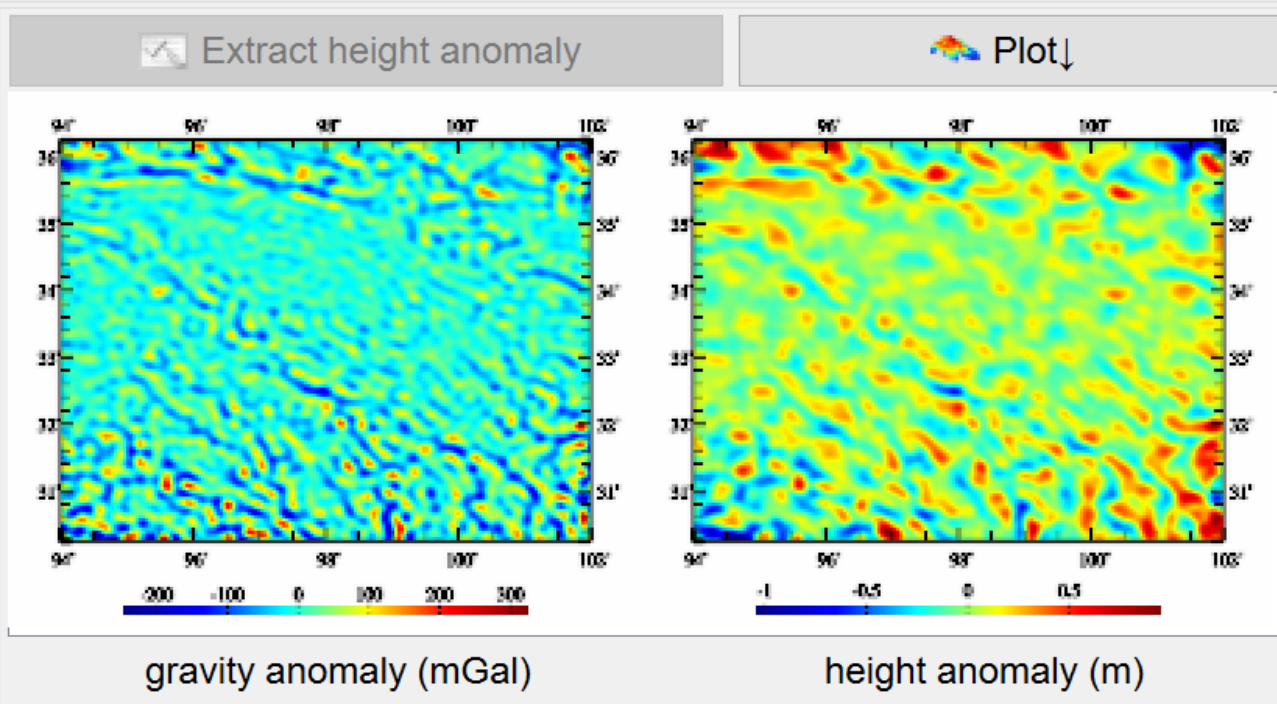
Integral radius 180 km

Save the results as

Import setting parameters

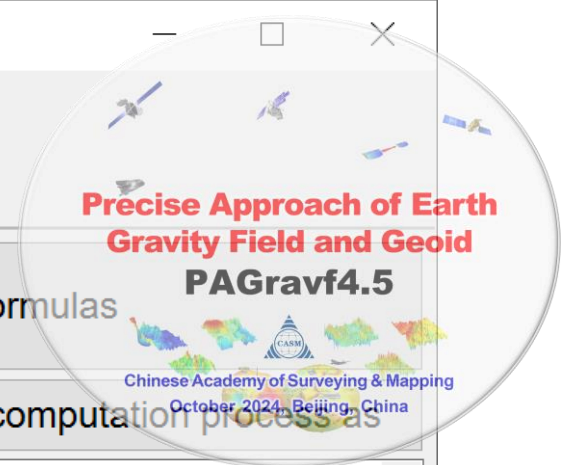
Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0952	-0.0880	-0.0882	-0.0965	-0.1123	-0.1340	-0.1600
-0.3732	-0.3838	-0.3920	-0.3989	-0.4053	-0.4126	-0.4224
-0.7210	-0.7623	-0.7987	-0.8291	-0.8527	-0.8694	-0.8802
-0.8921	-0.8822	-0.8643	-0.8363	-0.7968	-0.7448	-0.6806
0.0945	0.1479	0.1862	0.2089	0.2161	0.2087	0.1878
-0.2825	-0.3320	-0.3751	-0.4100	-0.4351	-0.4483	-0.4479
0.1639	0.2432	0.3053	0.3456	0.3612	0.3510	0.3162
-0.2177	-0.2100	-0.1866	-0.1515	-0.1100	-0.0683	-0.0304
-0.0415	-0.0652	-0.0882	-0.1099	-0.1299	-0.1480	-0.1642
-0.2320	-0.2323	-0.2309	-0.2270	-0.2199	-0.2087	-0.1924
0.0941	0.1026	0.0979	0.0796	0.0488	0.0077	-0.0403
-0.2009	-0.1641	-0.1212	-0.0745	-0.0260	0.0228	0.0710
0.4179	0.4290	0.4295	0.4189	0.3977	0.3672	0.3294
0.0566	0.0509	0.0472	0.0443	0.0414	0.0385	0.0360
0.1418	0.1571	0.1655	0.1650	0.1543	0.1328	0.1010



Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Hotine integral - Numerical



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Save computation process as

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity disturbance grid file on the equipotential surface

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
number of rows of file header: 1
column ordinal number of ellipsoidal height in the record: 4

>> Computation Process ** Operation Prompts

>> Complete the computation of the height anomaly outside the geoid!
 >> Computation end time: 2024-09-23 11:48:49
 >> [Function] From the ellipsoidal height grid of the equipotential surface and residual gravity disturbance (mGal) grid on the surface, compute the external residual height anomaly (m) by the Hotine integral.
 >> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landgeoidhgt.dat.
 >> Open residual gravity anomaly grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/resGMlgeoid541_1800.rga.
 >> Open the calculation point position file C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...
 >> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/rsthtn.txt.
 ** Record format: Behind the source calculation point file record, appends a column of residual height anomaly calculated, keeps 4 significant figures.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-23 11:50:54
 >> Complete the computation of the height anomaly outside the geoid!
 >> Computation end time: 2024-09-23 11:52:32

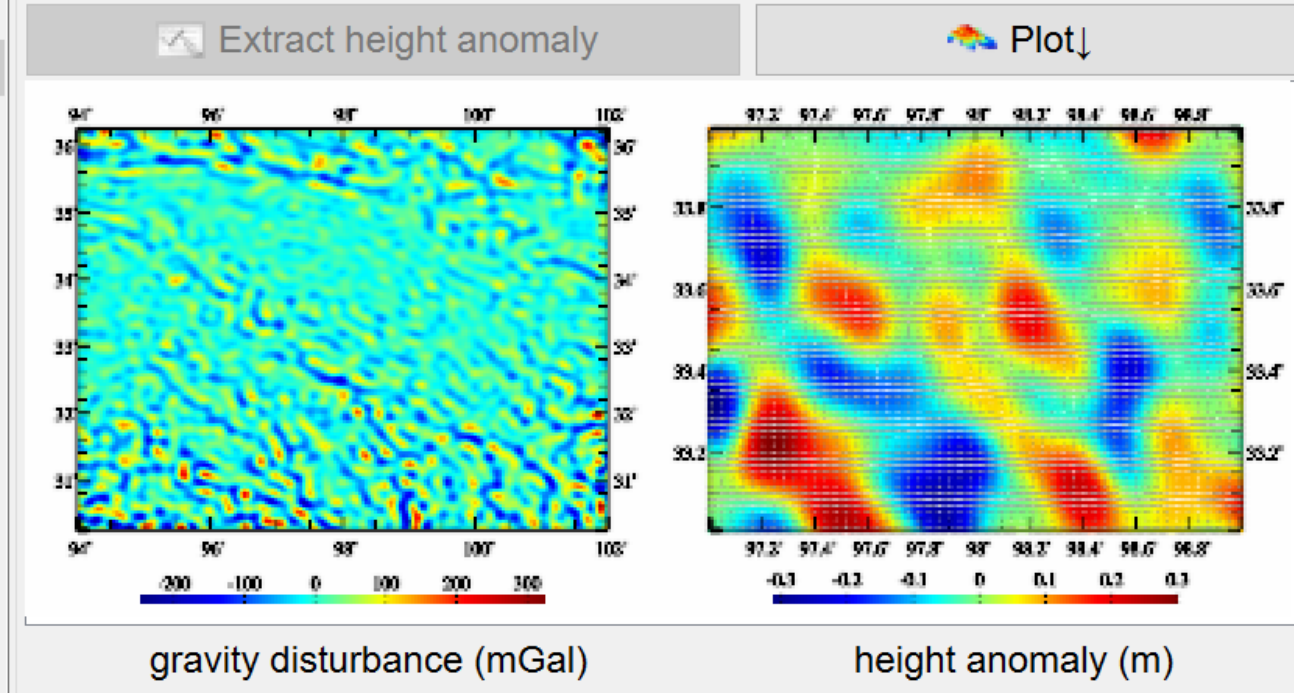
Integral radius: 180 km

Save the results as

Import setting parameters

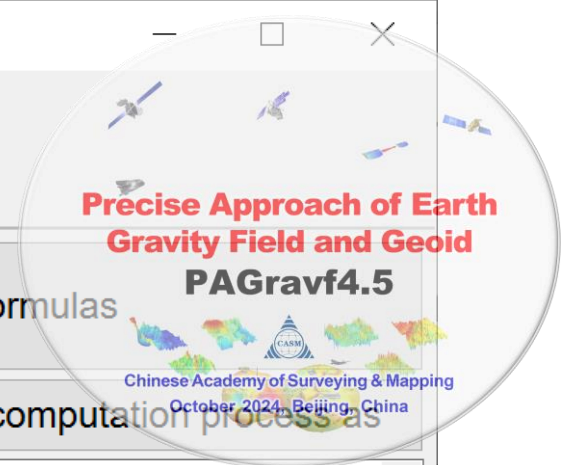
Start Computation

no	lon(degree/decimal)	lat	ellipHeight(m)	
1	97.008333	33.008333	3942.764	-0.0297
2	97.025000	33.008333	3989.787	-0.0343
3	97.041667	33.008333	4034.817	-0.0407
4	97.058333	33.008333	4070.847	-0.0488
5	97.075000	33.008333	4106.877	-0.0585
6	97.091667	33.008333	4119.913	-0.0697
7	97.108333	33.008333	4115.946	-0.0821
8	97.125000	33.008333	4090.977	-0.0955
9	97.141667	33.008333	4070.007	-0.1094
10	97.158333	33.008333	3991.047	-0.1239
11	97.175000	33.008333	3985.070	-0.1366
12	97.191667	33.008333	3956.107	-0.1479
13	97.208333	33.008333	3965.137	-0.1556
14	97.225000	33.008333	3964.173	-0.1596
15	97.241667	33.008333	3983.205	-0.1585
16	97.258333	33.008333	3953.251	-0.1530



- Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Hotine integral - Numerical



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity disturbance grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
numerical integral

>> Computation Process ** Operation Prompts

```
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:48:33
>> [Function] From the ellipsoidal height grid of the equipotential surface and residual gravity disturbance (mGal) grid on the surface, compute the external residual height anomaly (m) by the Hotine integral.
>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landgeoidhgt.dat.
>> Open residual gravity anomaly grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/resGMlgeoid541_1800.rga.
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/landbmsurfhgt.dat.
>> Compute external residual height anomaly by numerical integral...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/Hotinenintg.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 12:50:10
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 13:19:47
```

Integral radius 180 km

Save the results as

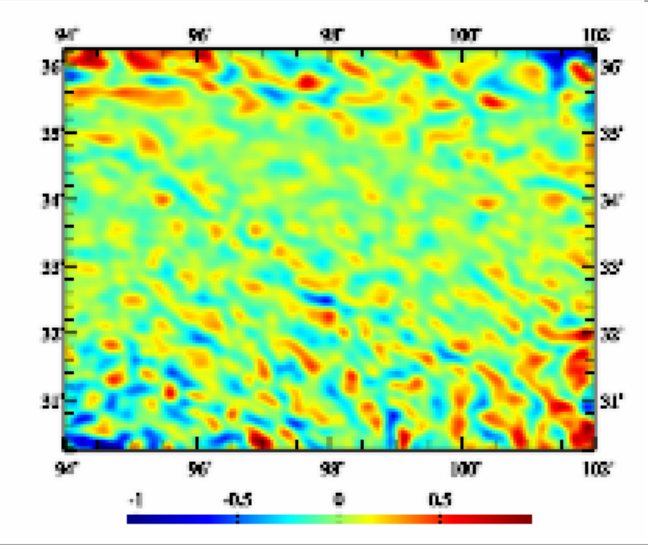
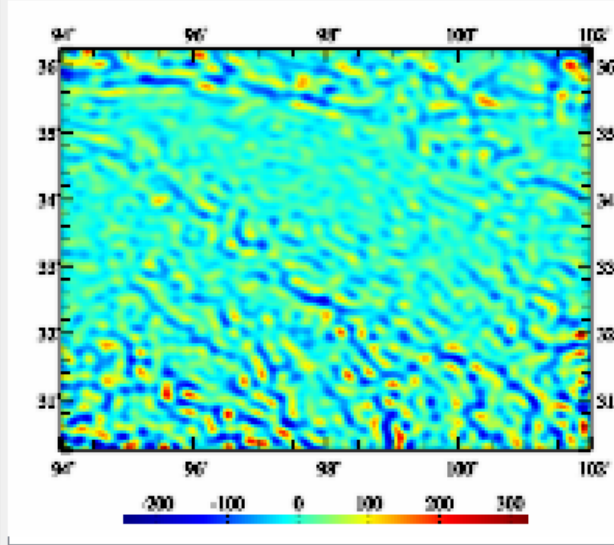
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0989	-0.0921	-0.0932	-0.1028	-0.1189	-0.1402	-0.1647
-0.3701	-0.3801	-0.3875	-0.3936	-0.4000	-0.4074	-0.4172
-0.7283	-0.7650	-0.8039	-0.8374	-0.8647	-0.8950	-0.9061
-1.0144	-1.0271	-1.0295	-1.0043	-0.9551	-0.8952	-0.8112
0.1000	0.1635	0.2067	0.2354	0.2497	0.2420	0.2171
-0.2861	-0.3407	-0.3926	-0.4340	-0.4716	-0.4968	-0.5044
0.1692	0.2423	0.2998	0.3336	0.3421	0.3357	0.3034
-0.2591	-0.2456	-0.2125	-0.1676	-0.1160	-0.0693	-0.0300
-0.0423	-0.0656	-0.0882	-0.1096	-0.1295	-0.1471	-0.1633
-0.2300	-0.2304	-0.2294	-0.2259	-0.2194	-0.2091	-0.1948
0.0853	0.0930	0.0874	0.0705	0.0420	0.0043	-0.0411
-0.2276	-0.1867	-0.1405	-0.0916	-0.0404	0.0083	0.0538
0.4131	0.4260	0.4283	0.4204	0.4008	0.3708	0.3325
0.0593	0.0540	0.0503	0.0472	0.0438	0.0402	0.0364
0.1406	0.1545	0.1605	0.1585	0.1471	0.1262	0.0960

Extract height anomaly

Plot



gravity disturbance (mGal)

height anomaly (m)

- Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Hotine integral - FFT

Import parameters Save as Start Computation Save process Follow example



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity disturbance grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
2D FFT algorithm

>> Computation Process ** Operation Prompts

```

resGMlgeoid541_1800.rga.
>> Compute external residual height anomaly by numerical integral...
>> Save the results as C:/PAGrav4.5_win64en/examples/IntgenStokesHotine/Hotinenintg.dat.
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGrav4.5_win64en/examples/IntgenStokesHotine/landbmsurfhgt.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 11:54:42
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:24:27
>> Compute external residual height anomaly by 2D FFT algorithm...
>> Save the results as C:/PAGrav4.5_win64en/examples/IntgenStokesHotine/HotineFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 12:45:58
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:45:59
    
```

Save computation process as

Integral radius 180 km

Save the results as

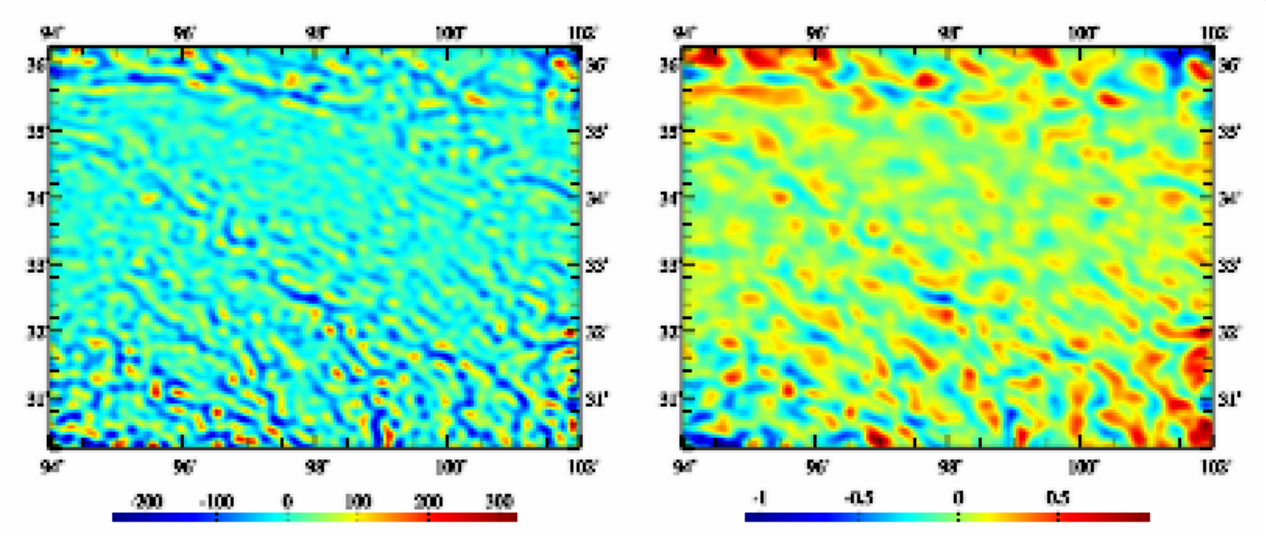
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0804	-0.0778	-0.0828	-0.0956	-0.1150	-0.1395	-0.1672
-0.3925	-0.4048	-0.4138	-0.4203	-0.4253	-0.4304	-0.4375
-0.7564	-0.8011	-0.8386	-0.8672	-0.8863	-0.8965	-0.8993
-0.9010	-0.8982	-0.8859	-0.8617	-0.8233	-0.7698	-0.7018
0.0895	0.1377	0.1713	0.1905	0.1959	0.1886	0.1698
-0.2700	-0.3189	-0.3609	-0.3941	-0.4166	-0.4267	-0.4226
0.1560	0.2246	0.2772	0.3102	0.3212	0.3097	0.2768
-0.2186	-0.2152	-0.1965	-0.1658	-0.1278	-0.0870	-0.0480
-0.0506	-0.0732	-0.0948	-0.1147	-0.1330	-0.1496	-0.1646
-0.2312	-0.2296	-0.2260	-0.2203	-0.2122	-0.2013	-0.1869
0.0560	0.0683	0.0701	0.0604	0.0395	0.0083	-0.0309
-0.2158	-0.1803	-0.1347	-0.0814	-0.0231	0.0376	0.0984
0.3955	0.3901	0.3780	0.3603	0.3384	0.3135	0.2871
0.0882	0.0704	0.0535	0.0382	0.0254	0.0163	0.0120
0.1644	0.1736	0.1739	0.1645	0.1453	0.1170	0.0811

Extract height anomaly

Plot



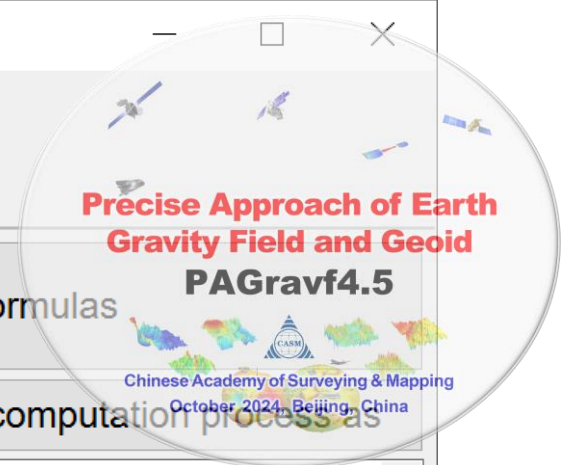
gravity disturbance (mGal)

height anomaly (m)

- Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

External height anomaly computation using generalized Hotine integral - FFT

Import parameters Save as Start Computation Save process Follow example



External height anomaly computation using generalized Stokes integral

External height anomaly computation using generalized Hotine integral

Stokes and Hotine integral formulas

Save computation process as

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity disturbance grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
1D FFT algorithm

>> Computation Process ** Operation Prompts

```
>> Computation start time: 2024-09-23 11:54:42
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:24:27
>> Compute external residual height anomaly by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/HotineFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 12:45:58
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:45:59
>> Compute external residual height anomaly by 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenStokesHotine/HotineFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 12:48:07
>> Complete the computation of the height anomaly outside the geoid!
>> Computation end time: 2024-09-23 12:48:33
```

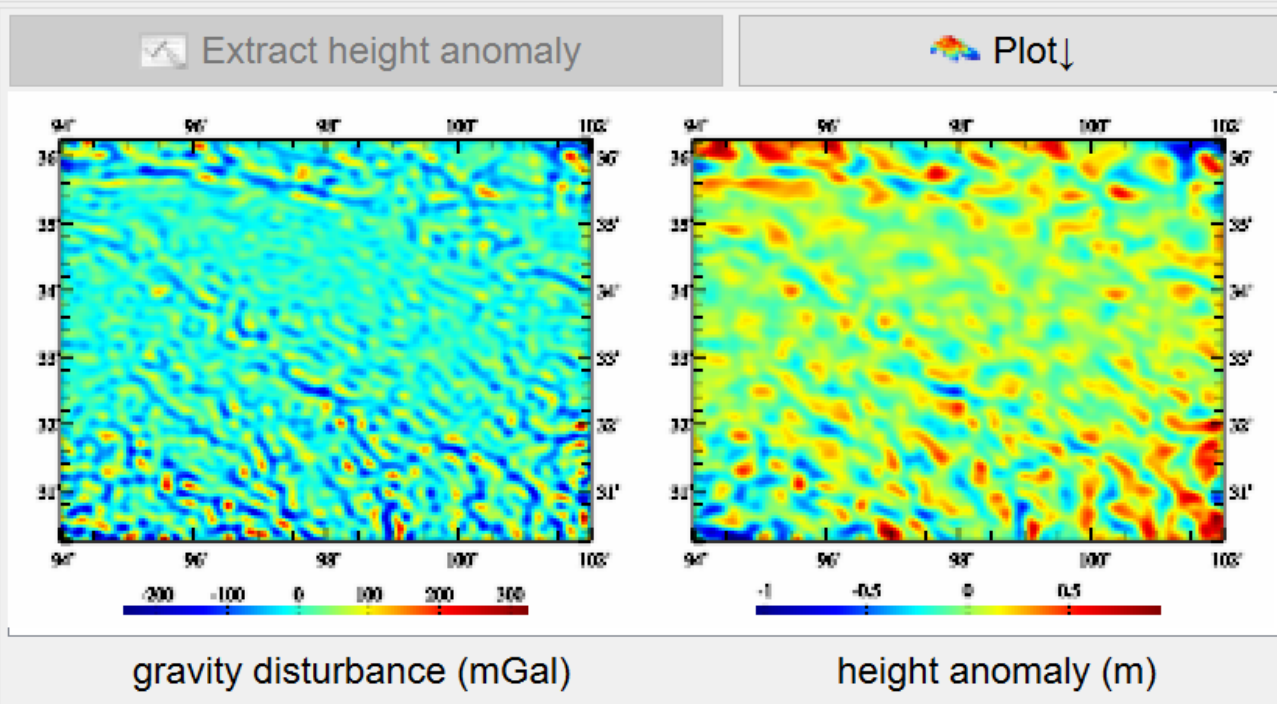
Integral radius 180 km

Save the results as

Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667	
-0.0955	-0.0883	-0.0885	-0.0969	-0.1127	-0.1345	-0.1605
-0.3743	-0.3849	-0.3932	-0.4000	-0.4065	-0.4139	-0.4236
-0.7228	-0.7642	-0.8007	-0.8311	-0.8547	-0.8715	-0.8824
-0.8943	-0.8844	-0.8664	-0.8384	-0.7988	-0.7467	-0.6824
0.0943	0.1478	0.1862	0.2091	0.2163	0.2088	0.1880
-0.2832	-0.3327	-0.3759	-0.4109	-0.4360	-0.4493	-0.4489
0.1640	0.2435	0.3057	0.3460	0.3617	0.3515	0.3167
-0.2180	-0.2103	-0.1868	-0.1517	-0.1102	-0.0684	-0.0304
-0.0416	-0.0654	-0.0884	-0.1102	-0.1302	-0.1483	-0.1646
-0.2327	-0.2331	-0.2316	-0.2278	-0.2207	-0.2095	-0.1932
0.0938	0.1024	0.0977	0.0794	0.0485	0.0074	-0.0406
-0.2011	-0.1642	-0.1211	-0.0743	-0.0257	0.0232	0.0716
0.4191	0.4302	0.4307	0.4201	0.3988	0.3682	0.3303
0.0570	0.0513	0.0475	0.0446	0.0418	0.0388	0.0363
0.1424	0.1576	0.1660	0.1655	0.1547	0.1332	0.1013



Stokes boundary value theory requires that the boundary surface should be an equipotential surface, that is, the gravity anomaly/disturbance should be on the equipotential surface.
The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external vertical deflection from gravity anomaly – Numerical integral



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid PAggrav4.5

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
number of rows of file header: 1
column ordinal number of ellipsoidal height in the record: 4

Integral radius: 180 km

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential surface and residual gravity anomaly (mGal) grid on the surface, compute the external residual vertical deflection (", SW, to south, to west) by the generalized Vening-Meinesz integral.

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/landgeoidht.dat.

>> Open residual gravity anomaly grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/resGMLgeoid541_1800.gra.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/rstgra.txt.

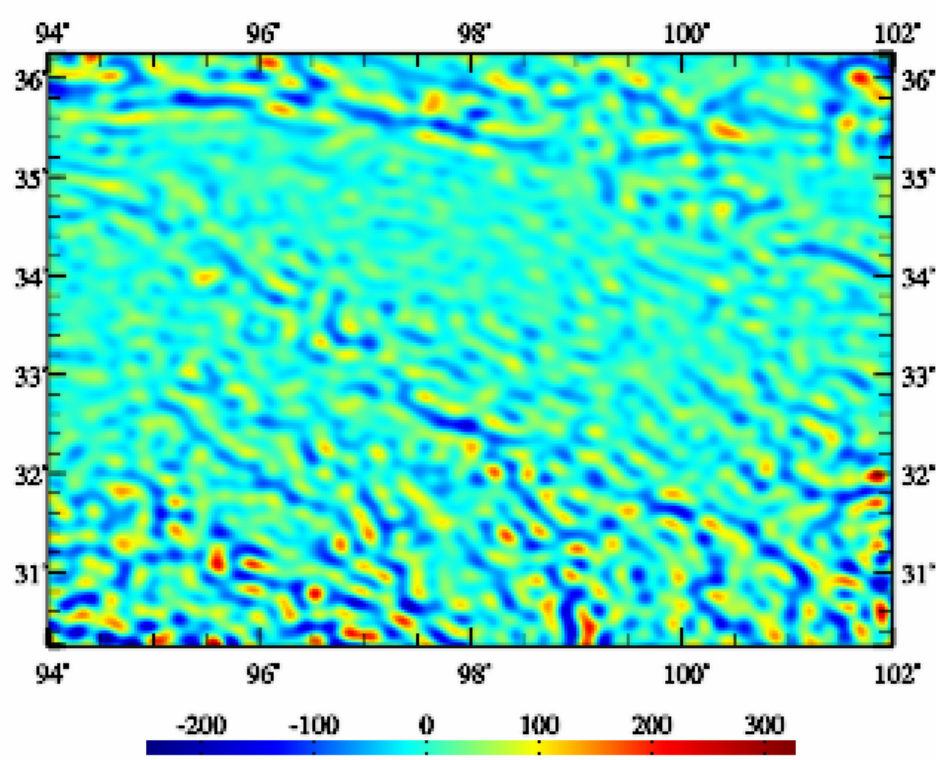
** Record format: Behind the source calculation point file record, appends two columns of residual vertical deflection southward and westward calculated, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

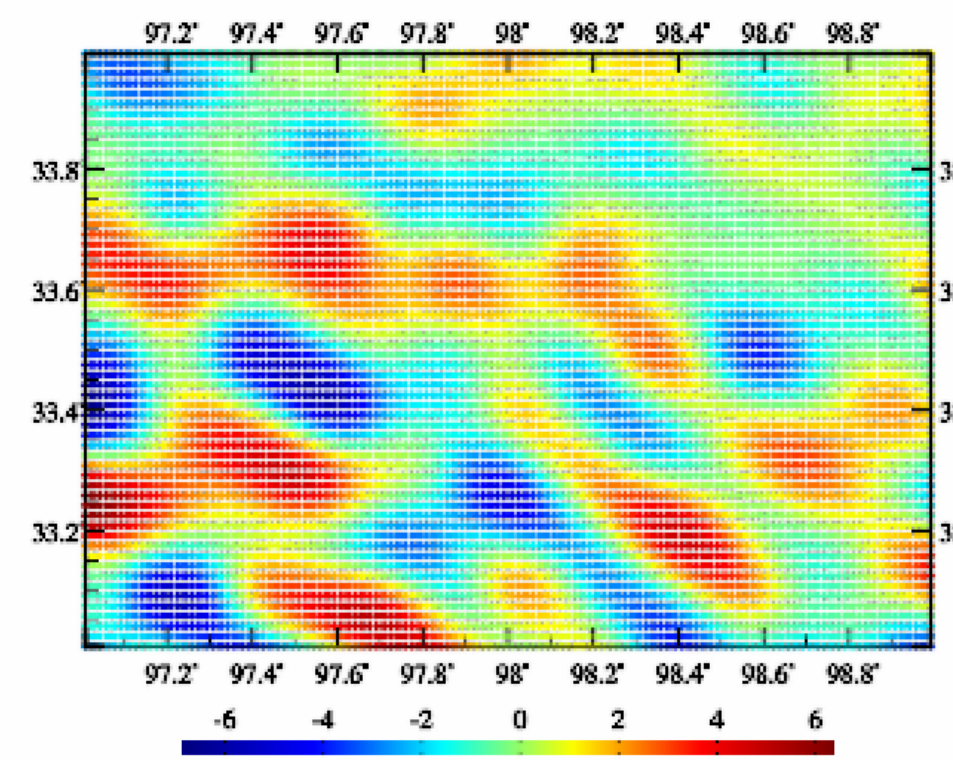
Save the results as Import setting parameters Start Computation

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-2.4975	0.4726
2	97.025000	33.008333	3989.787	-2.4200	0.6841
3	97.041667	33.008333	4034.817	-2.3012	0.9131
4	97.058333	33.008333	4070.847	-2.1495	1.1375
5	97.075000	33.008333	4106.877	-1.9758	1.3348

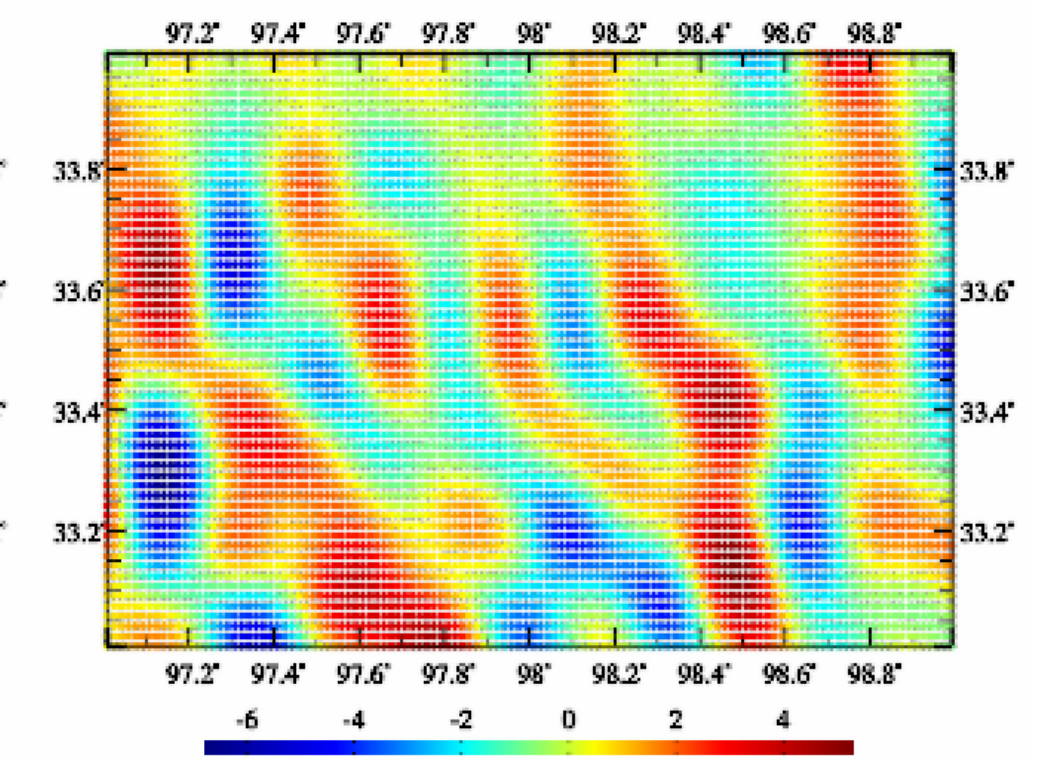
Extract vertical deflection Plot↓



gravity anomaly (mGal)



vertical deflection (", S)

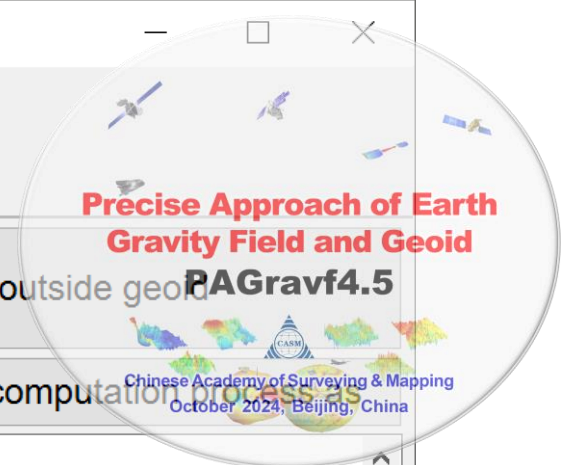


vertical deflection (", W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity anomaly – Numerical integral

Save as Import parameters Start Computation Save process Follow example



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface
 Open the residual gravity anomaly grid file on the equipotential surface

>> Computation Process ** Operation Prompts

```
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/gratovmnintg.dat.
>> The input and output files are not enough, please confirm!
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/landbmsurfhgt.dat.
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/gratovmnintg.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 14:08:57
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 14:48:53
```

Select calculation point file format
 ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

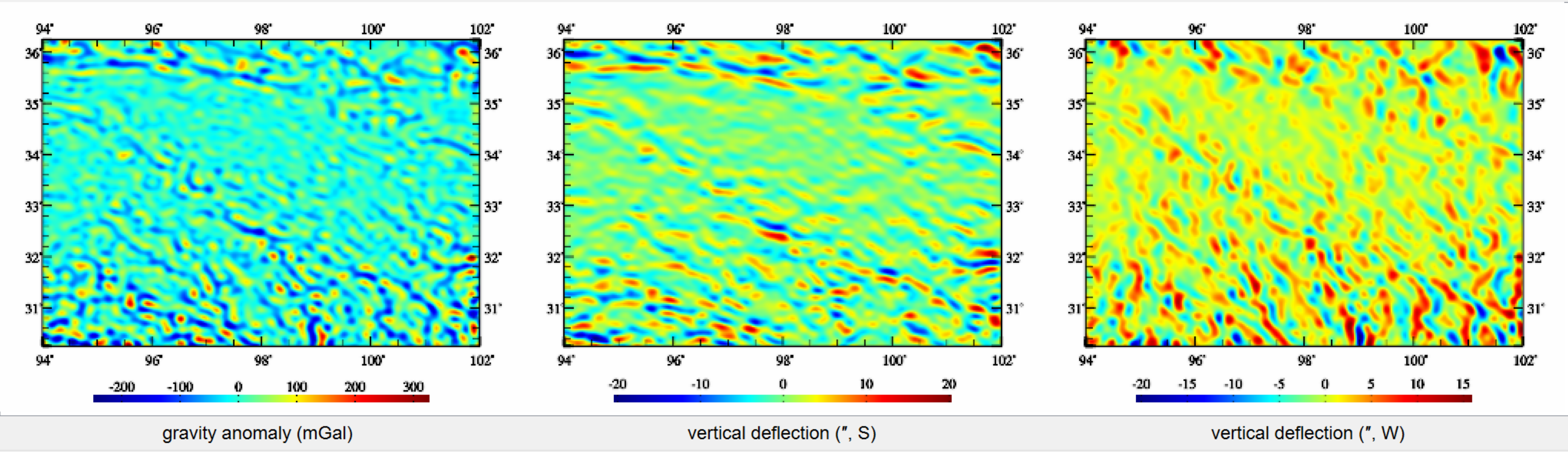
Select integral algorithm
 numerical integral

Integral radius 180 km

Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667				
-1.9493	-2.1696	-2.0858	-1.7165	-1.1882	-0.5582	0.1046	0.7554	1.4415	
4.3770	4.3096	4.0973	3.7678	3.3903	3.0314	2.7435	2.5574	2.5645	
8.0786	8.6212	9.2862	9.7457	9.9825	10.4228	10.1087	9.6478	9.2844	
12.3971	13.3915	14.1847	14.0751	13.2184	12.1703	10.3925	7.8678	5.3064	

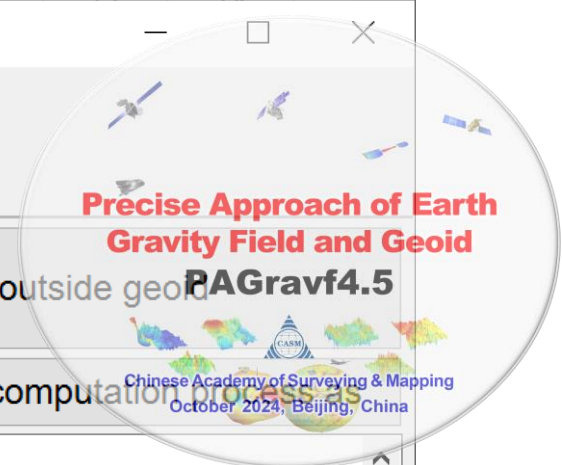
Extract vertical deflection Plot



The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity anomaly – FFT integral

Save as Import parameters Start Computation Save process Follow example



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface
 Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
 ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
 2D FFT algorithm

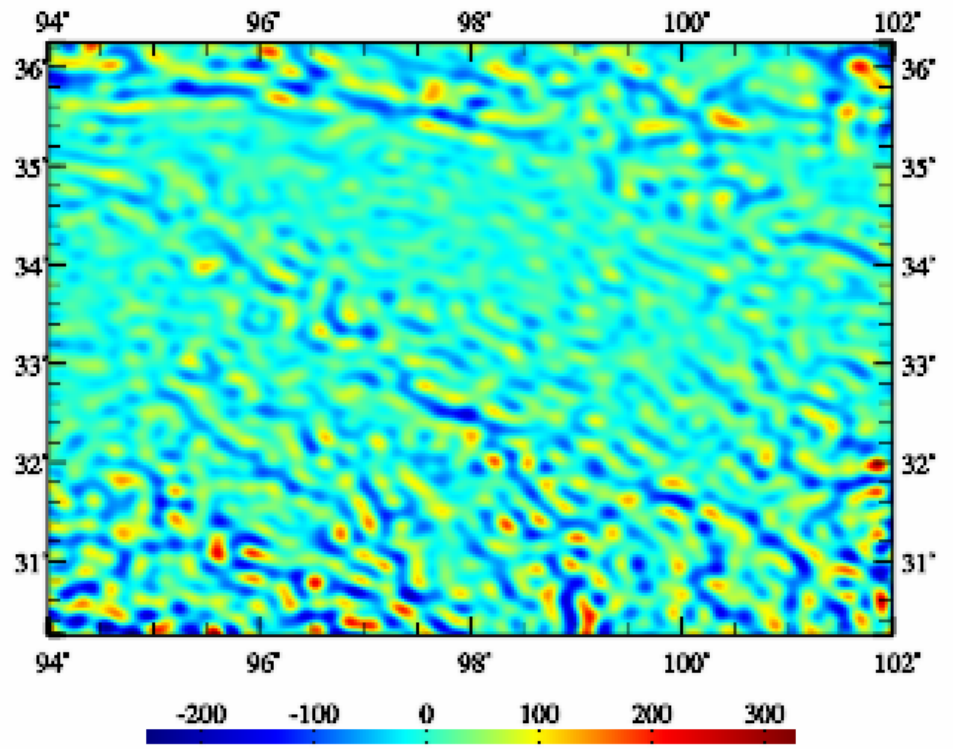
Integral radius 180 km

```
>> Computation Process ** Operation Prompts
>> Computation start time: 2024-09-23 14:08:57
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 14:48:53
>> Compute external residual vertical deflection by 2D FFT algorithm...
>> Save the results as C:/PAGrav4.5_win64en/examples/IntgenVeningMeinesz/gratovmFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 14:55:58
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 14:56:00
```

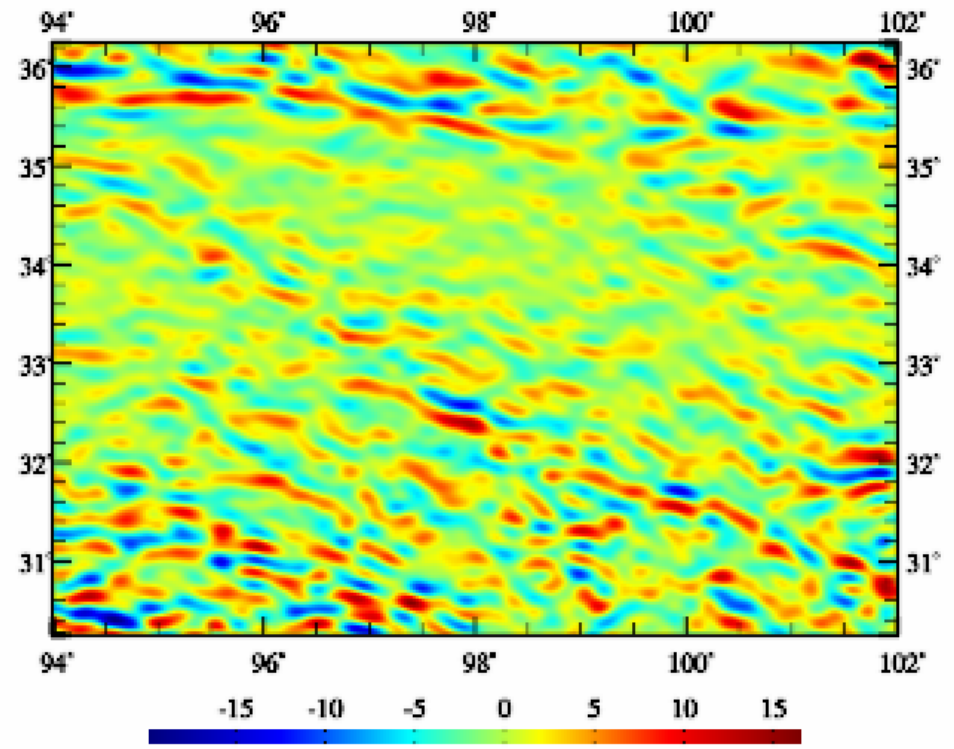
Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667				
-2.2955	-2.5663	-2.5312	-2.2038	-1.6530	-0.9588	-0.1916	0.5943	1.3597	
4.4045	4.3352	4.1336	3.8281	3.4637	3.0993	2.8020	2.6392	2.6689	
8.1418	8.9666	9.5719	9.9219	10.0144	9.8802	9.5792	9.1888	8.7932	
9.2908	9.5062	9.5374	9.3162	8.7965	7.9607	6.8206	5.4140	3.7999	

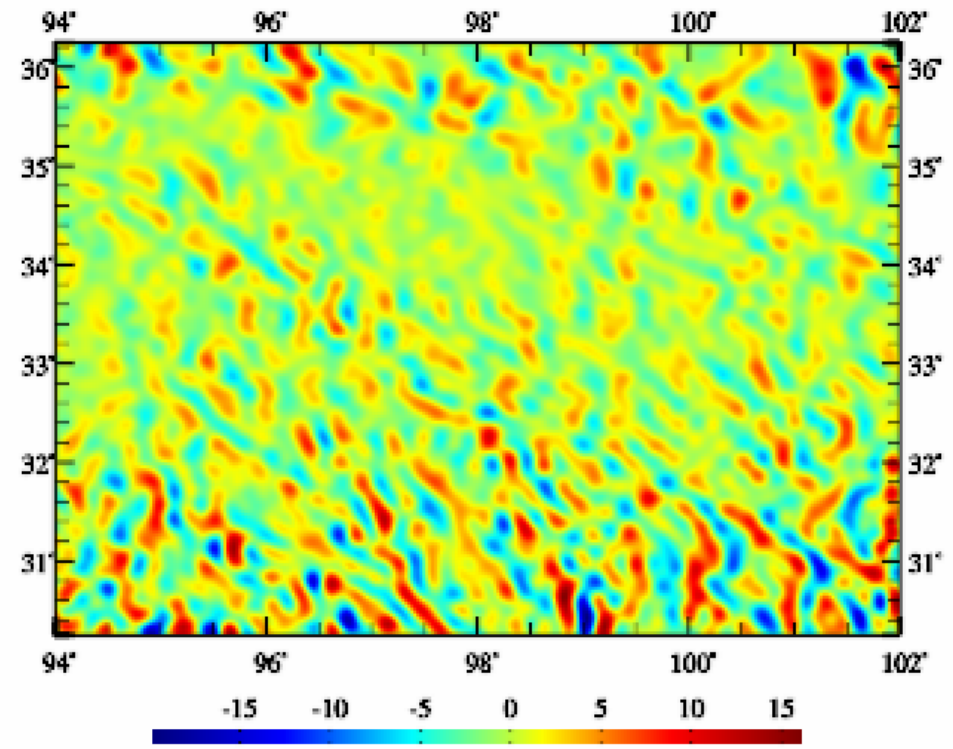
Extract vertical deflection Plot



gravity anomaly (mGal)



vertical deflection (", S)

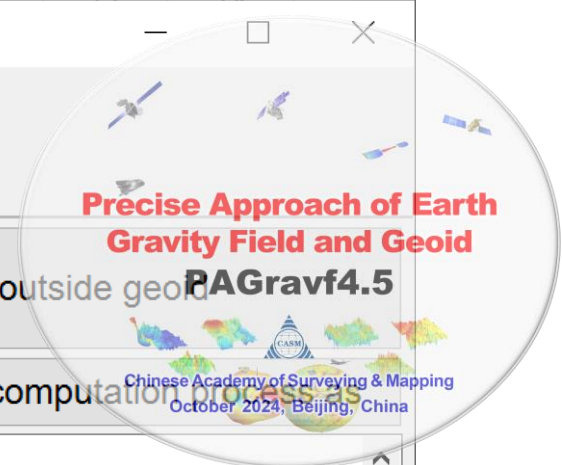


vertical deflection (", W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity anomaly – FFT integral

Save as Import parameters Start Computation Save process Follow example



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface
 Open the residual gravity anomaly grid file on the equipotential surface

Select calculation point file format
 ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

Select integral algorithm
 1D FFT algorithm

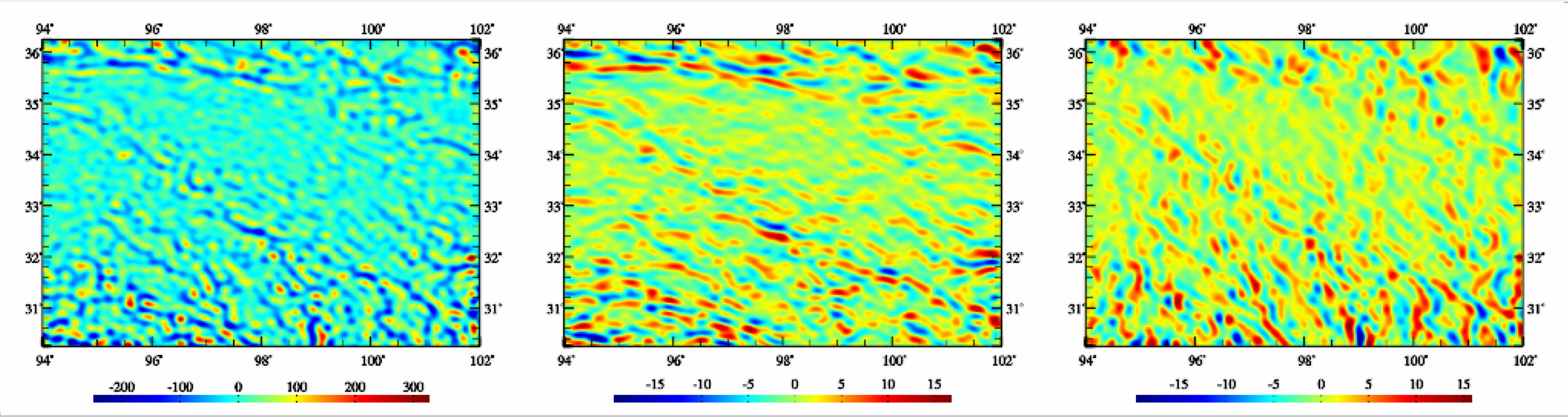
Integral radius 180 km

```
>> Computation Process ** Operation Prompts
>> Computation start time: 2024-09-23 14:55:58
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 14:56:00
>> Compute external residual vertical deflection by 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/gratovmFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 14:56:46
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 14:57:29
```

Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667				
-2.2866	-2.5693	-2.5365	-2.2060	-1.6513	-0.9553	-0.1892	0.5928	1.3523	
4.3578	4.2812	4.0701	3.7522	3.3727	2.9908	2.6747	2.4928	2.5043	
7.9132	8.7324	9.3302	9.6709	9.7517	9.6042	9.2891	8.8855	8.4788	
9.0235	9.2631	9.3211	9.1282	8.6380	7.8323	6.7225	5.3462	3.7619	

Extract vertical deflection Plot



gravity anomaly (mGal)

vertical deflection (", S)

vertical deflection (", W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity disturbance – Numerical integral



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface

Open the residual gravity disturbance grid file on the equipotential surface

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
number of rows of file header: 1
column ordinal number of ellipsoidal height in the record: 4

Integral radius: 180 km

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential surface and residual gravity disturbance (mGal) grid on the surface, compute the external residual vertical deflection (", SW, to south, to west) by the generalized Vening-Meinesz integral.

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/landgeoidht.dat.

>> Open residual gravity disturbance grid file on equipotential surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/resGMLgeoid541_1800.rga.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/rstrga.txt.

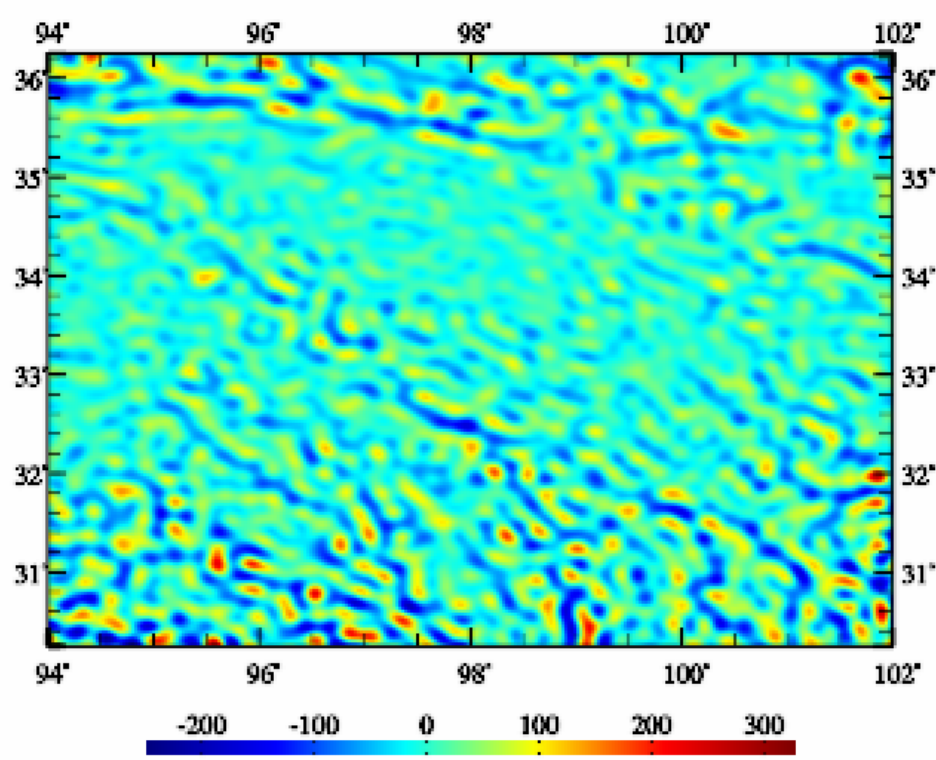
** Record format: Behind the source calculation point file record, appends two columns of residual vertical deflection southward and westward calculated, keeps 4 significant figures.

>> The parameter settings have been entered into the system!

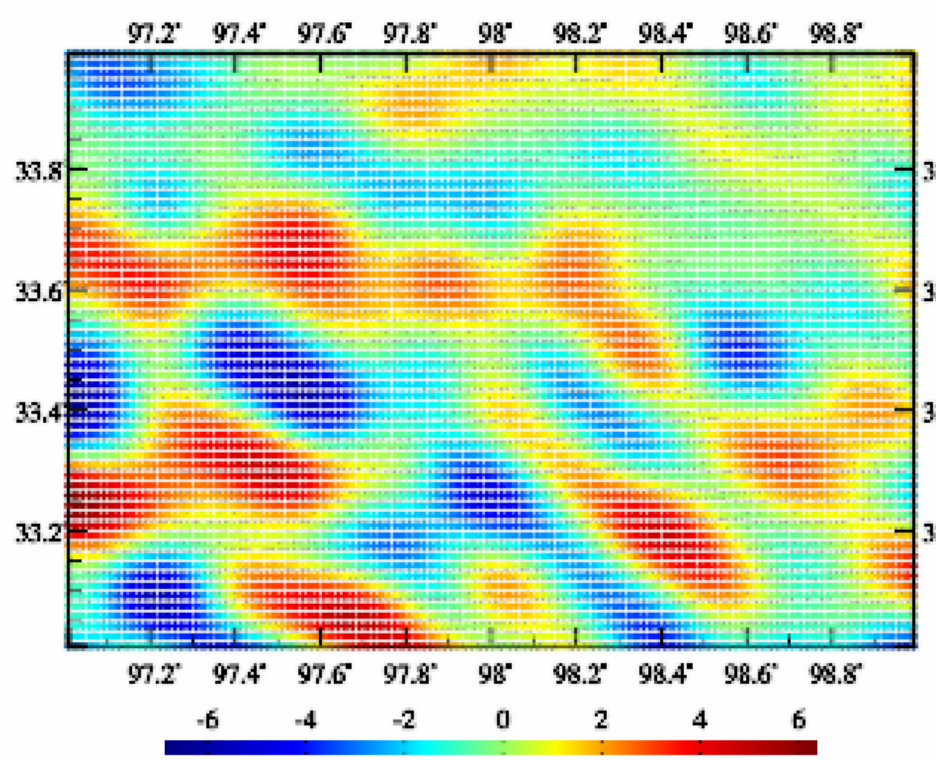
Save the results as Import setting parameters Start Computation

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-2.4923	0.4718
2	97.025000	33.008333	3989.787	-2.4149	0.6833
3	97.041667	33.008333	4034.817	-2.2964	0.9122
4	97.058333	33.008333	4070.847	-2.1450	1.1367
5	97.075000	33.008333	4106.877	-1.9717	1.3340

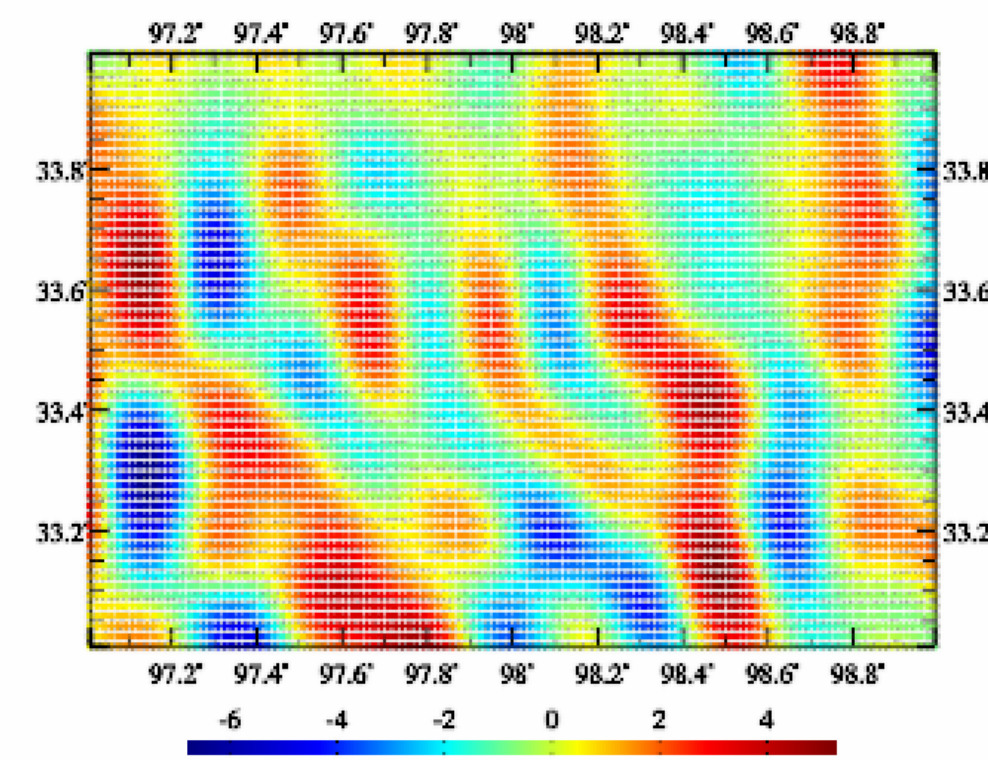
Extract vertical deflection Plot↓



gravity disturbance (mGal)



vertical deflection (", S)

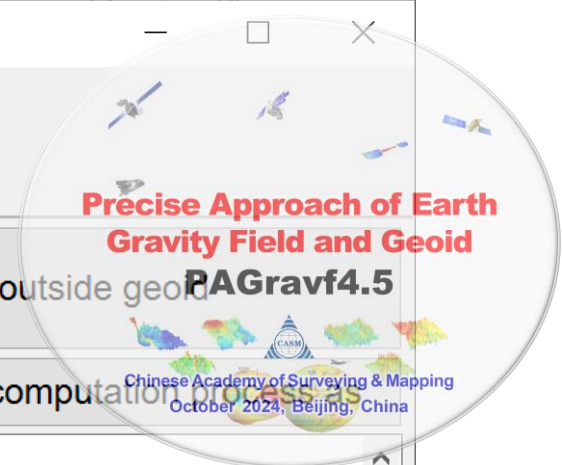


vertical deflection (", W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity disturbance – FFT integral

Save as Import parameters Start Computation Save process Follow example



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface
 Open the residual gravity disturbance grid file on the equipotential surface

>> Computation Process ** Operation Prompts

```
>> Computation end time: 2024-09-23 15:01:01
>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/landbmsurfhgt.dat.
>> Compute external residual vertical deflection by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/IntgenVeningMeinesz/rgatovmFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 15:03:49
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 15:03:51
```

Select calculation point file format
 ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

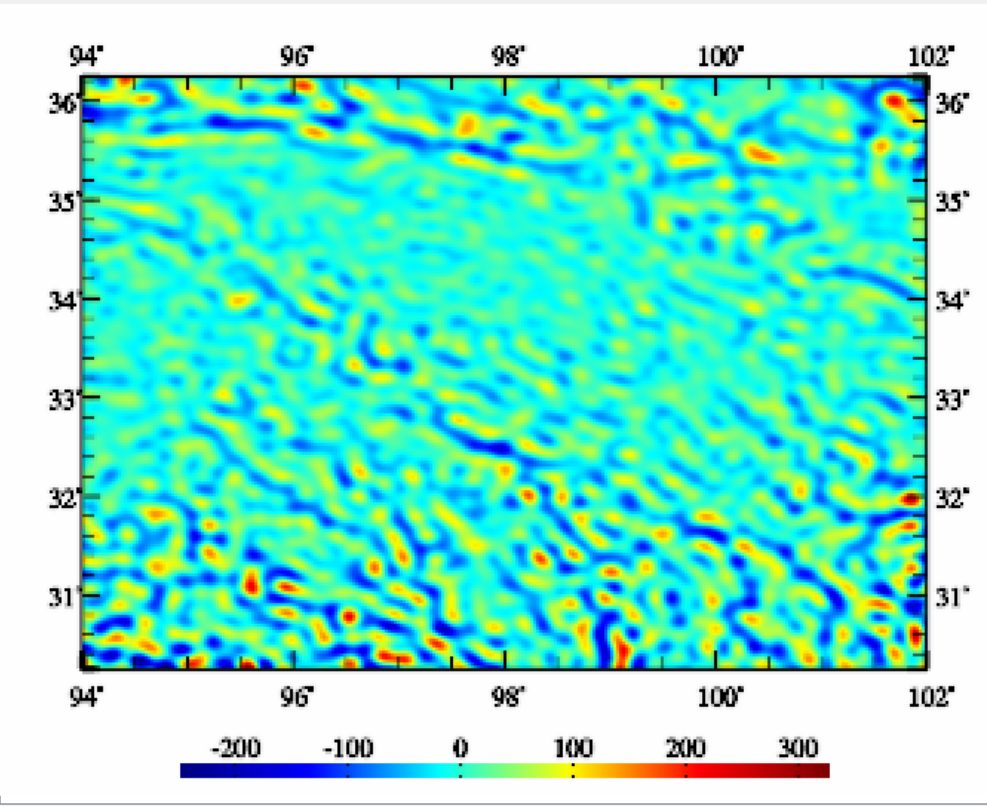
Select integral algorithm
 2D FFT algorithm

Integral radius 180 km

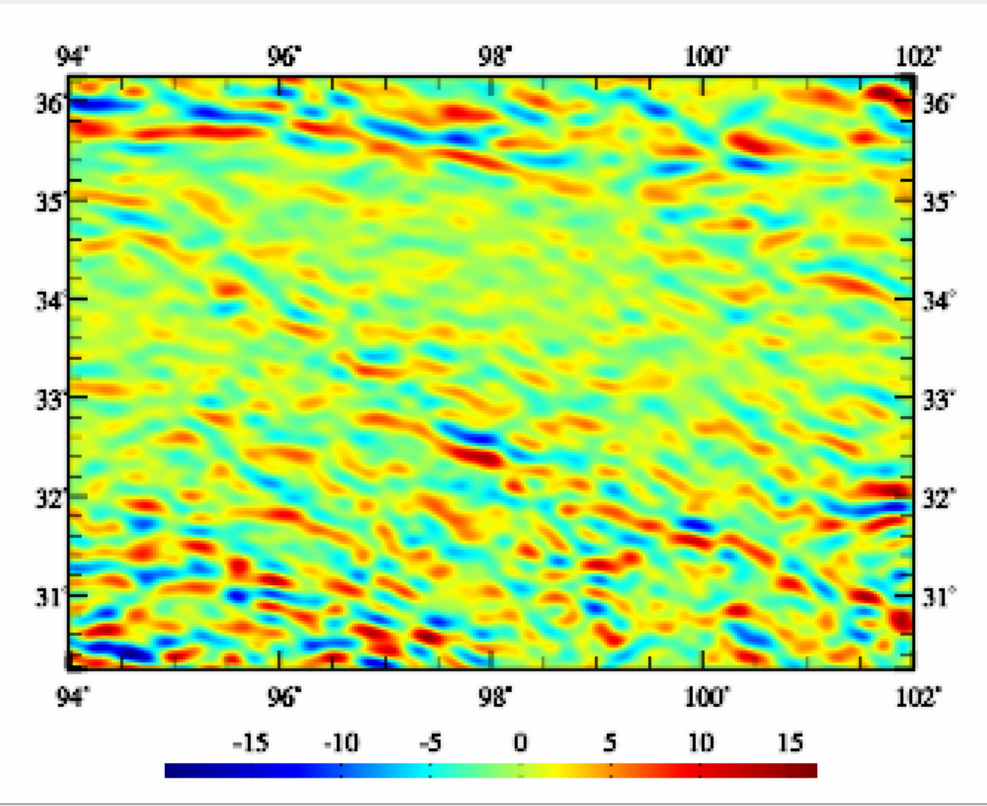
Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667				
-2.2983	-2.5692	-2.5347	-2.2082	-1.6585	-0.9656	-0.1997	0.5849	1.3491	
4.3900	4.3211	4.1201	3.8155	3.4521	3.0887	2.7923	2.6303	2.6604	
8.1264	8.9502	9.5548	9.9047	9.9975	9.8642	9.5643	9.1752	8.7810	
9.2803	9.4953	9.5263	9.3052	8.7862	7.9515	6.8129	5.4083	3.7964	

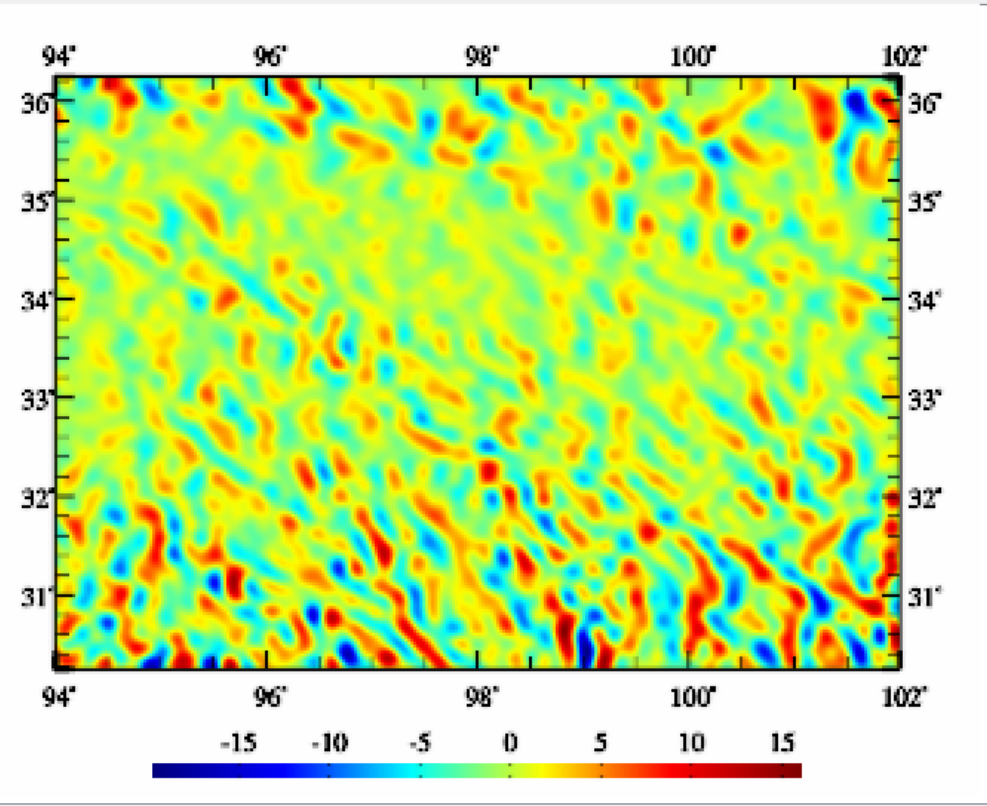
Extract vertical deflection Plot



gravity disturbance (mGal)



vertical deflection (" , S)

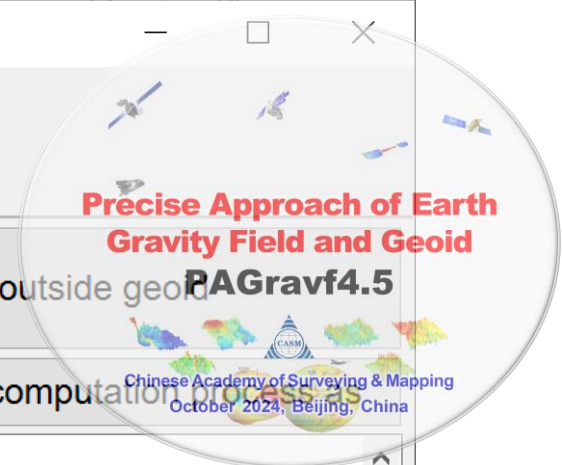


vertical deflection (" , W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of external vertical deflection from gravity disturbance – FFT integral

Save as Import parameters Start Computation Save process Follow example



Computation of external vertical deflection from gravity anomaly

Computation of external vertical deflection from gravity disturbance

Vening-Meinesz integral formulas outside geoid

Open the ellipsoidal height grid file of the equipotential surface
 Open the residual gravity disturbance grid file on the equipotential surface

>> Computation Process ** Operation Prompts

```
>> Computation start time: 2024-09-23 15:03:49
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 15:03:51
>> Compute external residual vertical deflection by 1D FFT algorithm...
>> Save the results as C:/PAGrav4.5_win64en/examples/IntgenVeningMeinesz/rgatovmFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 15:04:25
>> Complete the computation of the vertical deflection outside the geoid!
>> Computation end time: 2024-09-23 15:05:09
```

Select calculation point file format
 ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

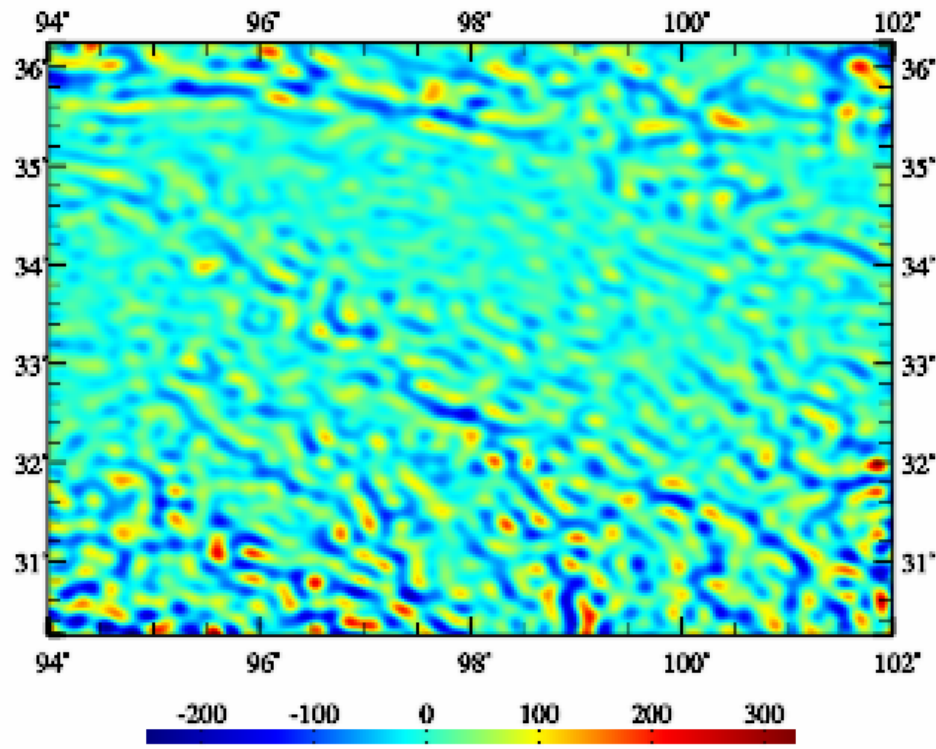
Select integral algorithm
 1D FFT algorithm

Integral radius 180 km

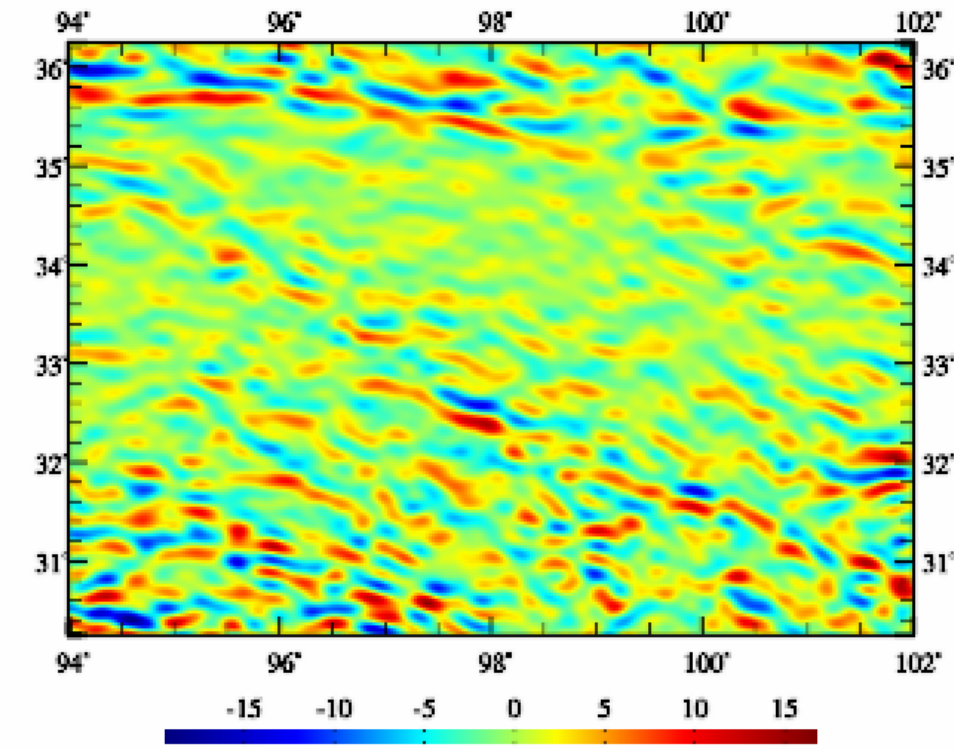
Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667				
-2.2902	-2.5728	-2.5404	-2.2106	-1.6569	-0.9620	-0.1970	0.5837	1.3422	
4.3438	4.2677	4.0572	3.7402	3.3616	2.9808	2.6656	2.4845	2.4963	
7.8987	8.7168	9.3140	9.6544	9.7356	9.5887	9.2746	8.8722	8.4667	
9.0128	9.2522	9.3100	9.1173	8.6277	7.8231	6.7148	5.3404	3.7583	

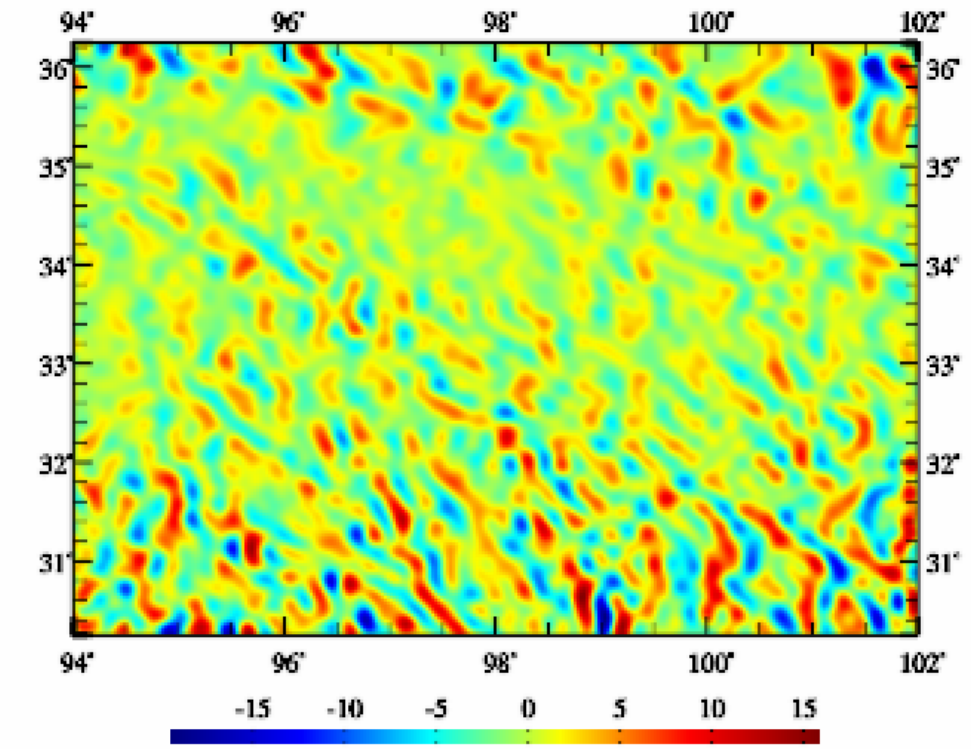
Extract vertical deflection Plot



gravity disturbance (mGal)



vertical deflection (" , S)



vertical deflection (" , W)

The generalized Vening-Meinesz formula is derived from the generalized Stokes/Hotine formula and belongs to the solution of the Stokes boundary value problem. Which requires the integrand gravity anomaly/disturbance to be on the equipotential surface.

Computation of gravity anomaly by the inverse Stokes integral – Numerical

Save as Import parameters Start Computation Save process Follow example

- Computation of gravity anomaly by the inverse Stokes integral
- Computation of gravity disturbance by the inverse Hotine integral
- Computation of the inverse Vening Meinesz integral
- Computation of anomalous field elements from height anomaly
- Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the height anomaly grid file on the equipotential surface

Select calculation point file format

discrete calculation point file

Open the calculation point file on the equipotential surface

Set input point file format

number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential boundary surface and residual height anomaly (m) grid on the surface, compute the residual gravity anomaly (mGal) on the equipotential surface by the inverse Stokes integral.

** Input the ellipsoidal height grid file of the equipotential surface and height anomaly grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/landgeoidhgt.dat.

>> Open the height anomaly grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/resGMIgeoid541_1800.ksi.

>> Open the calculation point file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstk.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual gravity anomaly.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 15:16:35

>> Complete the computation!

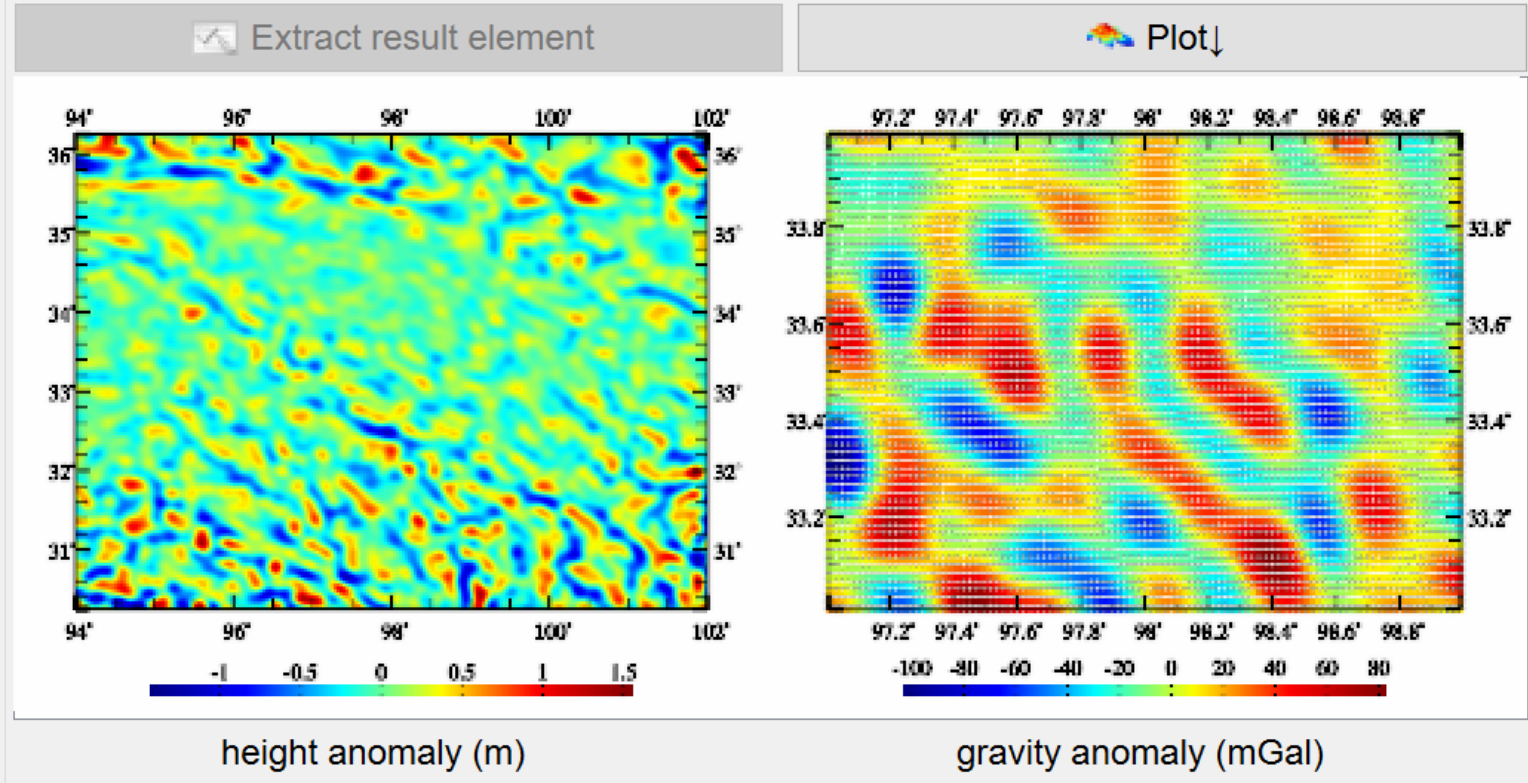
>> Computation end time: 2024-09-23 15:17:40

Integral radius 150 km

Save the results as Import setting parameters Start Computation

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-37.2501	24.7224
2	97.025000	33.008333	3989.787	-37.2203	24.6842
3	97.041667	33.008333	4034.817	-37.1899	22.9058
4	97.058333	33.008333	4070.847	-37.1590	19.2598
5	97.075000	33.008333	4106.877	-37.1276	13.9076
6	97.091667	33.008333	4119.913	-37.0959	7.1243
7	97.108333	33.008333	4115.946	-37.0640	-0.9416
8	97.125000	33.008333	4090.977	-37.0318	-9.7023
9	97.141667	33.008333	4070.007	-36.9990	-18.9075
10	97.158333	33.008333	3991.047	-36.9665	-27.8771
11	97.175000	33.008333	3985.070	-36.9327	-36.2732
12	97.191667	33.008333	3956.107	-36.8988	-43.4193
13	97.208333	33.008333	3965.137	-36.8642	-49.0686
14	97.225000	33.008333	3964.173	-36.8295	-52.4761
15	97.241667	33.008333	3983.205	-36.7943	-53.5072
16	97.258333	33.008333	3953.251	-36.7595	-51.6556
17	97.275000	33.008333	4016.279	-36.7238	-46.8428
18	97.291667	33.008333	4054.318	-36.6883	-39.1123
19	97.308333	33.008333	4090.360	-36.6528	-28.6690

Ignore the ellipsoidal height



- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity anomaly by the inverse Stokes integral – Numerical

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

- Open the ellipsoidal height grid file of the equipotential surface
- Open the height anomaly grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Select integral algorithm
numerical integral

>> Computation Process ** Operation Prompts

```

** Look at the file information in the window below, set the input file format parameters...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstk.txt.
>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual gravity anomaly.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 19:59:17
>> Complete the computation!
>> Computation end time: 2024-09-23 20:00:18
>> Compute by numerical integral...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstokesnintg.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 20:02:35
>> Complete the computation!
>> Computation end time: 2024-09-23 20:23:45
    
```

Save computation process as

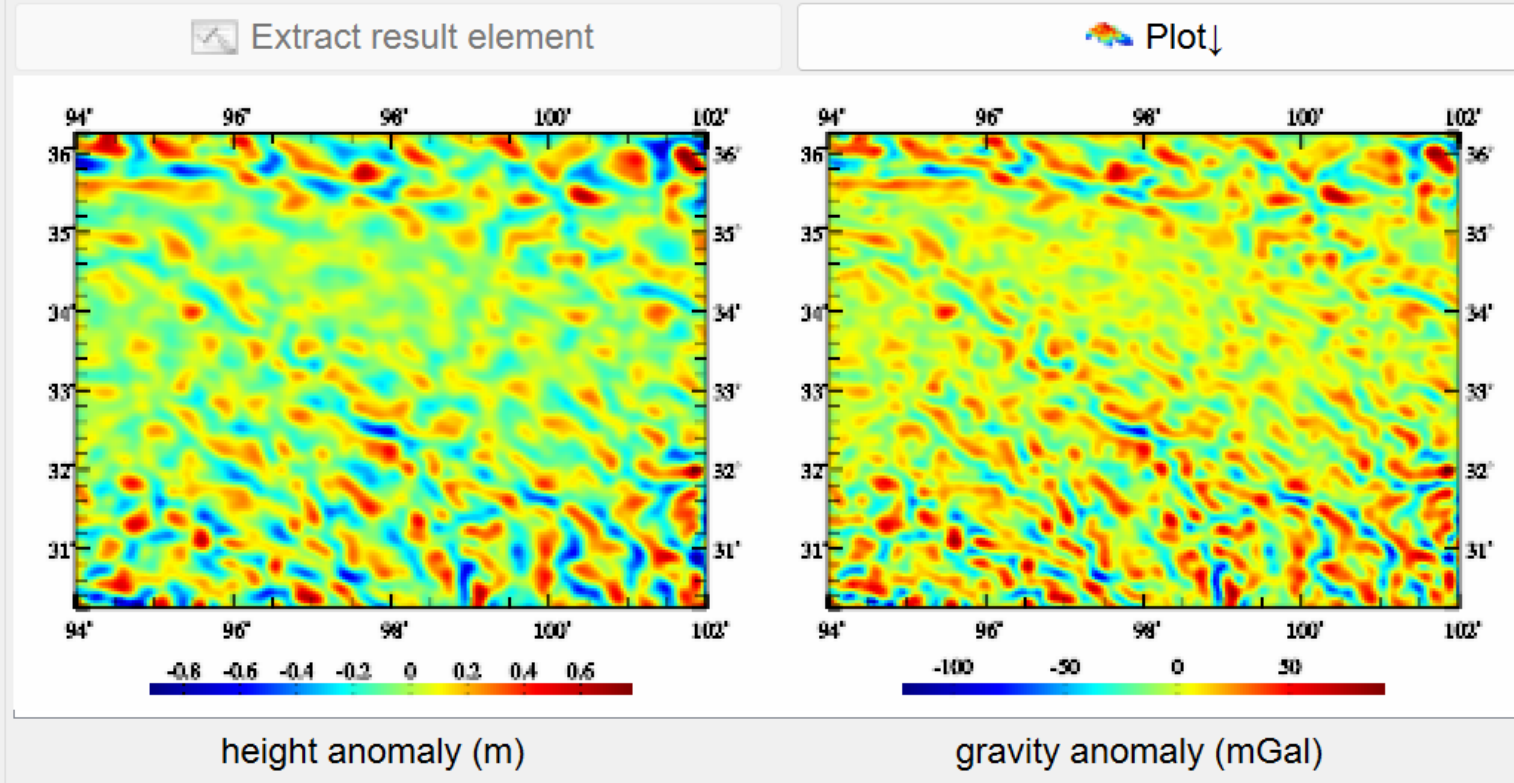
Integral radius 150 km

Save the results as

Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-6.7082	-3.5451	-0.1911	3.0391	6.6519	10.3730
36.7580	35.8638	35.2066	34.1624	32.4529	32.1184
43.8609	47.1039	49.4558	52.2163	55.5724	56.0212
4.5287	-8.9848	-23.7249	-30.1206	-31.7801	-39.6205
5.7532	11.3936	12.7210	14.9511	18.9953	19.5816
28.0887	27.6742	24.2507	20.7547	12.5472	2.4261
24.3313	32.0133	41.5405	46.6957	45.8446	49.2392
-58.8703	-52.9381	-43.6688	-32.7235	-18.4676	-7.3091
13.7746	11.6956	10.1260	9.3898	9.3222	10.0556
28.0073	27.1485	25.4340	22.3360	18.5072	14.2898
17.4349	22.5400	26.0993	29.6066	31.5147	32.3806
-12.9644	-15.9979	-19.6681	-24.2073	-28.0318	-33.9067
-60.1987	-59.1808	-55.8066	-52.7477	-48.8362	-44.7585
5.6019	8.5282	9.6246	8.9249	6.5753	3.0689
4.2451	11.7662	18.6738	25.5670	31.5455	36.9296
26.1350	18.6380	10.9680	3.6098	-7.6106	-18.3577
-30.1325	-19.4527	-10.3495	-2.6276	3.8415	9.0357
13.3615	14.0104	14.6722	15.2175	15.2282	14.6317



- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity anomaly by the inverse Stokes integral – FFT

Save as Import parameters Start Computation Save process Follow example

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the height anomaly grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Select integral algorithm

2D FFT algorithm

>> Computation Process ** Operation Prompts

>> Complete the computation!
 >> Computation end time: 2024-09-23 20:00:18
 >> Compute by numerical integral...
 >> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstokesnintg.dat.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-23 20:02:35
 >> Complete the computation!
 >> Computation end time: 2024-09-23 20:23:45
 >> Compute by 2D FFT algorithm...
 >> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstokesFFT2.dat.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-23 20:25:19
 >> Complete the computation!
 >> Computation end time: 2024-09-23 20:25:21

Save computation process as

Integral radius 150 km

Save the results as

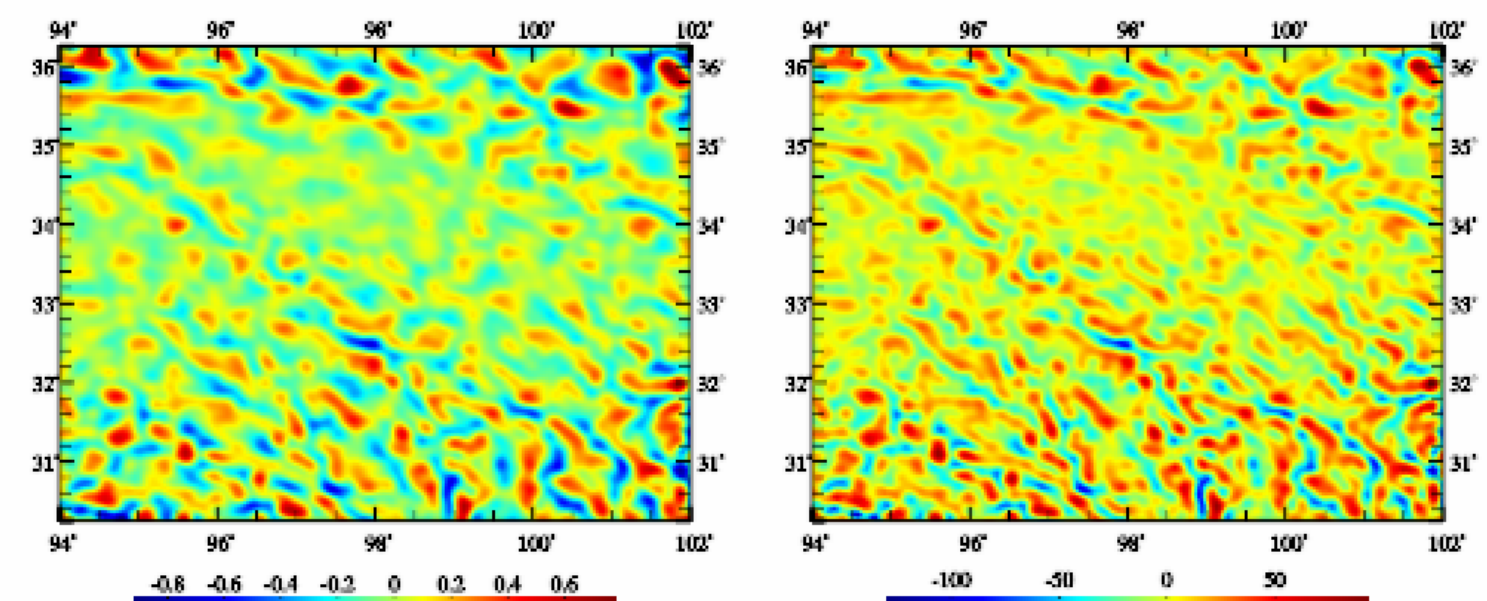
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-6.6410	-3.2026	0.2316	3.4593	7.0945	10.8255
37.5286	36.6150	35.9959	34.9908	33.2789	33.0452
44.8689	48.1887	50.5418	53.3854	56.9225	57.3500
3.9118	-10.4568	-26.1810	-32.8384	-34.3024	-42.4693
6.7626	12.8411	14.2203	16.5622	20.8387	21.3642
28.8099	28.2146	24.4426	20.6938	11.9247	1.1847
25.9640	34.1350	44.3150	49.8107	48.8515	52.5373
-62.4193	-55.9724	-46.0240	-34.3579	-19.1561	-7.3264
14.2773	12.0313	10.3367	9.5350	9.4416	10.1966
28.7700	27.8483	26.0376	22.7685	18.7392	14.3167
18.4754	23.9095	27.6606	31.3232	33.2401	34.0322
-14.0465	-16.9056	-20.4665	-24.9763	-28.7053	-34.6495
-61.5298	-60.5110	-56.9828	-53.8340	-49.8113	-45.6578
5.6003	8.6451	9.7903	9.0685	6.6274	2.9845
4.7836	12.6714	19.8668	27.0328	33.2128	38.7498
26.5940	18.7831	10.8483	3.3203	-8.3415	-19.4523
-31.0409	-19.8066	-10.2825	-2.2353	4.4813	9.8496
14.0066	14.7222	15.4382	16.0140	16.0022	15.3307

Extract result element

Plot



height anomaly (m)

gravity anomaly (mGal)

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity anomaly by the inverse Stokes integral – FFT

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

- Open the ellipsoidal height grid file of the equipotential surface
- Open the height anomaly grid file on the equipotential surface

Select calculation point file format
ellipsoidal height grid file

Select integral algorithm
1D FFT algorithm

>> Computation Process ** Operation Prompts

```
>> Complete the computation!
>> Computation end time: 2024-09-23 20:23:45
>> Compute by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstokesFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 20:25:19
>> Complete the computation!
>> Computation end time: 2024-09-23 20:25:21
>> Compute by 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invstokesFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 20:26:22
>> Complete the computation!
>> Computation end time: 2024-09-23 20:26:42
```

Save computation process as

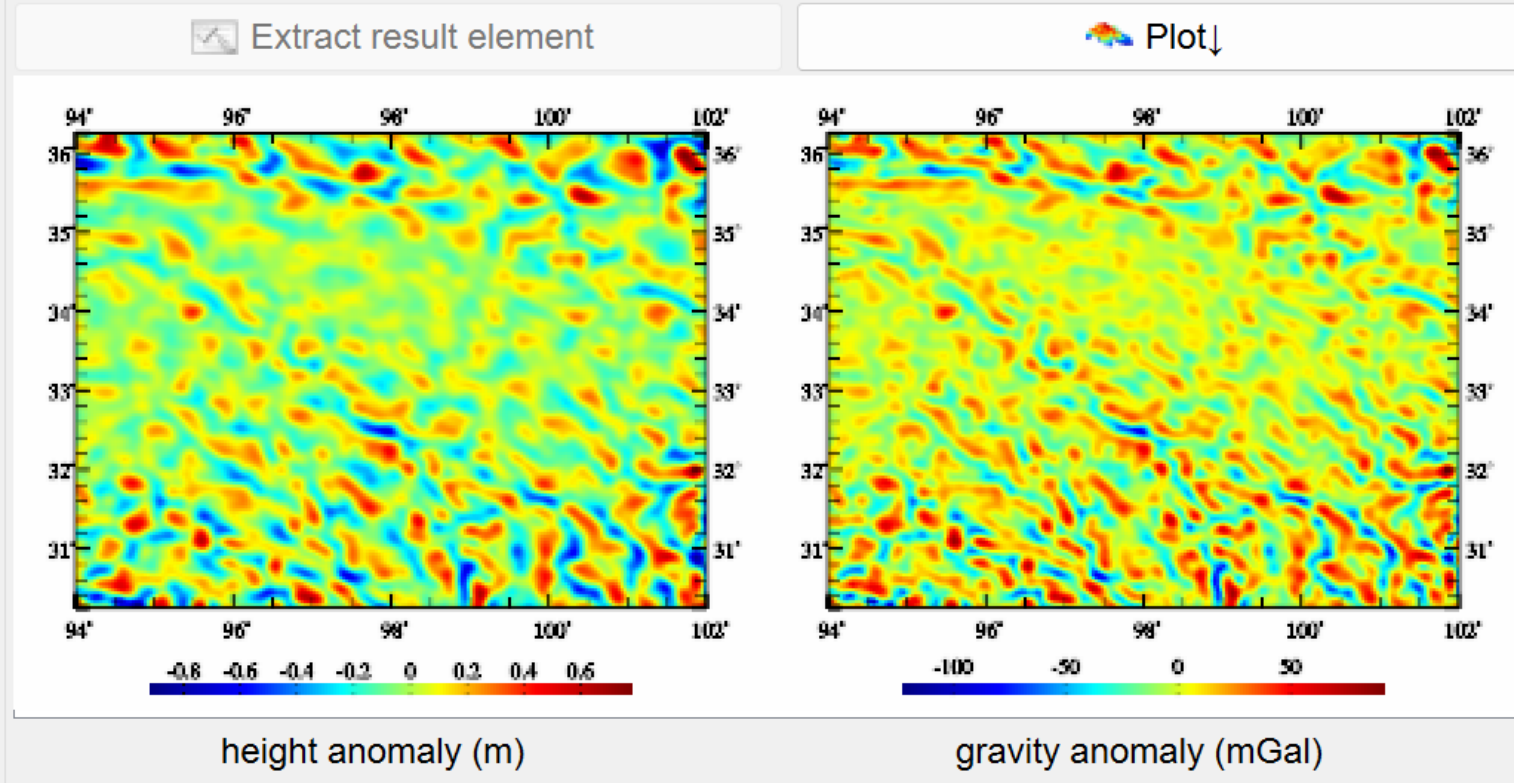
Integral radius 150 km

Save the results as

Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-6.6465	-3.4745	-0.1377	3.0659	6.6523	10.3445
36.5574	35.6681	35.0211	33.9905	32.2946	31.9757
43.6352	46.8619	49.1951	51.9439	55.2959	55.7383
4.4207	-9.0914	-23.8367	-30.2137	-31.8351	-39.6541
5.8305	11.4800	12.8026	15.0283	19.0690	19.6427
27.9519	27.5188	24.0797	20.5810	12.3695	2.2526
24.3372	32.0177	41.5493	46.7052	45.8468	49.2509
-58.8377	-52.8883	-43.6085	-32.6614	-18.4022	-7.2502
13.7252	11.6423	10.0699	9.3318	9.2618	9.9921
27.8775	27.0178	25.3051	22.2106	18.3875	14.1783
17.4225	22.5274	26.0820	29.5806	31.4745	32.3244
-12.9933	-15.9802	-19.6071	-24.1060	-27.8878	-33.7242
-59.8794	-58.8698	-55.5034	-52.4579	-48.5640	-44.5097
5.5570	8.4744	9.5680	8.8711	6.5288	3.0334
4.2763	11.7823	18.6700	25.5415	31.4969	36.8566
25.9836	18.5085	10.8679	3.5488	-7.6359	-18.3413
-30.0003	-19.3378	-10.2560	-2.5563	3.8909	9.0644
13.3320	13.9842	14.6477	15.1927	15.2008	14.6000



- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity disturbance by the inverse Hotine integral – Numerical

- Computation of gravity anomaly by the inverse Stokes integral
- Computation of gravity disturbance by the inverse Hotine integral**
- Computation of the inverse Vening Meinesz integral
- Computation of anomalous field elements from height anomaly
- Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the height anomaly grid file on the equipotential surface

Select calculation point file format
discrete calculation point file

Open the calculation point file on the equipotential surface

Set input point file format
number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential boundary surface and residual height anomaly (m) grid on the surface, compute the residual gravity disturbance on the surface by the inverse Hotine integral.

** Input the ellipsoidal height grid file of the equipotential surface and height anomaly grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/landgeoidhgt.dat.

>> Open the height anomaly grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/resGMlandbm541_1800.ksi.

>> Open the calculation point file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invhtn.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual gravity disturbance.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:30:46

>> Complete the computation!

>> Computation end time: 2024-09-23 20:31:41

Integral radius 150 km

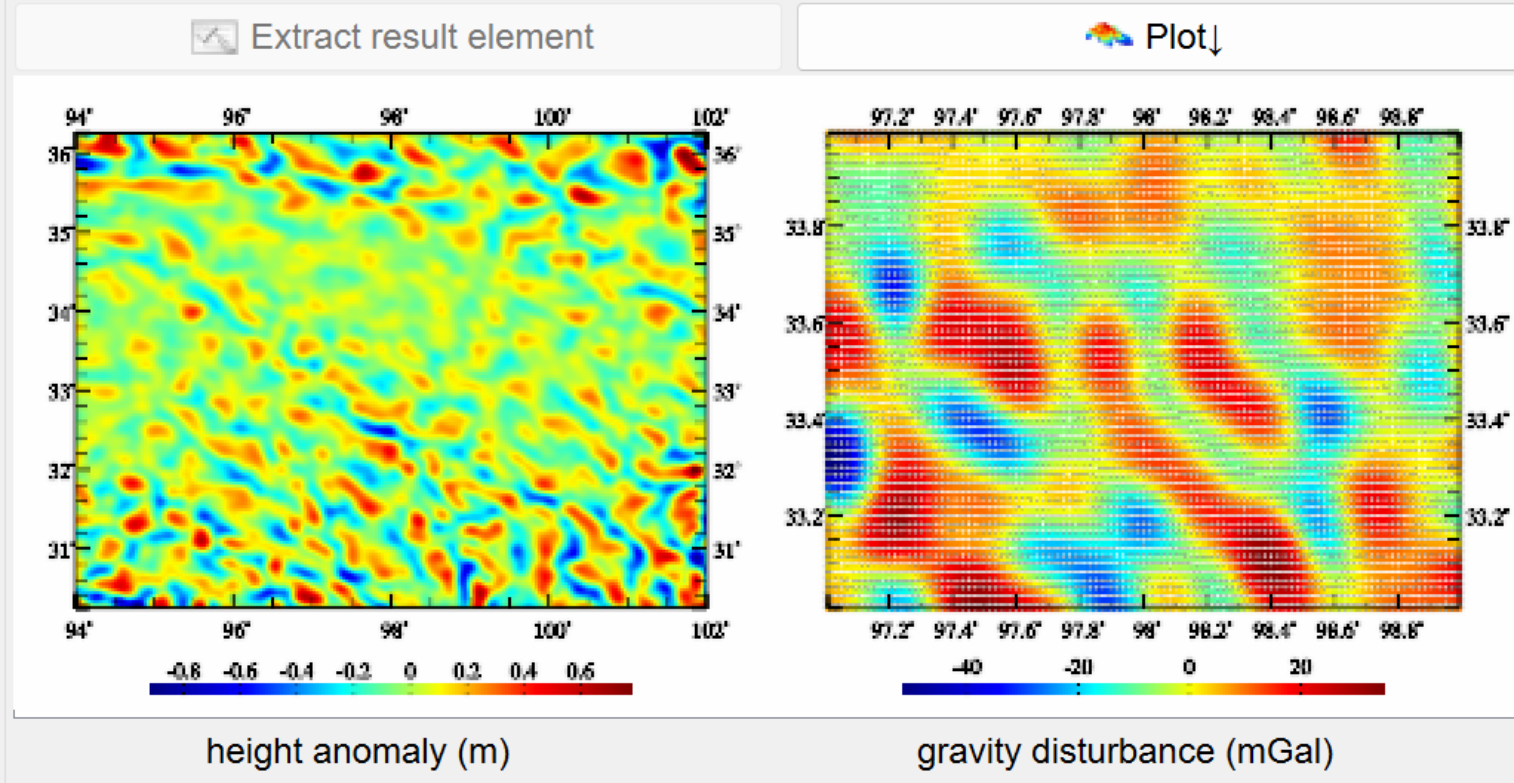
Save the results as

Import setting parameters

Start Computation

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-37.2501	6.2142
2	97.025000	33.008333	3989.787	-37.2203	5.8380
3	97.041667	33.008333	4034.817	-37.1899	4.9738
4	97.058333	33.008333	4070.847	-37.1590	3.6134
5	97.075000	33.008333	4106.877	-37.1276	1.6840
6	97.091667	33.008333	4119.913	-37.0959	-0.6950
7	97.108333	33.008333	4115.946	-37.0640	-3.4436
8	97.125000	33.008333	4090.977	-37.0318	-6.5390
9	97.141667	33.008333	4070.007	-36.9990	-9.6002
10	97.158333	33.008333	3991.047	-36.9665	-13.3681
11	97.175000	33.008333	3985.070	-36.9327	-16.1738
12	97.191667	33.008333	3956.107	-36.8988	-19.0284
13	97.208333	33.008333	3965.137	-36.8642	-20.6898
14	97.225000	33.008333	3964.173	-36.8295	-21.9527
15	97.241667	33.008333	3983.205	-36.7943	-21.8168
16	97.258333	33.008333	3953.251	-36.7595	-21.7681
17	97.275000	33.008333	4016.279	-36.7238	-18.7898
18	97.291667	33.008333	4054.318	-36.6883	-15.3468
19	97.308333	33.008333	4090.360	-36.6528	-10.9020

Ignore the ellipsoidal height



- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity disturbance by the inverse Hotine integral – FFT

Save as Import parameters Start Computation Save process Follow example

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the height anomaly grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Select integral algorithm

2D FFT algorithm

>> Computation Process ** Operation Prompts

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invhtn.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual gravity disturbance.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:30:46

>> Complete the computation!

>> Computation end time: 2024-09-23 20:31:41

>> Compute by 2D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invhotineFFT2.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:33:27

>> Complete the computation!

>> Computation end time: 2024-09-23 20:33:28

Save computation process as

Integral radius 150 km

Save the results as

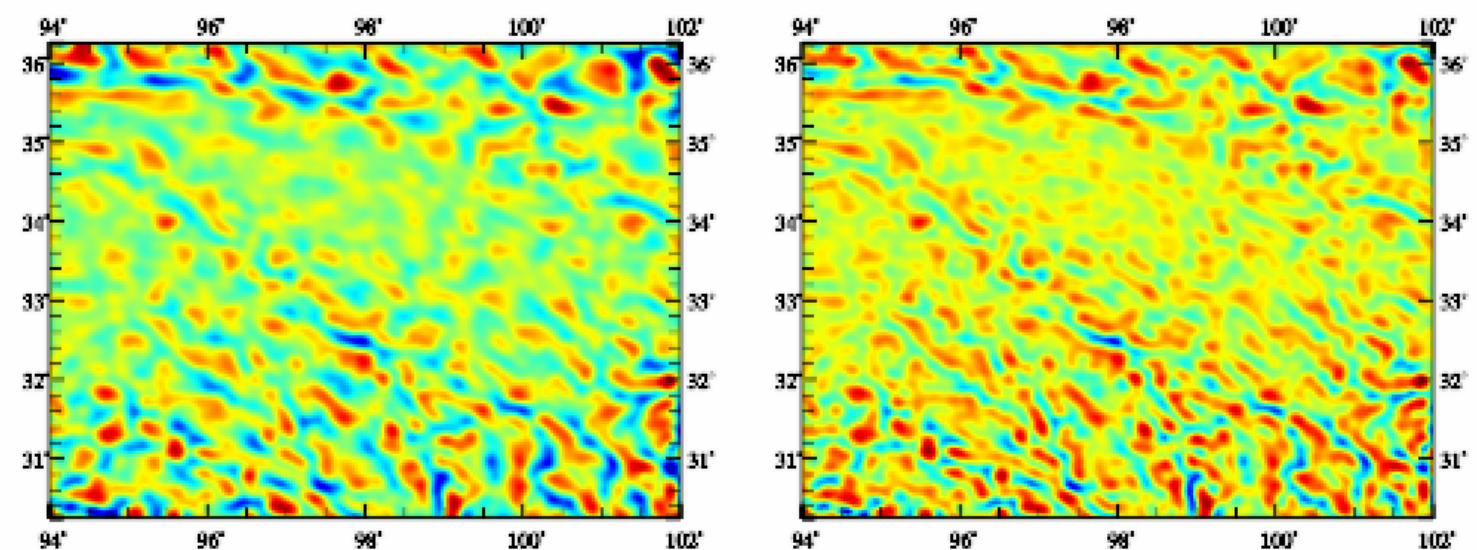
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-6.6584	-3.2208	0.2132	3.4412	7.0769	10.8086
37.5213	36.6085	35.9900	34.9853	33.2739	33.0405
44.8781	48.1997	50.5544	53.3990	56.9370	57.3653
3.9634	-10.3994	-26.1190	-32.7749	-34.2403	-42.4099
6.7417	12.8148	14.1902	16.5290	20.8034	21.3282
28.8052	28.2151	24.4487	20.7054	11.9420	1.2073
25.9420	34.1049	44.2783	49.7698	48.8091	52.4951
-62.3878	-55.9423	-45.9979	-34.3377	-19.1429	-7.3200
14.2696	12.0256	10.3328	9.5326	9.4403	10.1960
28.7690	27.8481	26.0383	22.7705	18.7425	14.3215
18.4605	23.8915	27.6406	31.3024	33.2198	34.0136
-14.0279	-16.8872	-20.4487	-24.9592	-28.6888	-34.6333
-61.5198	-60.5022	-56.9754	-53.8277	-49.8060	-45.6533
5.6004	8.6447	9.7898	9.0682	6.6277	2.9857
4.7680	12.6517	19.8438	27.0070	33.1853	38.7214
26.5999	18.7942	10.8645	3.3414	-8.3153	-19.4213
-31.0218	-19.7939	-10.2757	-2.2338	4.4783	9.8430
13.9926	14.7082	15.4246	16.0011	15.9904	15.3205

Extract result element

Plot



height anomaly (m)

gravity disturbance (mGal)

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of gravity disturbance by the inverse Hotine integral – FFT

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the height anomaly grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Select integral algorithm

1D FFT algorithm

>> Computation Process ** Operation Prompts

```
>> Complete the computation!
>> Computation end time: 2024-09-23 20:31:41
>> Compute by 2D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invhotineFFT2.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 20:33:27
>> Complete the computation!
>> Computation end time: 2024-09-23 20:33:28
>> Compute by 1D FFT algorithm...
>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invhotineFFT1.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-23 20:34:02
>> Complete the computation!
>> Computation end time: 2024-09-23 20:34:20
```

Save computation process as

Integral radius 150 km

Save the results as

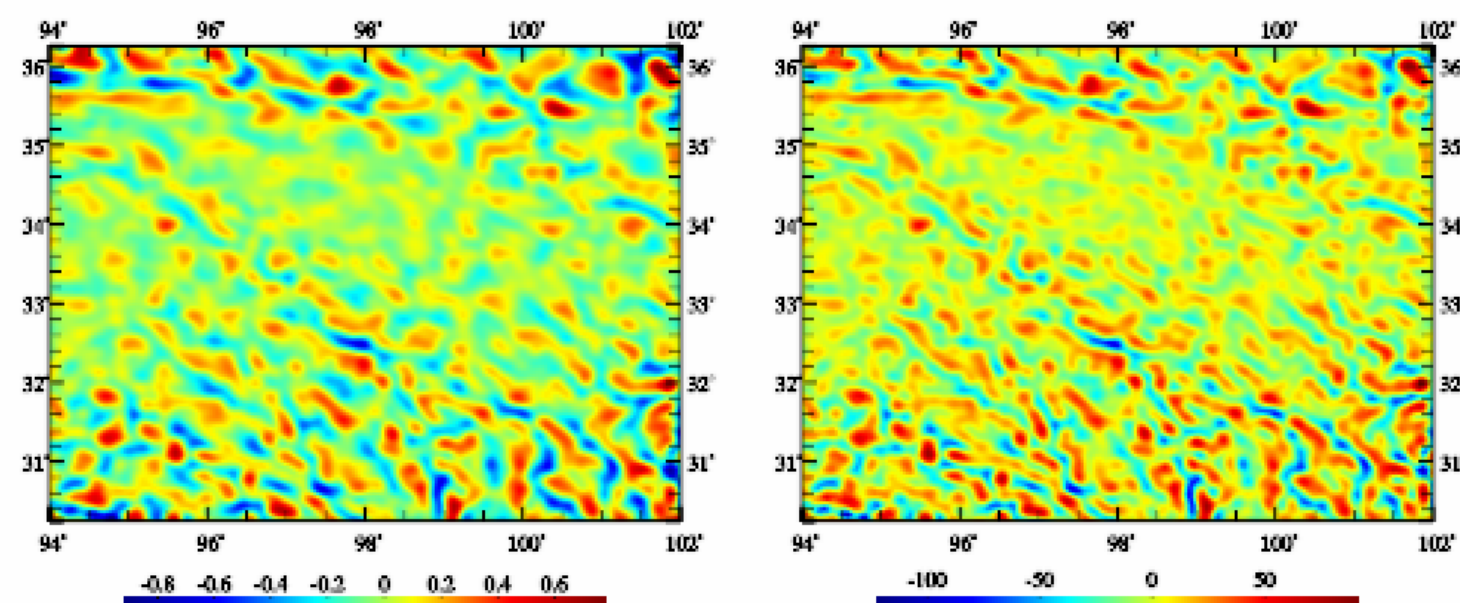
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-6.6639	-3.4926	-0.1560	3.0478	6.6347	10.3276
36.5500	35.6615	35.0152	33.9850	32.2896	31.9709
43.6445	46.8729	49.2076	51.9576	55.3104	55.7537
4.4722	-9.0340	-23.7747	-30.1502	-31.7729	-39.5946
5.8096	11.4537	12.7724	14.9951	19.0336	19.6067
27.9472	27.5193	24.0858	20.5926	12.3869	2.2753
24.3152	31.9876	41.5126	46.6642	45.8044	49.2087
-58.8062	-52.8582	-43.5824	-32.6412	-18.3890	-7.2438
13.7175	11.6366	10.0661	9.3293	9.2604	9.9915
27.8765	27.0175	25.3058	22.2126	18.3909	14.1831
17.4075	22.5094	26.0620	29.5597	31.4541	32.3058
-12.9747	-15.9618	-19.5893	-24.0889	-27.8713	-33.7079
-59.8694	-58.8610	-55.4960	-52.4517	-48.5587	-44.5051
5.5571	8.4740	9.5675	8.8708	6.5291	3.0346
4.2607	11.7627	18.6470	25.5158	31.4693	36.8281
25.9895	18.5196	10.8841	3.5698	-7.6097	-18.3103
-29.9812	-19.3251	-10.2492	-2.5548	3.8879	9.0578
13.3180	13.9702	14.6340	15.1797	15.1891	14.5899

Extract result element

Plot



height anomaly (m)

gravity disturbance (mGal)

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of the inverse Vening Meinesz integral – Numerical

- Computation of gravity anomaly by the inverse Stokes integral
- Computation of gravity disturbance by the inverse Hotine integral
- Computation of the inverse Vening Meinesz integral**
- Computation of anomalous field elements from height anomaly
- Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the vertical deflection vector grid file on the equipotential surface

Select calculation point file format

discrete calculation point file

Open the calculation point file on the equipotential surface

Set input point file format

number of rows of file header 1

>> Computation Process ** Operation Prompts

** Input the ellipsoidal height grid file of the equipotential surface and vertical deflection vector grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/landgeoidhgt.dat.

>> Open the vertical deflection vector grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/resGMLgeoid541_1800.dft.

>> Open the calculation point file on the equipotential surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMnintg.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and 3 columns of attributes including the residual height anomaly, gravity anomaly and gravity disturbance.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:35:31

>> Complete the computation!

>> Computation end time: 2024-09-23 20:36:44

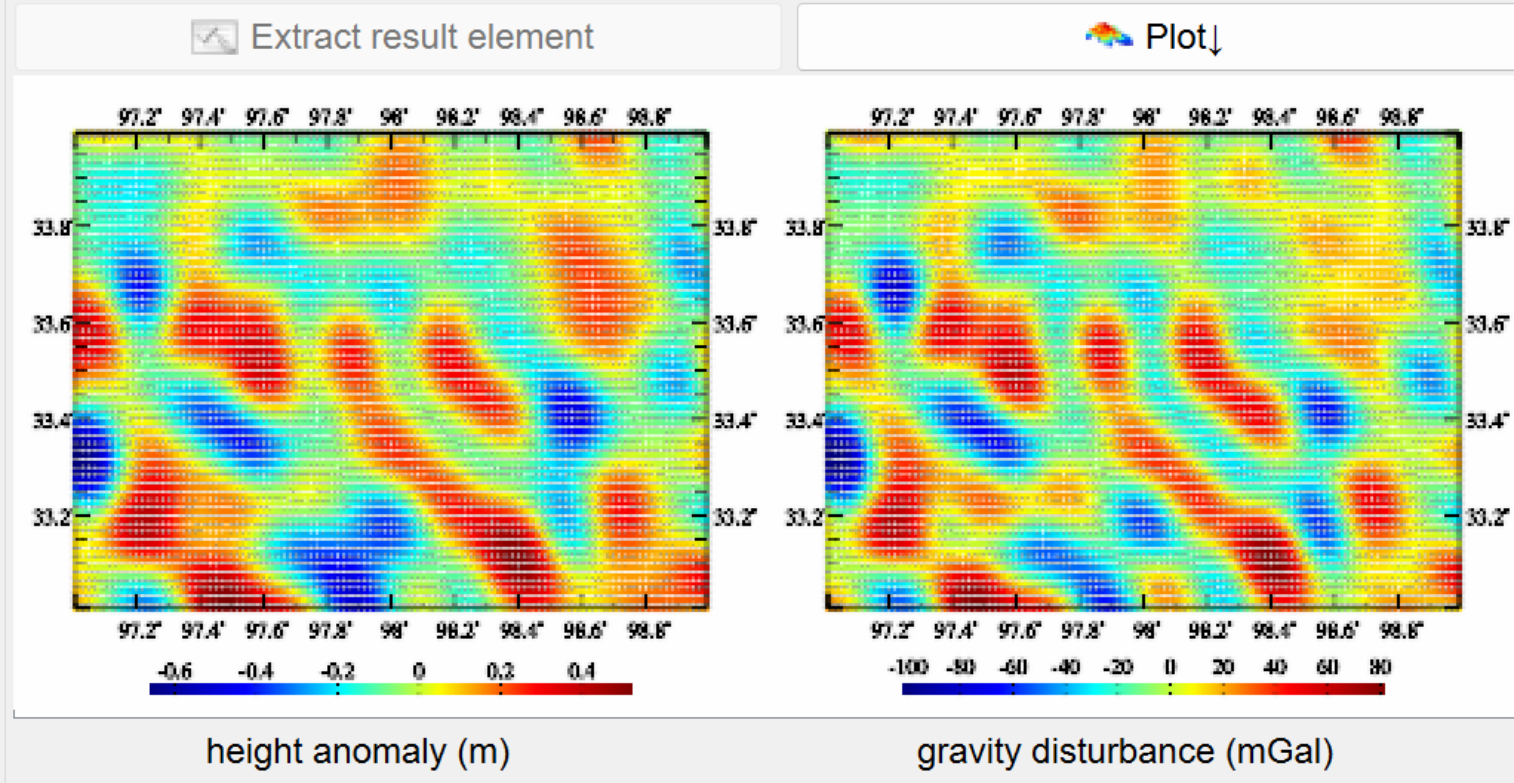
Integral radius 150 km

Save the results as

Import setting parameters

Start Computation

cimal)	lat	ellipHeight (m)				
3333	33.008333	3942.764	-37.2501	0.0986	23.0001	22.9698
5000	33.008333	3989.787	-37.2203	0.0846	22.9339	22.9078
1667	33.008333	4034.817	-37.1899	0.0639	21.1547	21.1350
3333	33.008333	4070.847	-37.1590	0.0366	17.6405	17.6293
5000	33.008333	4106.877	-37.1276	0.0033	12.4966	12.4956
1667	33.008333	4119.913	-37.0959	-0.0351	5.9362	5.9470
3333	33.008333	4115.946	-37.0640	-0.0772	-1.7394	-1.7156
5000	33.008333	4090.977	-37.0318	-0.1213	-10.1584	-10.1211
1667	33.008333	4070.007	-36.9990	-0.1655	-18.9011	-18.8502
3333	33.008333	3991.047	-36.9665	-0.2077	-27.5122	-27.4484
5000	33.008333	3985.070	-36.9327	-0.2458	-35.5120	-35.4365
1667	33.008333	3956.107	-36.8988	-0.2773	-42.4147	-42.3294
3333	33.008333	3965.137	-36.8642	-0.2999	-47.7421	-47.6499
5000	33.008333	964.173	-36.8295	-0.3115	-51.0471	-50.9514
1667	33.008333	983.205	-36.7943	-0.3100	-51.9444	-51.8491
3333	33.008333	953.251	-36.7595	-0.2941	-50.1432	-50.0528
5000	33.008333	4016.279	-36.7238	-0.2629	-45.4879	-45.4071
1667	33.008333	4054.318	-36.6883	-0.2165	-37.9888	-37.9222



Ignore the ellipsoidal height

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of the inverse Vening Meinesz integral – FFT

Save as Import parameters Start Computation Save process Follow example

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the vertical deflection vector grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Select integral algorithm

2D FFT algorithm

>> Computation Process ** Operation Prompts

disturbance.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:35:31

>> Complete the computation!

>> Computation end time: 2024-09-23 20:36:44

>> Compute by 2D FFT algorithm...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT2.txt.

>> Save the height anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT2.ksi.

>> Save the gravity disturbance grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT2.rga.

>> Save the gravity anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT2.gra.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:38:29

>> Complete the computation!

>> Computation end time: 2024-09-23 20:38:33

Save computation process as

Integral radius 150 km

Save the results as

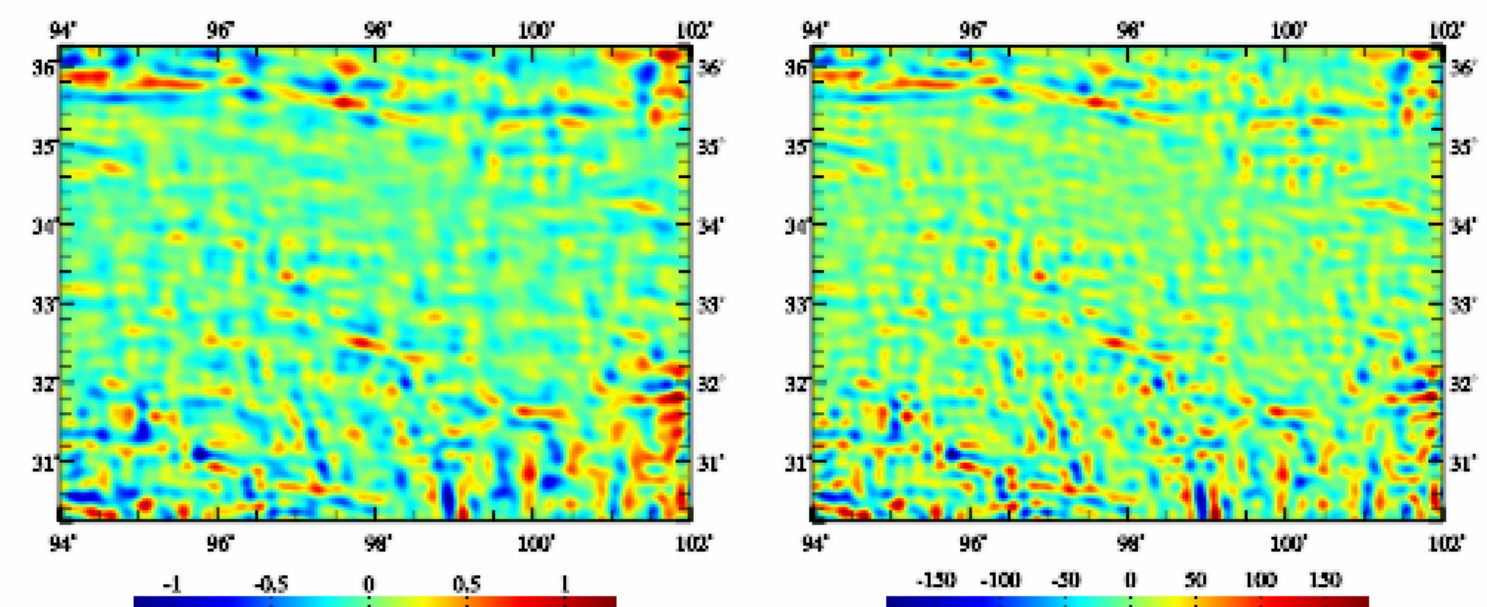
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
0.1280	0.1327	0.0986	0.0433	-0.0224	-0.0910
-0.4254	-0.3999	-0.3598	-0.3066	-0.2436	-0.1756
-0.1179	-0.1453	-0.1565	-0.1483	-0.1207	-0.0768
-0.0151	-0.0785	-0.1354	-0.1797	-0.2064	-0.2132
0.3349	0.3741	0.4003	0.4122	0.4089	0.3904
-0.3038	-0.3751	-0.4408	-0.5001	-0.5515	-0.5929
0.0786	0.2103	0.3196	0.3958	0.4316	0.4235
-0.2695	-0.2007	-0.1085	-0.0047	0.0984	0.1893
0.0264	-0.0020	-0.0203	-0.0307	-0.0365	-0.0410
-0.2177	-0.2401	-0.2634	-0.2873	-0.3108	-0.3316
0.0467	0.0913	0.1121	0.1052	0.0701	0.0100
-0.1209	0.0013	0.1284	0.2511	0.3614	0.4538
0.6658	0.6550	0.6320	0.5938	0.5387	0.4673
-0.1721	-0.1628	-0.1465	-0.1274	-0.1089	-0.0926
0.1315	0.1496	0.1536	0.1402	0.1083	0.0588
-0.2766	-0.2228	-0.1617	-0.0990	-0.0397	0.0128
0.2671	0.2814	0.2876	0.2833	0.2677	0.2411
0.0669	0.0819	0.0903	0.0883	0.0736	0.0461

Extract result element

Plot



height anomaly (m)

gravity disturbance (mGal)

The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of the inverse Vening Meinesz integral – FFT

Save as Import parameters Start Computation Save process Follow example

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the equipotential surface

Open the vertical deflection vector grid file on the equipotential surface

Select calculation point file format

ellipsoidal height grid file

Select integral algorithm

1D FFT algorithm

>> Computation Process ** Operation Prompts

>> Save the gravity anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT2.gra.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-23 20:38:29
 >> Complete the computation!
 >> Computation end time: 2024-09-23 20:38:33
 >> Compute by 1D FFT algorithm...
 >> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT1.txt.
 >> Save the height anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT1.ksi.
 >> Save the gravity disturbance grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT1.rga.
 >> Save the gravity anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invVMFFT1.gra.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-23 20:39:28
 >> Complete the computation!
 >> Computation end time: 2024-09-23 20:40:58

Save computation process as

Integral radius 150 km

Save the results as

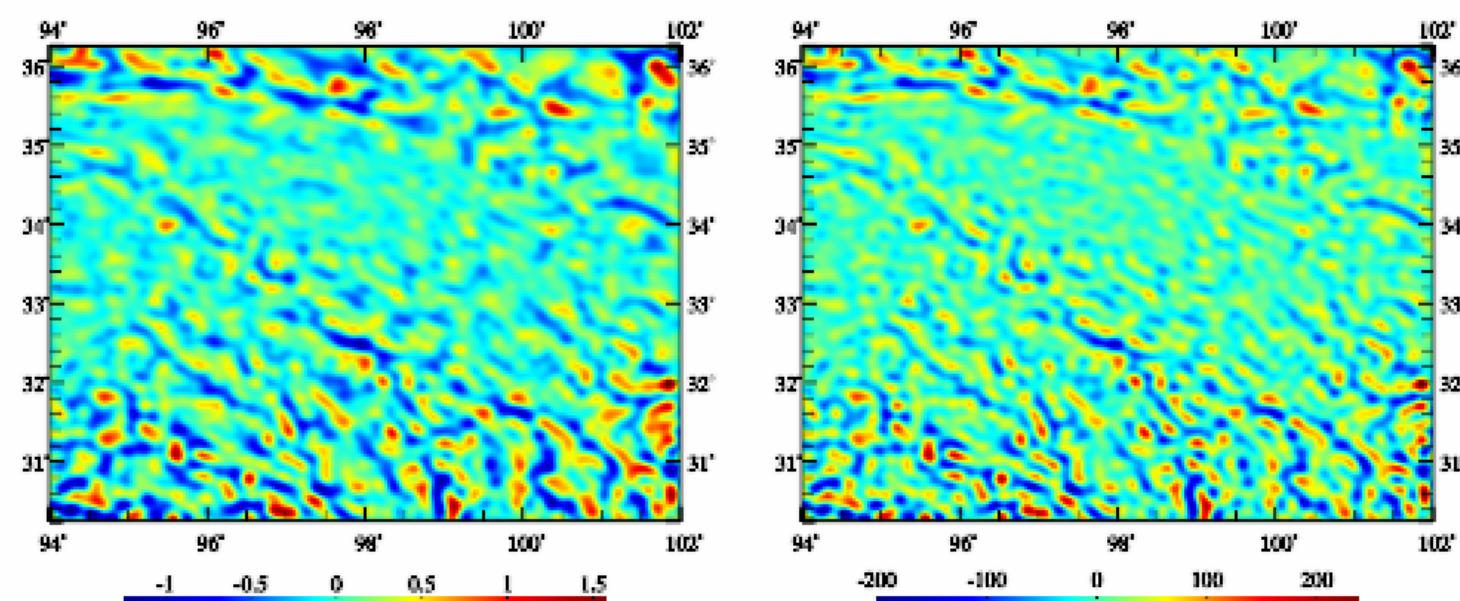
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
0.0580	0.0564	0.0585	0.0612	0.0638	0.0665
0.0288	0.0192	0.0142	0.0145	0.0196	0.0275
-0.2325	-0.2663	-0.2868	-0.2930	-0.2868	-0.2721
-0.6373	-0.6958	-0.7310	-0.7377	-0.7127	-0.6565
0.4076	0.4529	0.4809	0.4930	0.4911	0.4768
-0.0231	-0.0915	-0.1622	-0.2336	-0.3027	-0.3653
0.4099	0.5883	0.7397	0.8481	0.9025	0.8942
-0.5901	-0.5632	-0.4873	-0.3747	-0.2404	-0.1003
0.1089	0.0615	0.0211	-0.0111	-0.0350	-0.0515
0.0047	0.0079	0.0040	-0.0074	-0.0250	-0.0461
0.2976	0.3571	0.3940	0.4020	0.3780	0.3228
-0.3702	-0.3424	-0.3057	-0.2670	-0.2321	-0.2049
-0.0947	-0.0690	-0.0468	-0.0309	-0.0231	-0.0235
-0.0131	0.0018	0.0096	0.0082	-0.0031	-0.0230
0.1404	0.2157	0.2854	0.3430	0.3836	0.4036
-0.1584	-0.2263	-0.2908	-0.3517	-0.4083	-0.4590
-0.2058	-0.1199	-0.0404	0.0281	0.0820	0.1198
0.1510	0.1570	0.1570	0.1483	0.1292	0.0996

Extract result element

Plot



height anomaly (m)

gravity disturbance (mGal)

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external anomalous gravity field elements from height anomaly

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the boundary surface

Open the height anomaly grid file on the boundary surface

Select calculation point file format

discrete calculation point file

Open the calculation point position file

Set input point file format

number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the boundary surface and residual height anomaly grid (m) on the surface, compute the residual gravity anomaly (mGal), gravity disturbance (mGal) and vertical deflection vector (" SW) on or outside the geoid. The inverse operation of height anomaly adopts the combination algorithm with Poisson integral and differentiation, which does not require that the boundary surface should be a gravity equipotential surface.

** Input the ellipsoidal height grid of the boundary surface and height anomaly grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the boundary surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/landgeoidhgt.dat.

>> Open the height anomaly grid file on the boundary surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/resGMlgeoid541_1800.ksi.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/Integralgrainverse/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/invksiouter.txt.

>> Behind the input calculation point file record, appends 4 columns of attributes including residual gravity anomaly, residual gravity disturbance and residual vertical deflection southward and westward.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:46:10

>> Complete the computation!

>> Computation end time: 2024-09-23 20:54:09

Integral radius 150 km

Save the results as

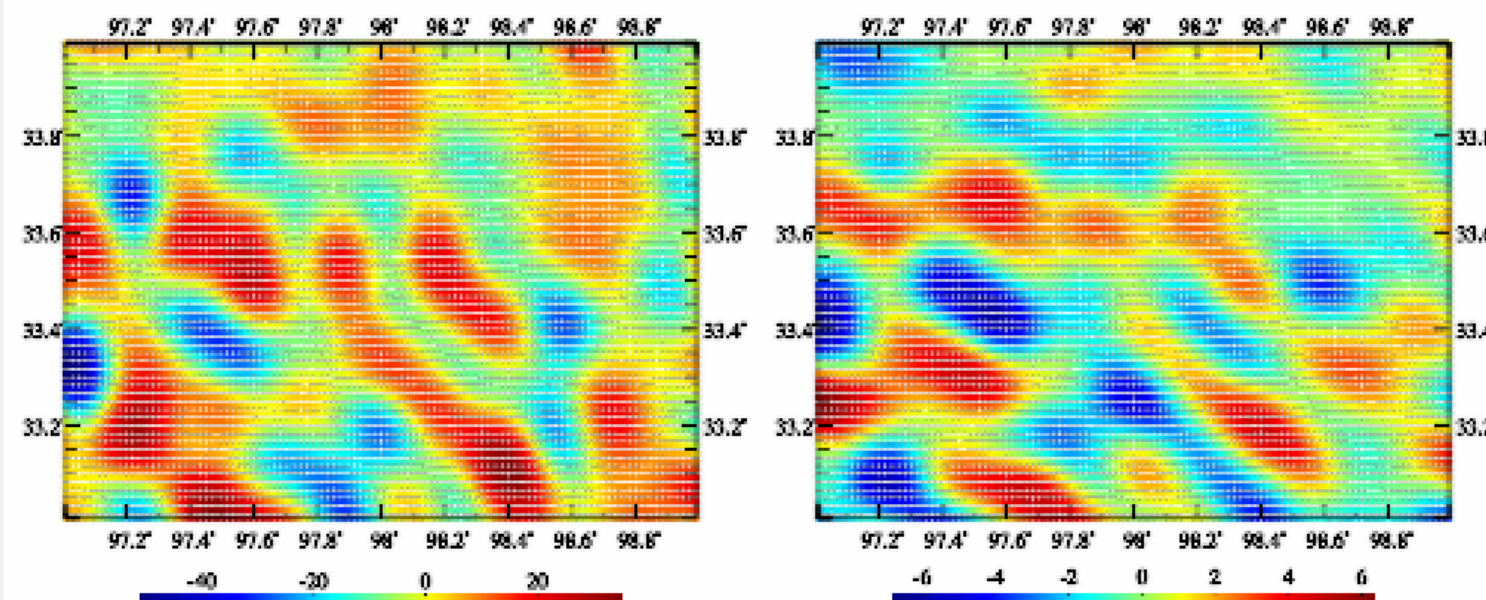
Import setting parameters

Start Computation

cimal)	lat	ellipHeight (m)				
3333	33.008333	3942.764	6.2612	6.2592	-2.5007	0.4847
5000	33.008333	3989.787	6.0388	6.0365	-2.4248	0.6987
1667	33.008333	4034.817	5.2179	5.2151	-2.3076	0.9304
3333	33.008333	4070.847	3.8190	3.8156	-2.1573	1.1571
5000	33.008333	4106.877	1.8631	1.8588	-1.9846	1.3566
1667	33.008333	4119.913	-0.5421	-0.5472	-1.8034	1.5177
3333	33.008333	4115.946	-3.3350	-3.3411	-1.6284	1.6250
5000	33.008333	4090.977	-6.4301	-6.4372	-1.4752	1.6670
1667	33.008333	4070.007	-9.6925	-9.7007	-1.3639	1.6181
3333	33.008333	3991.047	-13.0955	-13.1048	-1.3008	1.4939
5000	33.008333	3985.070	-16.1623	-16.1724	-1.3230	1.2209
1667	33.008333	3956.107	-18.9050	-18.9158	-1.4222	0.8360
3333	33.008333	3965.137	-20.8767	-20.8879	-1.6097	0.3179
5000	33.008333	3964.173	-22.0755	-22.0867	-1.8711	-0.3092
1667	33.008333	3983.205	-22.1895	-22.2002	-2.1941	-1.0304
3333	33.008333	3953.251	-21.4492	-21.4591	-2.5624	-1.8234
5000	33.008333	4016.279	-19.0783	-19.0868	-2.9355	-2.6206
1667	33.008333	4054.318	-15.7055	-15.7122	-3.2973	-3.3943

Extract result element

Plot



gravity disturbance (mGal)

vertical deflection S (")

- The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external anomalous gravity field elements from height anomaly

Save as Import parameters Start Computation Save process Follow example

Computation of gravity anomaly by the inverse Stokes integral

Computation of gravity disturbance by the inverse Hotine integral

Computation of the inverse Vening Meinesz integral

Computation of anomalous field elements from height anomaly

Integral formula of inverse operation

Open the ellipsoidal height grid file of the boundary surface

Open the height anomaly grid file on the boundary surface

Select calculation point file format

ellipsoidal height grid file

Open the ellipsoidal height grid file of the calculation surface

>> Computation Process ** Operation Prompts

and residual vertical deflection southward and westward.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 20:46:10

>> Complete the computation!

>> Computation end time: 2024-09-23 20:54:09

>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/Integralgrainverse/landbmsurfhgt.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/Integralgrainverse/surfgravfd.dat.

>> Save the gravity anomaly grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/surfgravfd.gra.

>> Save the gravity disturbance grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/surfgravfd.rga.

>> Save vertical deflection vector grid as C:/PAGravf4.5_win64en/examples/Integralgrainverse/surfgravfd.dft.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-23 21:01:44

>> Complete the computation!

>> Computation end time: 2024-09-23 23:13:21

Integral radius 150 km

Save the results as

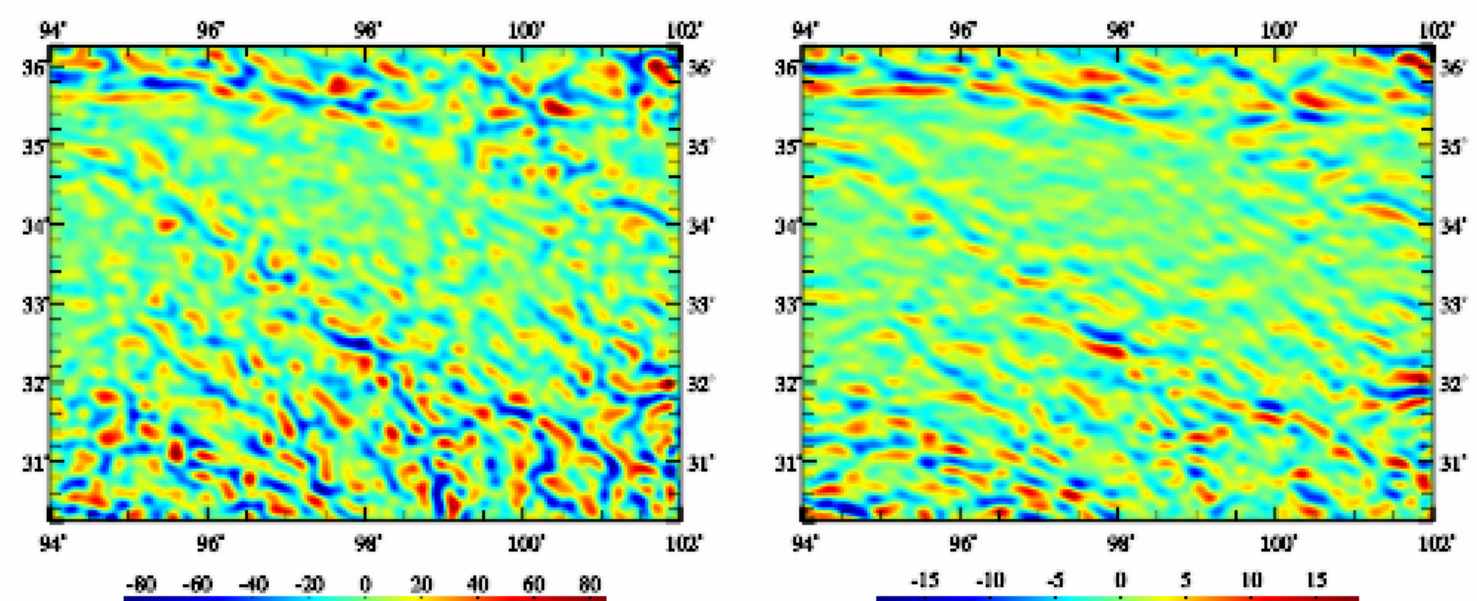
Import setting parameters

Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
11.4128	13.0112	13.5037	13.3752	12.9300	12.3297
12.2286	12.9126	13.7712	14.4755	14.8649	15.6350
-0.5715	-4.2236	-6.0262	-6.7989	-6.5922	-4.3403
-37.2156	-44.7613	-51.0366	-54.3760	-54.4024	-52.2276
27.4578	31.0473	33.1427	34.1140	34.0444	32.8437
-0.8411	-5.0104	-9.3308	-14.1952	-19.0398	-23.9456
28.3579	38.0082	45.8366	50.5764	51.8258	51.0678
-41.3629	-38.2614	-31.7155	-23.1777	-13.4434	-4.5923
7.0217	4.5954	2.5959	1.1491	0.2233	-0.2655
5.2099	5.1750	4.9190	4.0159	2.8697	1.6782
23.9381	27.0111	28.5656	28.6058	26.8087	23.3214
-30.2443	-29.8047	-28.8801	-27.9116	-26.9503	-26.7764
-14.4973	-12.8509	-10.7049	-9.1703	-7.6347	-6.3731
-0.6123	-0.1993	-0.4046	-1.2941	-2.8020	-4.6823
10.4837	15.6332	19.9038	23.1644	25.2077	26.0062
-9.3028	-13.0914	-16.8779	-20.5369	-24.4111	-28.3535
-14.6855	-8.5257	-3.2954	0.8040	3.7755	5.6646
6.8612	8.0384	8.9141	9.2855	8.9443	7.8440

Extract result element

Plot



gravity disturbance (mGal)

vertical deflection S (")

The integral of inverse operation formula belongs to the solution of the Stokes boundary value problem, which requires the integrand height anomaly or vertical deflection to be on the equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Operation of radial gradient integral on anomalous gravity field element

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
Computation of external gravity disturbance from disturbing gravity gradient
Computation of disturbing gravity gradient by inverse operation integral
Computation of external disturbing gravity gradient from gravity disturbance
Computation of Poisson integral on external anomalous field element

Select calculation point file format

 Set input point file format

 number of rows of file header

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential boundary surface and anomalous gravity field element grid on the surface, compute the radial gradient (/km) of the field element on the surface by the numerical integral.

** Input the ellipsoidal height grid file of the equipotential surface and height anomaly grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landgeoidhgt.dat.

>> Open anomalous field element grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/resGMIgeoid541_1800.ksi.

>> Open the calculation point file on the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the radial gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgradient.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of calculated radial gradient.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

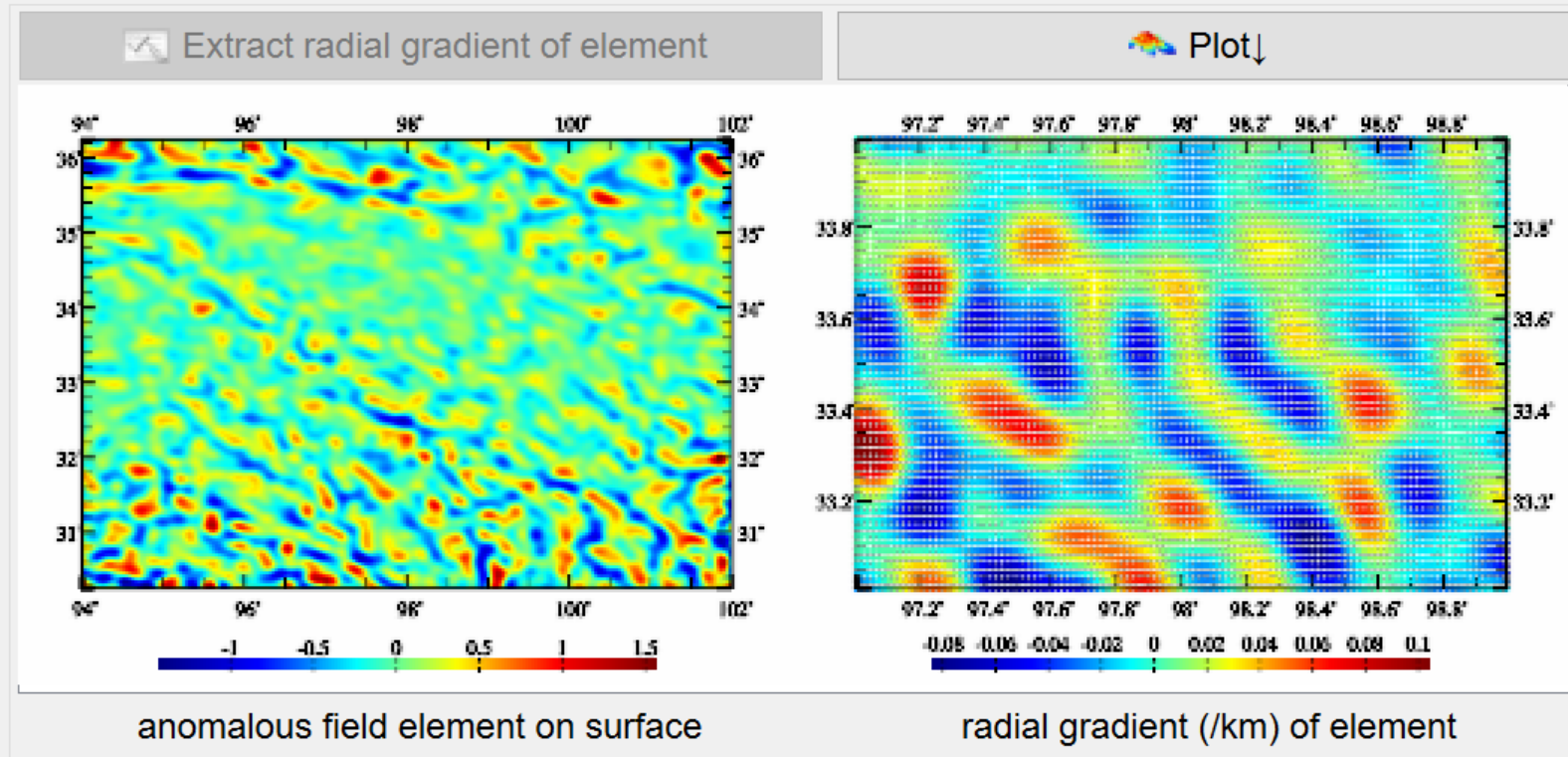
>> Computation start time: 2024-09-24 10:57:09

>> Complete the computation!

Integral radius

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-37.2501	-0.0252
2	97.025000	33.008333	3989.787	-37.2203	-0.0252
3	97.041667	33.008333	4034.817	-37.1899	-0.0234
4	97.058333	33.008333	4070.847	-37.1590	-0.0197
5	97.075000	33.008333	4106.877	-37.1276	-0.0142
6	97.091667	33.008333	4119.913	-37.0959	-0.0074
7	97.108333	33.008333	4115.946	-37.0640	0.0008
8	97.125000	33.008333	4090.977	-37.0318	0.0097
9	97.141667	33.008333	4070.007	-36.9990	0.0190
10	97.158333	33.008333	3991.047	-36.9665	0.0281
11	97.175000	33.008333	3985.070	-36.9327	0.0366
12	97.191667	33.008333	3956.107	-36.8988	0.0439
13	97.208333	33.008333	3965.137	-36.8642	0.0496
14	97.225000	33.008333	3964.173	-36.8295	0.0531
15	97.241667	33.008333	3983.205	-36.7943	0.0541
16	97.258333	33.008333	3953.251	-36.7595	0.0523
17	97.275000	33.008333	4016.279	-36.7238	0.0474
18	97.291667	33.008333	4054.318	-36.6883	0.0396

Ignore the ellipsoidal height



- The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.
- The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Operation of radial gradient integral on anomalous gravity field element

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
Computation of external gravity disturbance from disturbing gravity gradient
Computation of disturbing gravity gradient by inverse operation integral
Computation of external disturbing gravity gradient from gravity disturbance
Computation of Poisson integral on external anomalous field element

Open the ellipsoidal height grid file of the boundary surface
Open the anomalous field element grid file on the boundary surface
 Select calculation point file format
 ellipsoidal height grid file

>> Computation Process ** Operation Prompts

** Look at the file information in the window below, set the input file format parameters...

>> Save the radial gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgradient.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of calculated radial gradient.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 10:57:09

>> Complete the computation!

>> Computation end time: 2024-09-24 10:57:50

>> Save the radial gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgradient.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 10:59:30

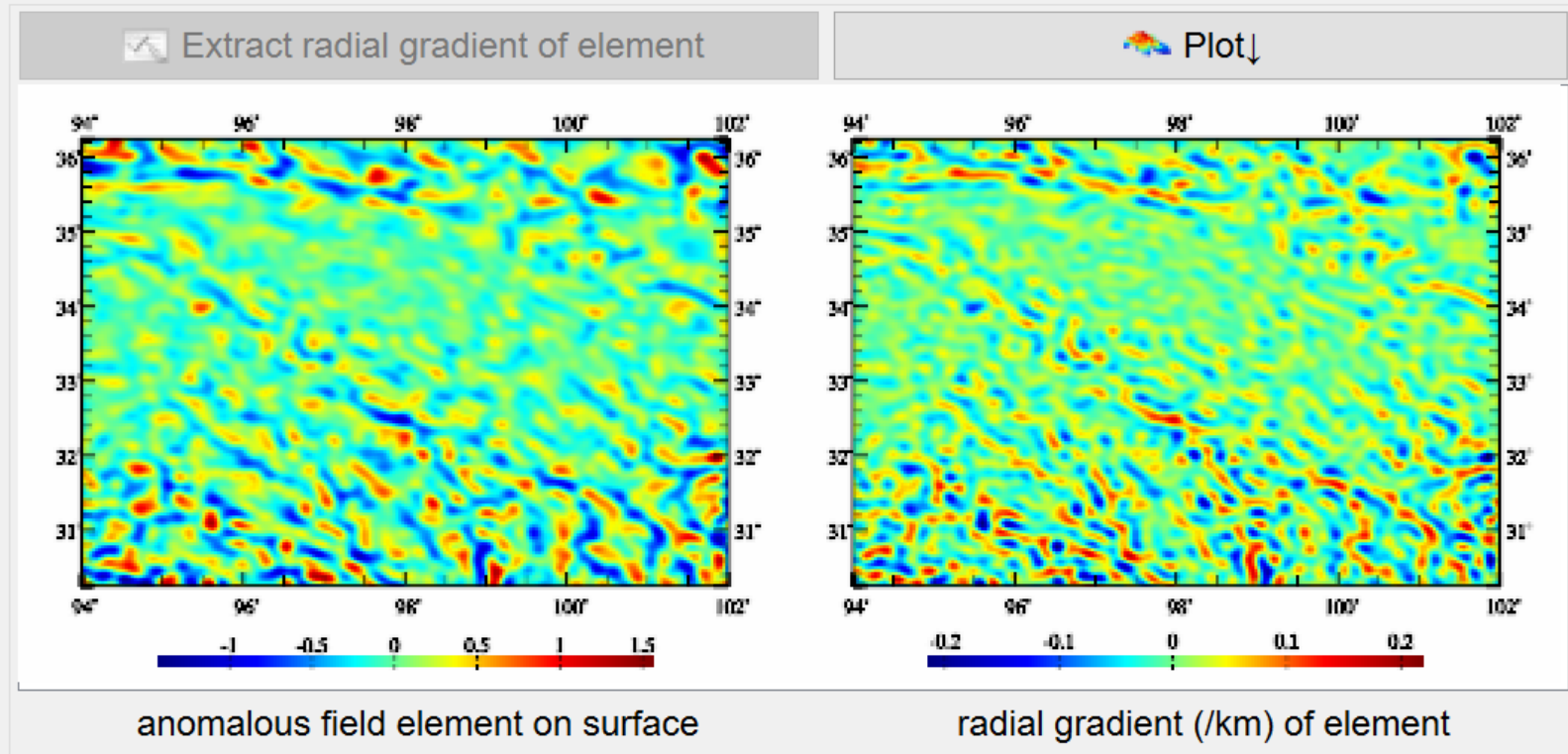
>> Complete the computation!

>> Computation end time: 2024-09-24 11:12:48

Save computation process as

Integral radius 120 km Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
0.0400	0.0328	0.0240	0.0142	0.0038	-0.0069
-0.0688	-0.0663	-0.0637	-0.0617	-0.0608	-0.0612
-0.0857	-0.0891	-0.0935	-0.0989	-0.1046	-0.1097
0.0182	0.0393	0.0565	0.0688	0.0758	0.0774
0.0011	-0.0004	-0.0007	-0.0002	0.0005	0.0010
-0.0504	-0.0517	-0.0487	-0.0409	-0.0283	-0.0119
-0.0393	-0.0745	-0.1071	-0.1333	-0.1497	-0.1542
0.1109	0.1033	0.0857	0.0610	0.0323	0.0029
-0.0338	-0.0252	-0.0187	-0.0142	-0.0119	-0.0114
-0.0577	-0.0573	-0.0535	-0.0458	-0.0346	-0.0207
-0.0108	-0.0273	-0.0417	-0.0522	-0.0578	-0.0580
0.0330	0.0372	0.0423	0.0493	0.0586	0.0704
0.1409	0.1330	0.1239	0.1145	0.1051	0.0958
-0.0367	-0.0444	-0.0469	-0.0438	-0.0353	-0.0222
0.0168	-0.0040	-0.0257	-0.0469	-0.0657	-0.0814
-0.0545	-0.0390	-0.0212	-0.0016	0.0194	0.0411
0.0536	0.0318	0.0109	-0.0075	-0.0218	-0.0315



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.
The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external gravity disturbance from disturbing gravity gradient

Save as Import parameters Start computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Open the ellipsoidal height grid file of the equipotential surface
 Open residual disturbing gradient grid file on the equipotential surface
 Select calculation point file format

 Open the calculation point file on the equipotential surface
 Set input point file format
 number of rows of file header

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential boundary surface and residual disturbing gravity gradient (E, radial) grid on the surface, compute the residual gravity disturbance (mGal) on or outside the geoid by the numerical integral.

** Input the ellipsoidal height grid file of the equipotential surface and residual disturbing gravity gradient grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landgeoidhgt.dat.

>> Open disturbing gravity gradient grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/resGMLgeoid541_1800.grr.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/Intgendistgradient/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the gravity disturbance as C:/PAGravf4.5_win64en/examples/Intgendistgradient/grrtorgadbm.txt.

>> Behind the input calculation point file record, appends a column of residual gravity disturbance, and keeps four significant digits.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

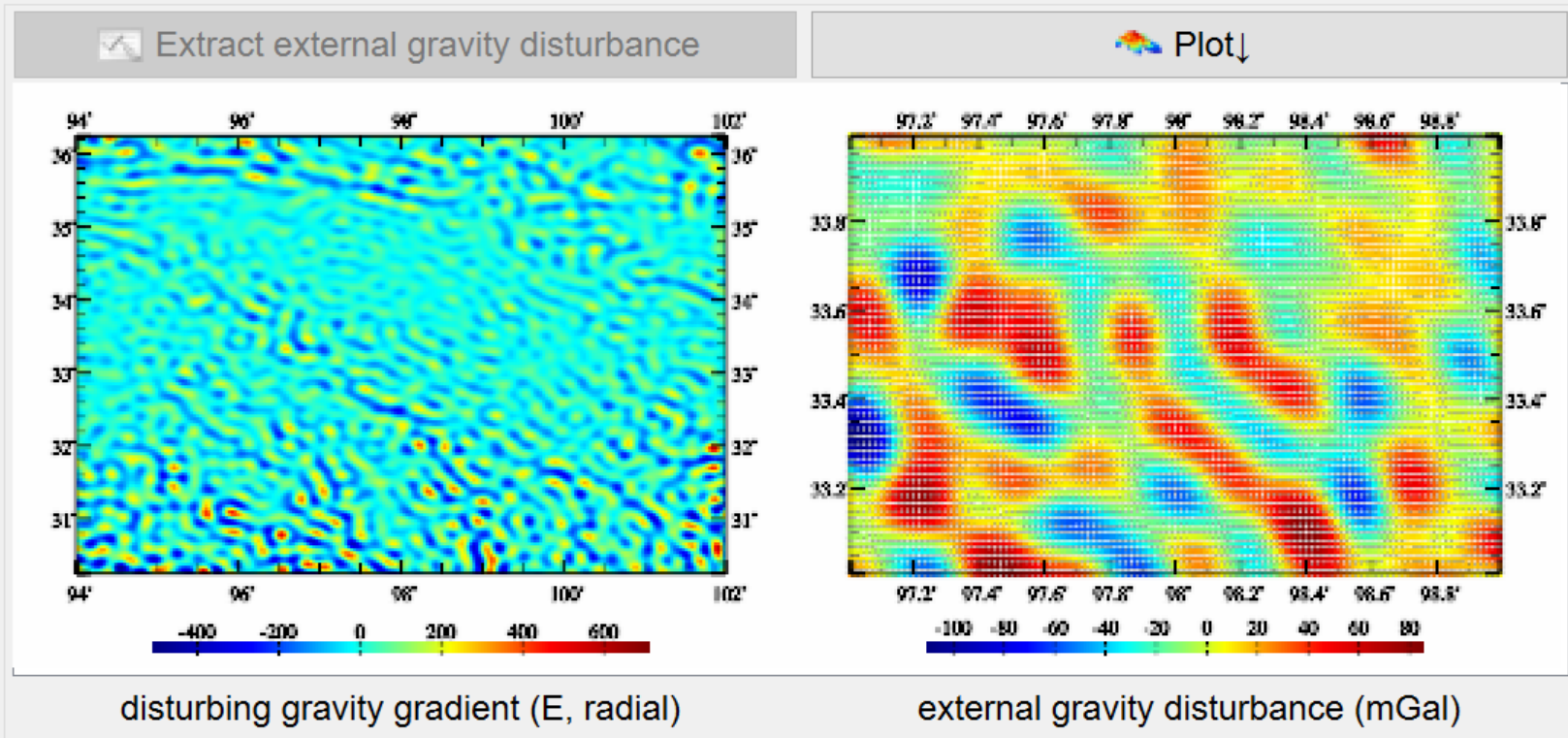
>> Computation start time: 2024-09-24 11:16:45

>> Complete the computation!

>> Computation end time: 2024-09-24 11:17:30

Integral radius

no	lon(degree/decimal)	lat	ellipHeight (m)	
1	97.008333	33.008333	3942.764	22.6149
2	97.025000	33.008333	3989.787	22.6235
3	97.041667	33.008333	4034.817	20.9473
4	97.058333	33.008333	4070.847	17.5408
5	97.075000	33.008333	4106.877	12.4745
6	97.091667	33.008333	4119.913	5.9244
7	97.108333	33.008333	4115.946	-1.8431
8	97.125000	33.008333	4090.977	-10.4866
9	97.141667	33.008333	4070.007	-19.5993
10	97.158333	33.008333	3991.047	-28.7201
11	97.175000	33.008333	3985.070	-37.3472
12	97.191667	33.008333	3956.107	-44.9479
13	97.208333	33.008333	3965.137	-50.9812
14	97.225000	33.008333	3964.173	-54.9269
15	97.241667	33.008333	3983.205	-56.3203
16	97.258333	33.008333	3953.251	-54.7987
17	97.275000	33.008333	4016.279	-50.1460
18	97.291667	33.008333	4054.318	-42.3364



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external gravity disturbance from disturbing gravity gradient

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Open the ellipsoidal height grid file of the equipotential surface
 Open residual disturbing gradient grid file on the equipotential surface
 Select calculation point file format

 Open the ellipsoidal height grid file of the calculation surface

>> Computation Process ** Operation Prompts

** Look at the file information in the window below, set the input file format parameters...

>> Save the gravity disturbance as C:/PAGrav4.5_win64en/examples/Intgendistgradient/grrtorgadbm.txt.

>> Behind the input calculation point file record, appends a column of residual gravity disturbance, and keeps four significant digits.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 11:16:45

>> Complete the computation!

>> Computation end time: 2024-09-24 11:17:30

>> Open the ellipsoidal height grid file of the calculation surface C:/PAGrav4.5_win64en/examples/Intgendistgradient/landbmsurfhgt.dat.

>> Save the gravity disturbance as C:/PAGrav4.5_win64en/examples/Intgendistgradient/grrtorgadbm.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 11:18:55

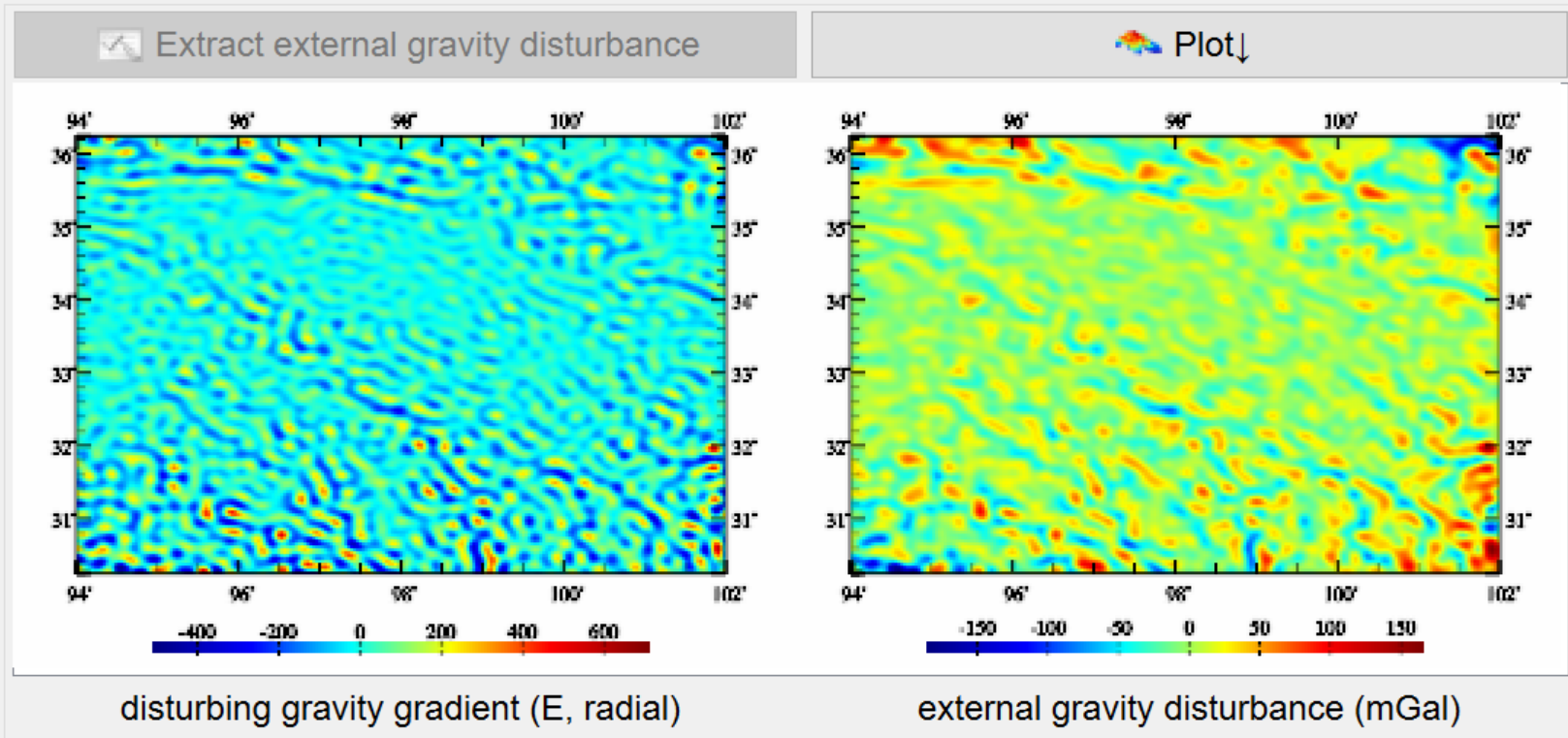
>> Complete the computation!

>> Computation end time: 2024-09-24 11:33:37

Save computation process as

Integral radius
 Save the results as
 Import setting parameters

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-5.4909	-6.4631	-8.5821	-11.7865	-15.6321	-19.85
-48.0048	-47.6351	-46.4747	-44.8593	-43.2903	-41.71
-101.2762	-109.7248	-117.7312	-123.8692	-127.9094	-131.70
-148.8079	-151.8567	-152.3336	-146.9276	-136.2635	-123.03
41.7051	49.2578	53.6431	56.2174	57.0286	54.74
-41.2681	-51.9621	-61.8403	-69.4929	-76.4285	-81.21
23.8710	36.8403	47.6062	54.4733	57.0010	57.05
-51.5814	-47.2451	-38.7297	-27.8056	-15.6015	-4.54
-7.7964	-12.6661	-16.4324	-18.9854	-20.3489	-20.49
-2.8810	-2.4568	-2.4804	-2.9259	-3.5347	-4.01
35.0115	37.7838	38.0756	36.0699	31.3534	24.23
-52.4301	-47.7452	-41.8967	-35.5431	-28.7790	-22.76
34.0699	39.2253	43.5772	46.8551	48.5496	48.48
1.9419	-1.9419	-5.4733	-8.6848	-11.5458	-13.95
11.3998	16.6768	20.7352	23.4826	24.5368	23.73
-58.0468	-64.7971	-69.1522	-71.2812	-72.4016	-71.62
-12.4080	-8.9217	-7.0164	-6.4471	-6.9306	-8.11



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of disturbing gravity gradient by inverse operation integral

Save as Import parameters Start Computation Save process Follow example

Select calculation point file format

discrete calculation point file

Set input point file format

number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the equipotential surface and residual gravity disturbance (mGal) grid on the surface, compute the residual disturbing gravity gradient (E, radial) on the surface by the inverse operation integral.

** Input the ellipsoidal height grid file of the equipotential surface and residual gravity disturbance grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landgeoidhgt.dat.

>> Open the gravity disturbance grid file on the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/resGMLgeoid541_1800.rga.

>> Open the calculation point file on the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save disturbing gravity gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrrdwm.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual disturbing gravity gradient.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

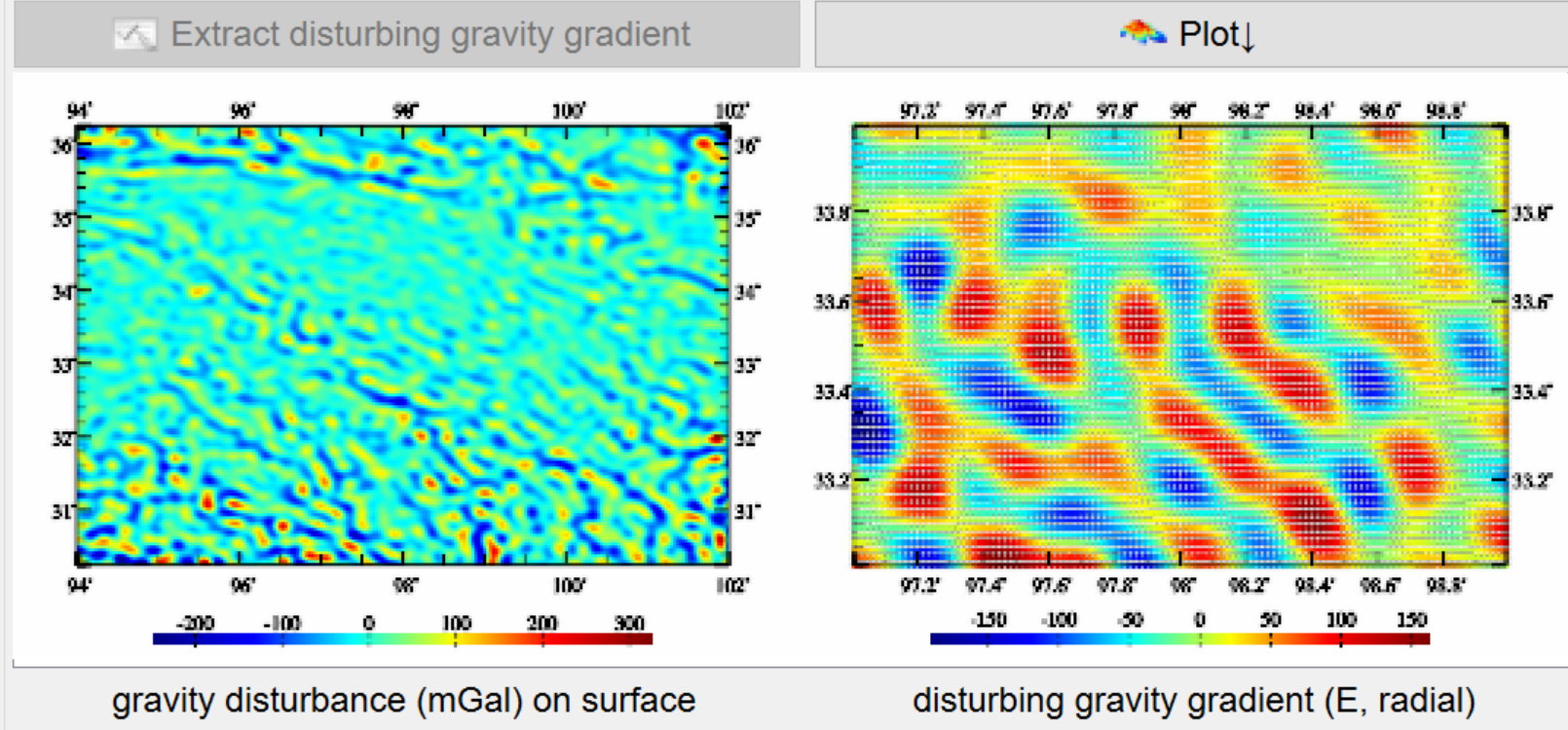
>> Computation start time: 2024-09-24 11:36:04

>> Complete the computation!

Integral radius 120 km

no	lon(degree/decimal)	lat	ellipHeight (m)		
1	97.008333	33.008333	3942.764	-37.2501	78.0127
2	97.025000	33.008333	3989.787	-37.2203	78.1982
3	97.041667	33.008333	4034.817	-37.1899	73.5460
4	97.058333	33.008333	4070.847	-37.1590	64.0699
5	97.075000	33.008333	4106.877	-37.1276	50.1369
6	97.091667	33.008333	4119.913	-37.0959	32.3982
7	97.108333	33.008333	4115.946	-37.0640	11.7263
8	97.125000	33.008333	4090.977	-37.0318	-10.8216
9	97.141667	33.008333	4070.007	-36.9990	-34.0982
10	97.158333	33.008333	3991.047	-36.9665	-56.8946
11	97.175000	33.008333	3985.070	-36.9327	-77.9552
12	97.191667	33.008333	3956.107	-36.8988	-96.0585
13	97.208333	33.008333	3965.137	-36.8642	-110.0355
14	97.225000	33.008333	3964.173	-36.8295	-118.8129
15	97.241667	33.008333	3983.205	-36.7943	-121.5105
16	97.258333	33.008333	3953.251	-36.7595	-117.5025
17	97.275000	33.008333	4016.279	-36.7238	-106.5158
18	97.291667	33.008333	4054.318	-36.6883	-88.7022

Ignore the ellipsoidal height



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of disturbing gravity gradient by inverse operation integral

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Select calculation point file format

>> Computation Process ** Operation Prompts

** Look at the file information in the window below, set the input file format parameters...

>> Save disturbing gravity gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrrdwm.txt.

>> Behind the input calculation point file record, appends a column of ellipsoidal height of the calculation point interpolated from the ellipsoidal height grid of the equipotential surface and a column of integral value of the residual disturbing gravity gradient.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 11:36:04

>> Complete the computation!

>> Computation end time: 2024-09-24 11:36:47

>> Save disturbing gravity gradient as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrrdwm.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

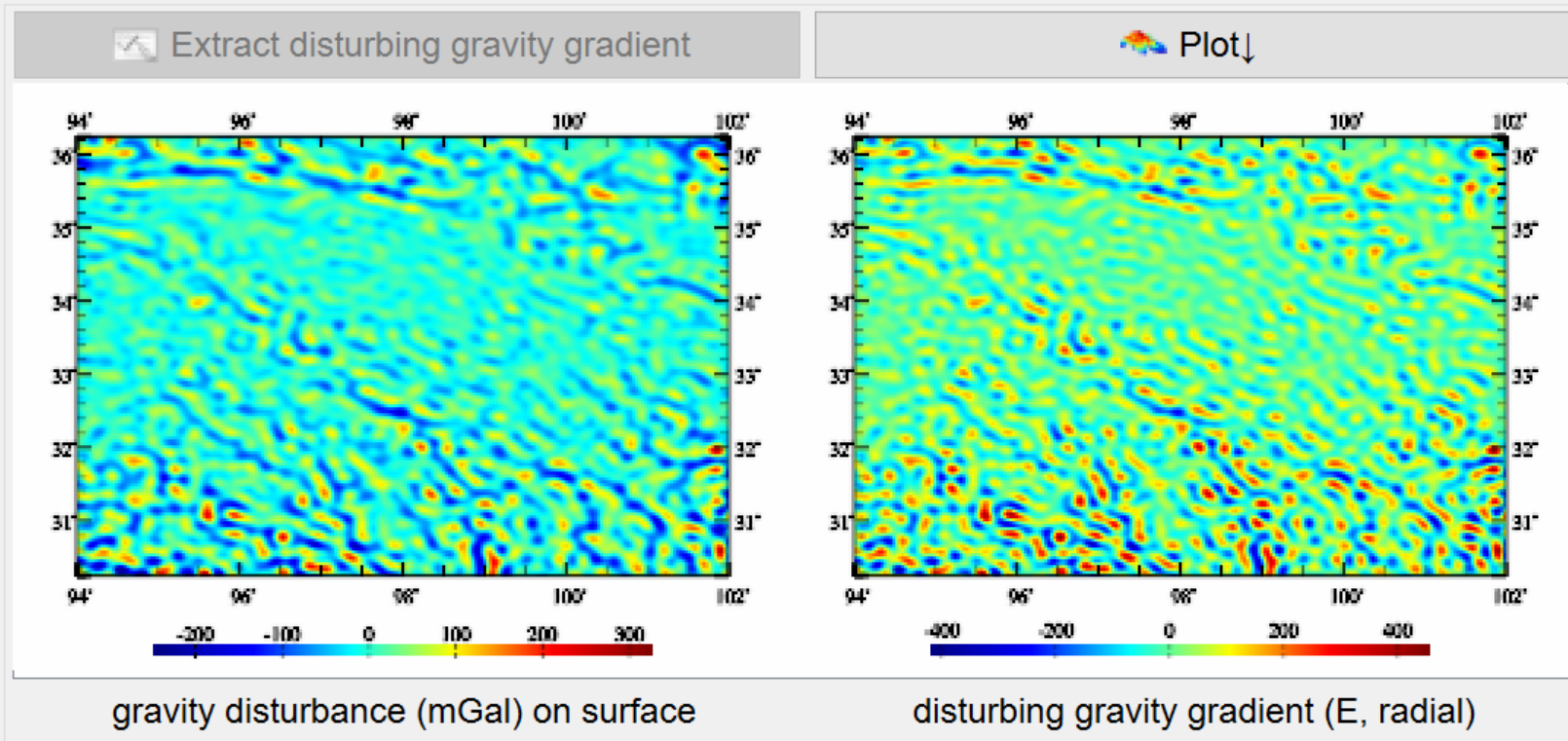
>> Computation start time: 2024-09-24 11:39:12

>> Complete the computation!

>> Computation end time: 2024-09-24 11:52:56

Integral radius

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
-112.9508	-100.5689	-86.2807	-70.0350	-52.3943	-33.13
100.5612	94.8312	89.0615	84.9566	83.7303	85.91
148.3945	156.5703	167.8025	181.6957	196.9110	211.24
-82.3655	-130.7107	-168.9299	-194.7092	-207.1051	-206.56
-19.2439	-19.3484	-22.6509	-27.9468	-33.9816	-39.49
78.8567	89.5537	90.5251	79.9201	57.2490	23.71
63.1468	147.8592	228.7399	296.4236	342.6878	361.58
-204.1974	-185.9357	-145.8509	-90.3037	-26.9057	36.56
62.7685	40.9181	23.6119	10.8818	2.2801	-2.78
88.2194	92.8901	89.1706	75.8932	53.1062	22.23
-40.4884	-4.3659	27.5326	51.2541	64.1525	65.23
-79.6335	-78.5558	-80.3205	-87.2888	-100.8419	-121.12
-246.8885	-228.8089	-209.8435	-191.5598	-174.7083	-159.11
116.3989	134.4200	139.7425	130.9599	108.2413	73.42
-77.8705	-33.6482	13.0742	58.2786	98.6038	131.66
103.9993	78.5124	48.1730	13.0325	-26.0951	-67.53
-74.0066	-28.4254	13.5757	47.9650	71.7441	83.31



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external disturbing gravity gradient from gravity disturbance

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Select calculation point file format

discrete calculation point file

Set input point file format

number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the boundary surface and the residual anomalous gravity field element grid on the surface, compute the residual anomalous gravity field element on or outside the geoid by the Poisson integral. The Poisson integral is the solution of the first boundary value problem in the mathematical sense, and the boundary surface need be not an equipotential surface.

** Input the ellipsoidal height grid file of the boundary surface and residual gravity disturbance grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landgeoidhgt.dat.

>> Open the gravity disturbancet grid file on the boundary surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/resGMIgeoid541_1800.rga.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/Intgendistgradient/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrdbm.txt.

>> Behind the input calculation point file record, appends a column of residual disturbing gravity gradient, and keeps 4 significant digits.

>> The parameter settings have been entered into the system!

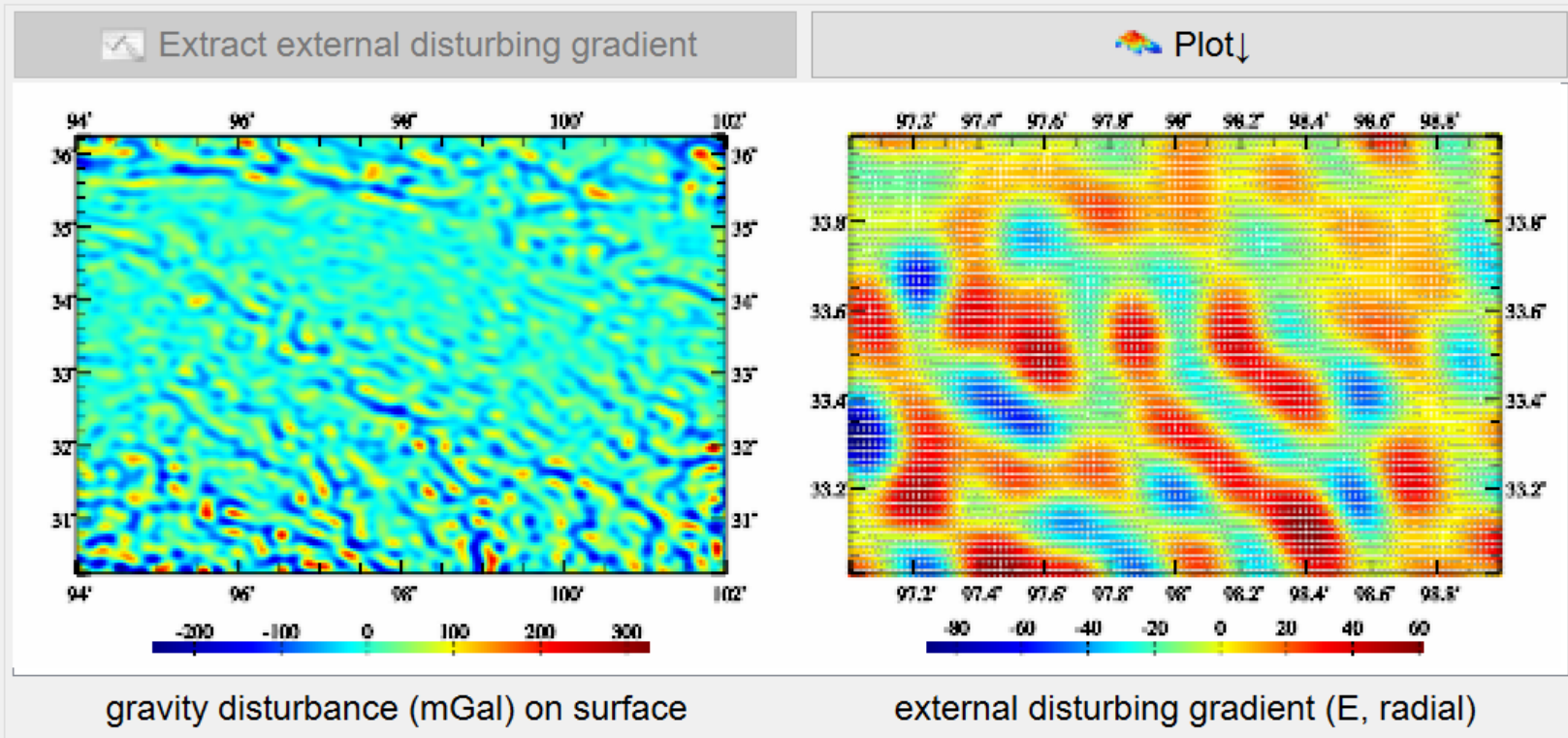
** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 12:40:10

>> Complete the computation!

Integral radius 120 km

no	lon(degree/decimal)	lat	ellipHeight (m)	
1	97.008333	33.008333	3942.764	25.9295
2	97.025000	33.008333	3989.787	25.7579
3	97.041667	33.008333	4034.817	23.9132
4	97.058333	33.008333	4070.847	20.4859
5	97.075000	33.008333	4106.877	15.5549
6	97.091667	33.008333	4119.913	9.4470
7	97.108333	33.008333	4115.946	2.3353
8	97.125000	33.008333	4090.977	-5.5390
9	97.141667	33.008333	4070.007	-13.8461
10	97.158333	33.008333	3991.047	-22.4698
11	97.175000	33.008333	3985.070	-30.3218
12	97.191667	33.008333	3956.107	-37.3873
13	97.208333	33.008333	3965.137	-42.6330
14	97.225000	33.008333	3964.173	-46.0654
15	97.241667	33.008333	3983.205	-46.9850
16	97.258333	33.008333	3953.251	-45.9626
17	97.275000	33.008333	4016.279	-41.2274
18	97.291667	33.008333	4054.318	-34.2891



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of external disturbing gravity gradient from gravity disturbance

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Open the ellipsoidal height grid file of the boundary surface
 Open the gravity disturbance grid file on the boundary surface
 Select calculation point file format

 Open the ellipsoidal height grid file of the calculation surface

>> Computation Process ** Operation Prompts

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrdbm.txt.

>> Behind the input calculation point file record, appends a column of residual disturbing gravity gradient, and keeps 4 significant digits.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 12:40:10

>> Complete the computation!

>> Computation end time: 2024-09-24 12:41:33

>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landbmsurfhgt.dat.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/rgatogrdbm.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 12:42:52

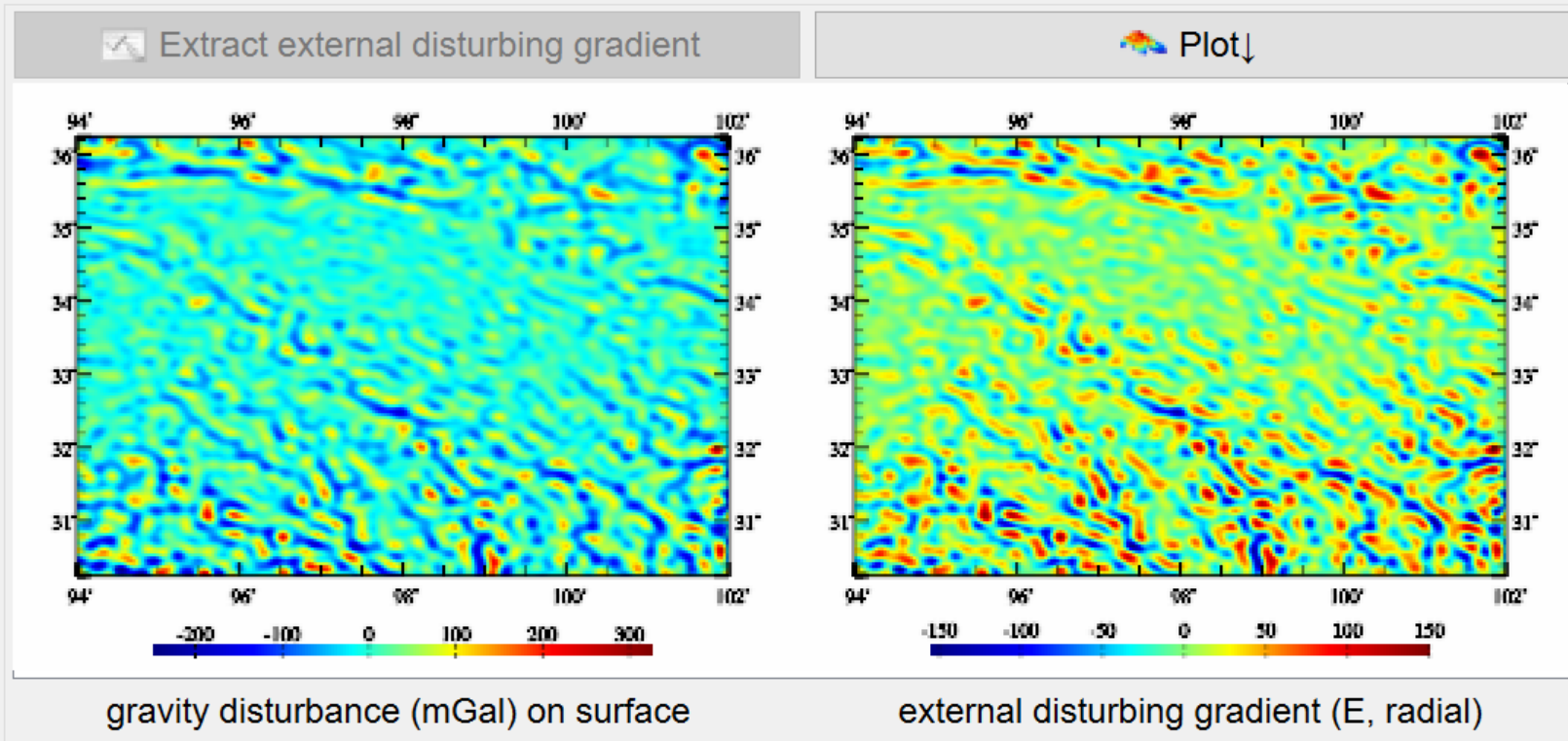
>> Complete the computation!

>> Computation end time: 2024-09-24 13:10:17

Save computation process as

Integral radius
 Save the results as
 Import setting parameters

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
14.6051	17.5215	18.0702	17.4698	16.3007	14.99
20.9381	23.0694	25.6901	28.3122	30.5699	33.43
-2.7578	-10.4204	-14.1851	-15.2348	-13.6703	-7.62
-75.0731	-93.2156	-108.3839	-115.8375	-115.1837	-109.98
50.2266	54.0463	54.9180	53.5865	50.2999	45.38
-11.7013	-16.9682	-22.7388	-29.9474	-37.8645	-46.80
54.9276	75.7649	92.8410	103.4299	106.5498	105.51
-83.8409	-75.3493	-59.6411	-40.0281	-18.8092	-0.10
10.4136	4.9826	0.7599	-2.1680	-3.9809	-4.83
10.0486	10.9698	11.1755	9.7821	7.4297	4.47
42.3009	49.1534	52.8730	53.1980	49.5080	42.01
-67.1126	-64.2747	-60.7099	-57.4379	-54.6517	-53.89
-27.1247	-22.3809	-16.8609	-12.6879	-8.9451	-6.13
10.7742	12.1184	11.5347	8.7999	4.0323	-2.10
11.3436	22.6686	32.2028	39.4727	44.0296	45.78
-20.5958	-26.0426	-31.3601	-36.5253	-42.2897	-48.51
-19.6726	-8.7585	-0.2185	5.7385	8.9329	9.66



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of Poisson integral on external anomalous gravity field element

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element Computation of external gravity disturbance from disturbing gravity gradient Computation of disturbing gravity gradient by inverse operation integral Computation of external disturbing gravity gradient from gravity disturbance **Computation of Poisson integral on external anomalous field element**

Open the ellipsoidal height grid file of the boundary surface

Open the anomalous field element grid file on the boundary surface

Select calculation point file format
discrete calculation point file

Open the calculation point position file

Set input point file format
number of rows of file header 1

>> Computation Process ** Operation Prompts

>> [Function] From the ellipsoidal height grid of the boundary surface and residual gravity disturbance grid (mGal) on the surface, compute the residual disturbing gravity gradient (E, radial) on or outside the geoid. The inverse integral of gravity disturbance adopts the combination algorithm with Poisson integral and differentiation, which does not require that the boundary surface should be a gravity equipotential surface.

** Input the ellipsoidal height grid of the boundary surface and residual anomalous gravity field element grid file on the surface with the same grid specification...

>> Open the ellipsoidal height grid file of the boundary surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landgeoidhgt.dat.

>> Open anomalous field element grid file on the boundary surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/resGMIgeoid541_1800.ksi.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/Intgendistgradient/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save Poisson integral results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/possonksi.txt.

>> Behind the input calculation point file record, appends a column of Poisson integral value, and keeps 4 significant digits.

>> The parameter settings have been entered into the system!

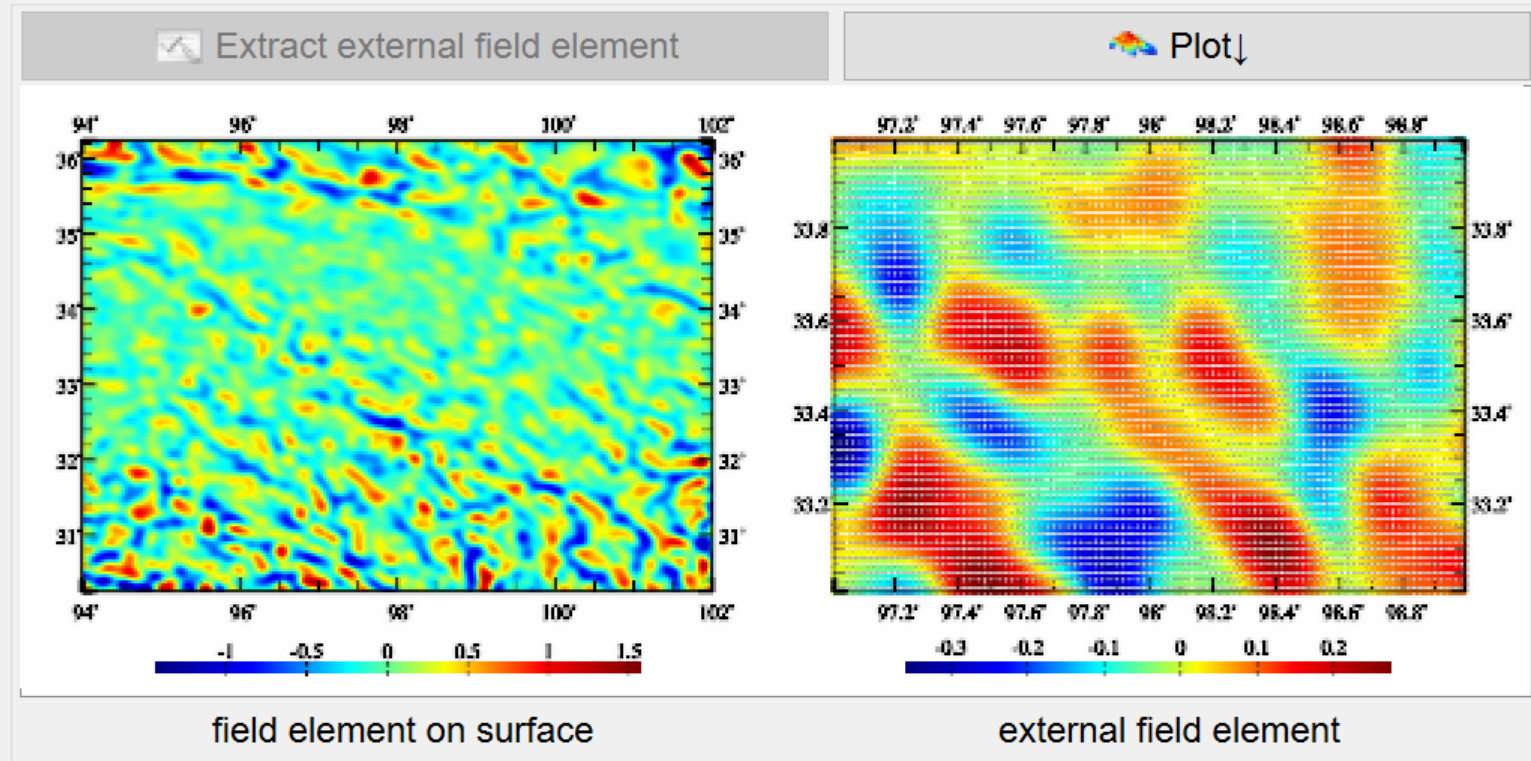
** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 11:57:56

Save computation process as

Integral radius 120 km Save the results as Import setting parameters Start Computation

no	lon(degree/decimal)	lat	ellipHeight (m)	
1	97.008333	33.008333	3942.764	-0.0249
2	97.025000	33.008333	3989.787	-0.0297
3	97.041667	33.008333	4034.817	-0.0365
4	97.058333	33.008333	4070.847	-0.0451
5	97.075000	33.008333	4106.877	-0.0555
6	97.091667	33.008333	4119.913	-0.0673
7	97.108333	33.008333	4115.946	-0.0803
8	97.125000	33.008333	4090.977	-0.0941
9	97.141667	33.008333	4070.007	-0.1079
10	97.158333	33.008333	3991.047	-0.1218
11	97.175000	33.008333	3985.070	-0.1332
12	97.191667	33.008333	3956.107	-0.1424
13	97.208333	33.008333	3965.137	-0.1472
14	97.225000	33.008333	3964.173	-0.1477
15	97.241667	33.008333	3983.205	-0.1421
16	97.258333	33.008333	3953.251	-0.1316
17	97.275000	33.008333	4016.279	-0.1126
18	97.291667	33.008333	4054.318	-0.0878



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Computation of Poisson integral on external anomalous gravity field element

Save as Import parameters Start Computation Save process Follow example

Operation of radial gradient integral on anomalous gravity field element
 Computation of external gravity disturbance from disturbing gravity gradient
 Computation of disturbing gravity gradient by inverse operation integral
 Computation of external disturbing gravity gradient from gravity disturbance
 Computation of Poisson integral on external anomalous field element

Open the ellipsoidal height grid file of the boundary surface
 Open the anomalous field element grid file on the boundary surface
 Select calculation point file format
 ellipsoidal height grid file
 Open the ellipsoidal height grid file of the calculation surface

>> Computation Process ** Operation Prompts

>> Save Poisson integral results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/possonksi.txt.
 >> Behind the input calculation point file record, appends a column of Poisson integral value, and keeps 4 significant digits.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-24 11:57:56
 >> Complete the computation!
 >> Computation end time: 2024-09-24 11:58:39

>> Open the ellipsoidal height grid file of the calculation surface C:/PAGravf4.5_win64en/examples/Intgendistgradient/landbmsurfhgt.dat.
 ** Look at the file information in the window below, set the input file format parameters...

>> Save Poisson integral results as C:/PAGravf4.5_win64en/examples/Intgendistgradient/possonksi.dat.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

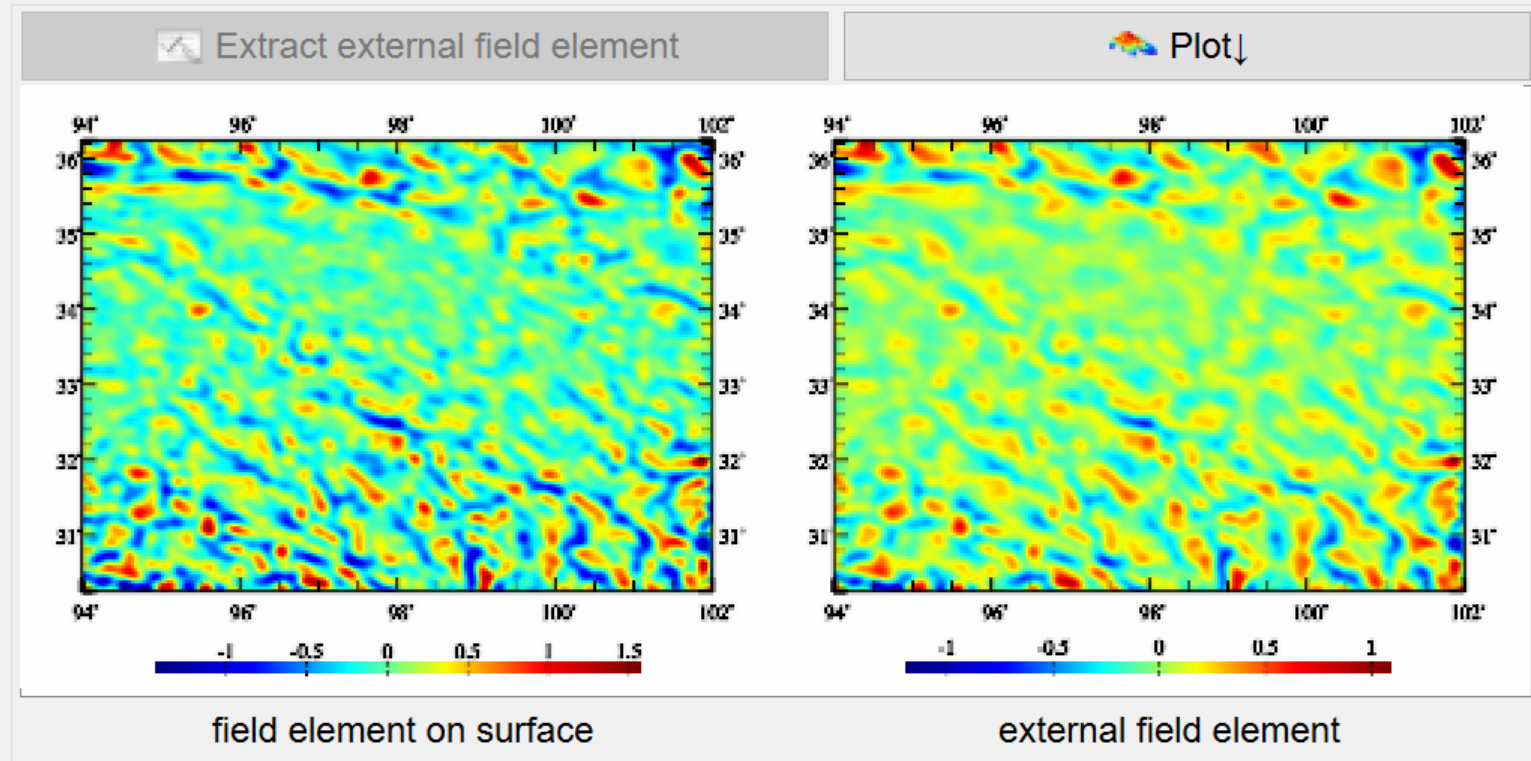
>> Computation start time: 2024-09-24 12:02:31
 >> Complete the computation!
 >> Computation end time: 2024-09-24 12:16:41

Save computation process as

Integral radius 120 km

Save the results as Import setting parameters Start Computation

94.000000	102.000000	30.250000	36.250000	0.01666667	0.01666667
0.3283	0.3516	0.3557	0.3454	0.3266	0.3029
0.0801	0.0710	0.0679	0.0696	0.0741	0.0810
-0.3085	-0.3635	-0.4051	-0.4321	-0.4459	-0.4514
-1.0346	-1.1190	-1.1757	-1.1896	-1.1583	-1.0882
0.5155	0.6084	0.6724	0.7119	0.7284	0.7189
-0.0396	-0.1417	-0.2460	-0.3482	-0.4471	-0.5346
0.5164	0.7299	0.9093	1.0347	1.0939	1.0872
-0.6194	-0.5895	-0.5028	-0.3759	-0.2243	-0.0702
0.1364	0.0800	0.0310	-0.0087	-0.0388	-0.0601
-0.0306	-0.0352	-0.0469	-0.0662	-0.0903	-0.1156
0.3409	0.4104	0.4527	0.4630	0.4370	0.3761
-0.4895	-0.4688	-0.4373	-0.4023	-0.3679	-0.3410
-0.0821	-0.0393	-0.0001	0.0306	0.0517	0.0622
0.0534	0.0552	0.0489	0.0331	0.0082	-0.0232
0.2543	0.3460	0.4259	0.4880	0.5265	0.5386
-0.2457	-0.3323	-0.4132	-0.4886	-0.5612	-0.6270
-0.2904	-0.1767	-0.0722	0.0170	0.0875	0.1375



The radial gradient integral algorithm of anomalous field element is derived from the solution of Stokes boundary value problem, which requires the integrand field elements to be on the equipotential surface. The Poisson integral is the solution of the first boundary value problem, and the boundary surface is not required to be an equipotential surface.

The equipotential surface can be constructed from a global geopotential model (not greater than 360 degrees), which can also be represent by a normal (orthometric) equiheight surface with the altitude of not more than ten kilometers.

Spatial and spectral performance analysis of spherical radial basis functions

Calculation and save Extract plot data Follow example Save plot

Spatial and spectral performance analysis of spherical radial basis functions

Reuter spherical network construction with given level

Select anomalous field element **gravity disturbance**

Algorithms of the spherical radial basis function and Reuter grid



Save computation process as

[SRBFs] The point mass kernel, Poisson kernel, m-order radial multipole and m-order Poisson wavelet kernel functions

specified latitude and longitude range, to design the SRBF network and corresponding approach algorithm of gravity field. The program does not require an input file.

>> Select the function module from the two control buttons at the top left of the interface...

>> Save the results as C:/PAGrav4.5_win64en/examples/SRBFperformance/rgaSRBF.txt.

>> The program output four kinds of SRBF spatial curve calculation results of the given type of gravity field element. Record format: spherical angular distance (independent variable), point mass kernel function value, Poisson kernel function value, m-order radial multipole kernel function value and m-order Poisson wavelet kernel function value.

** At the same time, the program outputs the spectral domain curve file *.dgr of four SRBF of the given type of gravity field element into the current directory, where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.

Set SRBF parameters

minimum degree

maximum degree

burial depth of Bjerhammar sphere

order

action distance of SBRF center

spatial interval

Calculation and save

Display of the input-output file ↓

1.446667	-0.004675	-0.006049	-0.008050	-0.017435
1.450000	-0.004839	-0.006275	-0.008335	-0.017861
1.453333	-0.004972	-0.006457	-0.008560	-0.018159
1.456667	-0.005075	-0.006593	-0.008723	-0.018330
1.460000	-0.005147	-0.006683	-0.008825	-0.018372
1.463333	-0.005188	-0.006726	-0.008864	-0.018285
1.466667	-0.005197	-0.006723	-0.008840	-0.018072
1.470000	-0.005174	-0.006674	-0.008755	-0.017735
1.473333	-0.005120	-0.006579	-0.008609	-0.017276
1.476667	-0.005037	-0.006440	-0.008404	-0.016700
1.480000	-0.004923	-0.006257	-0.008142	-0.016012
1.483333	-0.004781	-0.006032	-0.007824	-0.015217
1.486667	-0.004611	-0.005768	-0.007454	-0.014321
1.490000	-0.004416	-0.005466	-0.007034	-0.013332
1.493333	-0.004195	-0.005128	-0.006567	-0.012256
1.496667	-0.003952	-0.004758	-0.006058	-0.011102
1.500000	-0.003689	-0.004357	-0.005509	-0.009878

Curve type **Spatial curves of SRBFs**

Line thickness

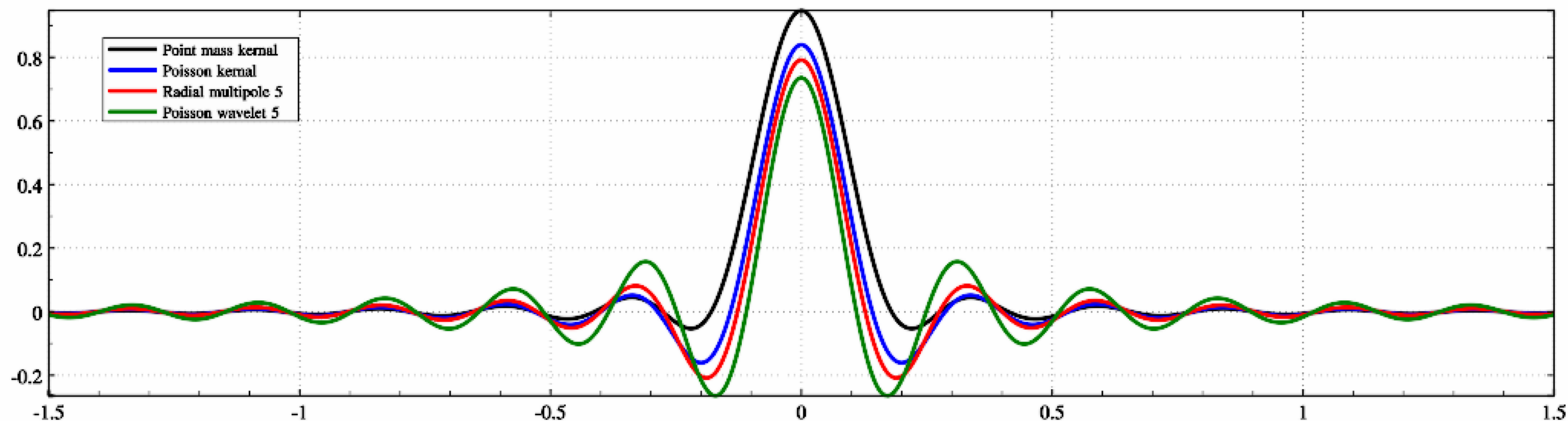
Start end row number

Extract plot data

Chart plot ↓

Spatial and spectral curves of spherical radial basis functions (SRBF)

Save current plot as



Spatial and spectral performance analysis of spherical radial basis functions

Spatial and spectral performance analysis of spherical radial basis functions

Reuter spherical network construction with given level

Select anomalous field element **gravity disturbance**

Algorithms of the spherical radial basis function and Reuter grid
PAGrav4.5
 Chinese Academy of Surveying & Mapping
 October 2024, Beijing, China

Save computation process as

[SRBFs] The point mass kernel, Poisson kernel, m-order radial multipole and m-order Poisson wavelet kernel functions

Set SRBF parameters

minimum degree 30

maximum degree 1440

burial depth of Bjerhammar sphere 5km

order 5

action distance of SBRF center 1.5°

spatial interval 0.20'

Display of the input-output file ↓

1424	0.991387	0.980618	0.958923	0.876948
1425	0.991223	0.981833	0.961462	0.884220
1426	0.991058	0.983047	0.964004	0.891546
1427	0.990892	0.984261	0.966550	0.898927
1428	0.990725	0.985475	0.969100	0.906362
1429	0.990557	0.986688	0.971653	0.913853
1430	0.990388	0.987900	0.974211	0.921399
1431	0.990219	0.989112	0.976773	0.929001
1432	0.990048	0.990324	0.979338	0.936660
1433	0.989876	0.991536	0.981907	0.944375
1434	0.989704	0.992746	0.984480	0.952147
1435	0.989531	0.993957	0.987057	0.959977
1436	0.989356	0.995167	0.989638	0.967864
1437	0.989181	0.996376	0.992223	0.975810
1438	0.989005	0.997585	0.994811	0.983814
1439	0.988828	0.998794	0.997404	0.991877
1440	0.988650	1.000002	1.000000	1.000000

specified latitude and longitude range, to design the SRBF network and corresponding approach algorithm of gravity field. The program does not require an input file.

>> Select the function module from the two control buttons at the top left of the interface...

>> Save the results as C:/PAGrav4.5_win64en/examples/SRBFperformance/rgaSRBF.txt.

>> The program output four kinds of SRBF spatial curve calculation results of the given type of gravity field element. Record format: spherical angular distance (independent variable), point mass kernel function value, Poisson kernel function value, m-order radial multipole kernel function value and m-order Poisson wavelet kernel function value.

** At the same time, the program outputs the spectral domain curve file *. dgr of four SRBF of the given type of gravity field element into the current directory, where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.

Calculation and save

Curve type **Spectral curves of SRBFs**

Line thickness 3

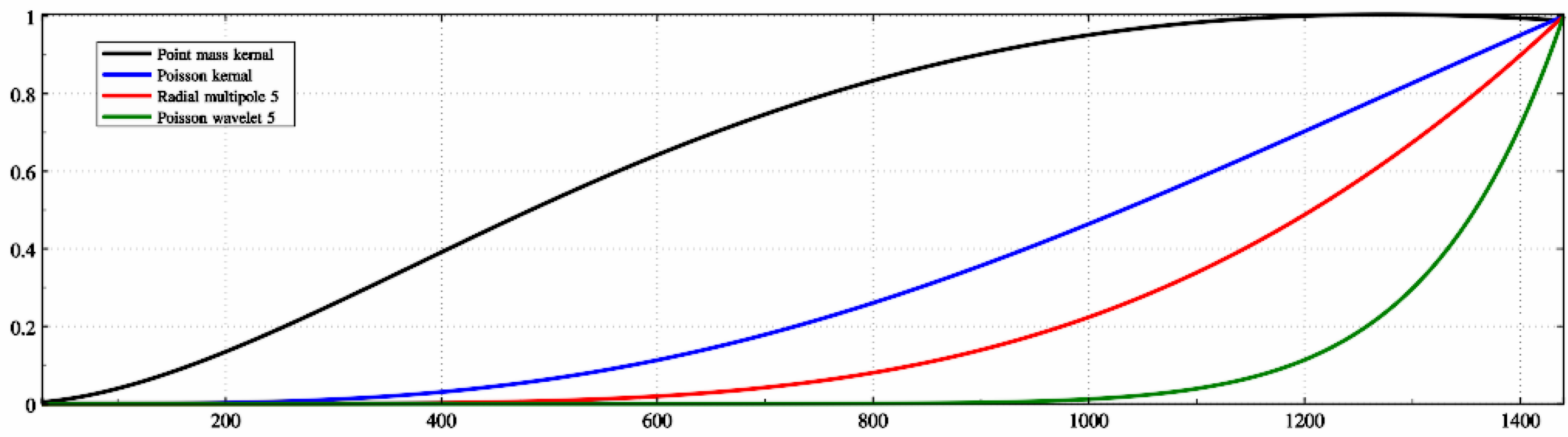
Start end row number 1 3600

Extract plot data

Chart plot ↓

Spatial and spectral curves of spherical radial basis functions (SRBF)

Save current plot as



Spatial and spectral performance analysis of spherical radial basis functions

Spatial and spectral performance analysis of spherical radial basis functions

Reuter spherical network construction with given level

Select anomalous field element **height anomaly / disturbing potential**

Algorithms of the spherical radial basis function and Reuter grid
PAGrav4.5
 Chinese Academy of Surveying & Mapping
 October 2024, Beijing, China

Save computation process as

[SRBFs] The point mass kernel, Poisson kernel, m-order radial multipole and m-order Poisson wavelet kernel functions

where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.
 >> Save the results as C:/PAGrav4.5_win64en/examples/SRBFperformance/ksiSRBF.txt.
 >> The program output four kinds of SRBF spatial curve calculation results of the given type of gravity field element. Record format: spherical angular distance (independent variable), point mass kernel function value, Poisson kernel function value, m-order radial multipole kernel function value and m-order Poisson wavelet kernel function value.
 ** At the same time, the program outputs the spectral domain curve file *.dgr of four SRBF of the given type of gravity field element into the current directory, where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.

Set SRBF parameters

minimum degree 30
 maximum degree 1440
 burial depth of Bjerhammar sphere 5km
 order 5
 action distance of SBRF center 1.5°
 spatial interval 0.20'

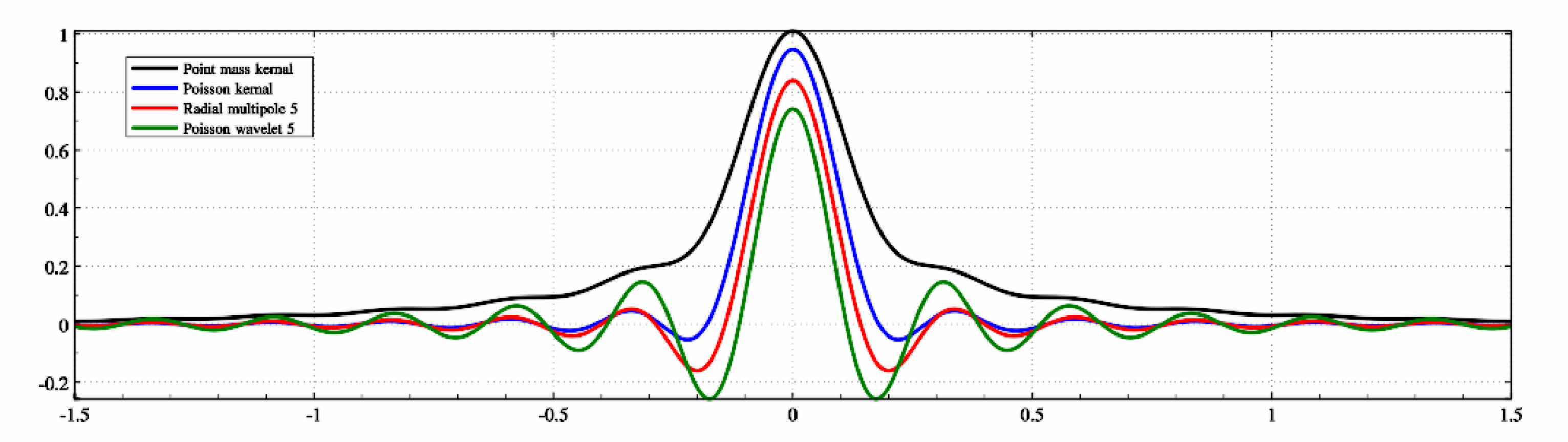
Display of the input-output file ↓

1.446667	0.010961	-0.004686	-0.006052	-0.015008
1.450000	0.010781	-0.004850	-0.006278	-0.015414
1.453333	0.010616	-0.004984	-0.006460	-0.015710
1.456667	0.010464	-0.005087	-0.006597	-0.015894
1.460000	0.010327	-0.005158	-0.006687	-0.015967
1.463333	0.010204	-0.005199	-0.006730	-0.015928
1.466667	0.010097	-0.005207	-0.006727	-0.015778
1.470000	0.010004	-0.005185	-0.006678	-0.015519
1.473333	0.009925	-0.005131	-0.006583	-0.015153
1.476667	0.009860	-0.005047	-0.006443	-0.014685
1.480000	0.009810	-0.004933	-0.006260	-0.014117
1.483333	0.009773	-0.004791	-0.006035	-0.013455
1.486667	0.009749	-0.004622	-0.005771	-0.012703
1.490000	0.009738	-0.004426	-0.005468	-0.011868
1.493333	0.009738	-0.004205	-0.005130	-0.010955
1.496667	0.009749	-0.003962	-0.004759	-0.009972
1.500000	0.009770	-0.003698	-0.004359	-0.008927

Curve type **Spatial curves of SRBFs** | Line thickness 3 | Start end row number 1 3600

Extract plot data | Chart plot ↓

Spatial and spectral curves of spherical radial basis functions (SRBF) | Save current plot as



Spatial and spectral performance analysis of spherical radial basis functions



Spatial and spectral performance analysis of spherical radial basis functions

Reuter spherical network construction with given level

Select anomalous field element **height anomaly / disturbing potential**

Algorithms of the spherical radial basis function and Reuter grid

Save computation process as

[SRBFs] The point mass kernel, Poisson kernel, m-order radial multipole and m-order Poisson wavelet kernel functions

where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.

>> Save the results as C:/PAGrav4.5_win64en/examples/SRBFperformance/ksiSRBF.txt.

>> The program output four kinds of SRBF spatial curve calculation results of the given type of gravity field element. Record format: spherical angular distance (independent variable), point mass kernel function value, Poisson kernel function value, m-order radial multipole kernel function value and m-order Poisson wavelet kernel function value.

** At the same time, the program outputs the spectral domain curve file *.dgr of four SRBF of the given type of gravity field element into the current directory, where * is the output file name. Record format: SRBF Legendre expansion degree (independent variable), point mass kernel degree variance, Poisson kernel degree variance, m-order radial multipole kernel degree variance and m-order Poisson wavelet kernel degree variance.

Set SRBF parameters

minimum degree 30

maximum degree 1440

burial depth of Bjerhammar sphere 5km

order 5

action distance of SBRF center 1.5°

spatial interval 0.20'

Display of the input-output file ↓

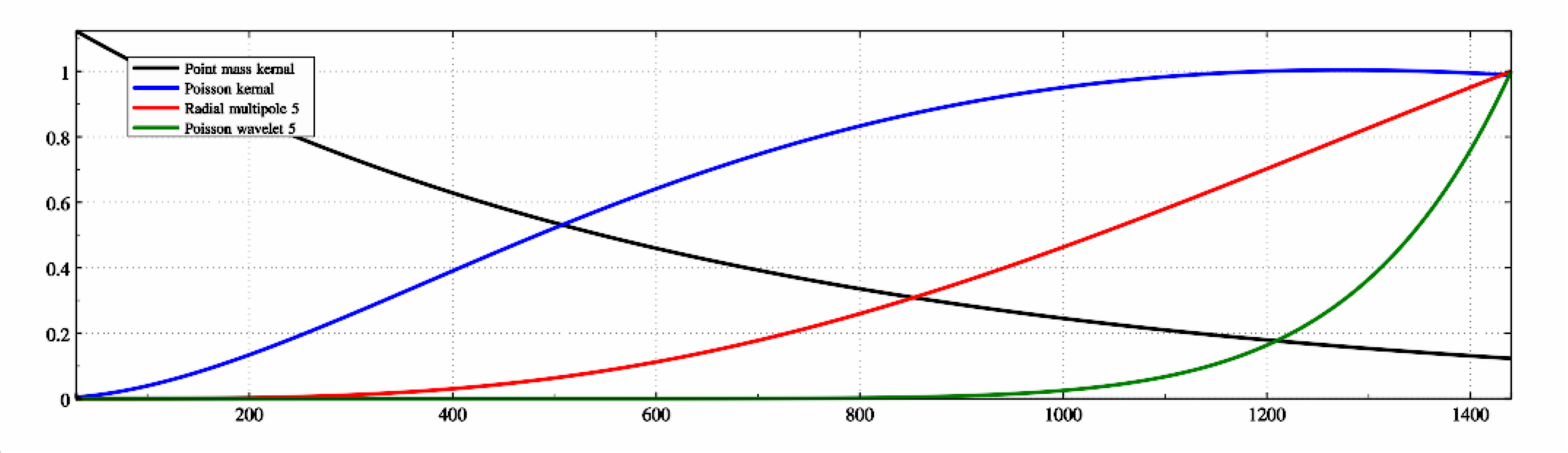
1424	0.126130	0.991339	0.980579	0.896752
1425	0.125932	0.991175	0.981797	0.902920
1426	0.125735	0.991011	0.983013	0.909126
1427	0.125538	0.990846	0.984230	0.915368
1428	0.125341	0.990679	0.985446	0.921648
1429	0.125145	0.990512	0.986661	0.927966
1430	0.124949	0.990344	0.987876	0.934322
1431	0.124753	0.990174	0.989091	0.940715
1432	0.124557	0.990004	0.990305	0.947147
1433	0.124362	0.989833	0.991518	0.953617
1434	0.124167	0.989661	0.992732	0.960126
1435	0.123973	0.989488	0.993944	0.966674
1436	0.123778	0.989315	0.995157	0.973260
1437	0.123584	0.989140	0.996369	0.979886
1438	0.123391	0.988964	0.997580	0.986551
1439	0.123197	0.988787	0.998791	0.993256
1440	0.123004	0.988610	1.000002	1.000000

Calculation and save

Curve type **Spectral curves of SRBFs** | Line thickness 3 | Start end row number 1 3600

Extract plot data | Chart plot ↓

Spatial and spectral curves of spherical radial basis functions (SRBF) | Save current plot as



Minimum Maximum geocentric latitude

-90.0°

90.0°

Minimum Maximum longitude

0.0°

360°

Set Reuter level K 90

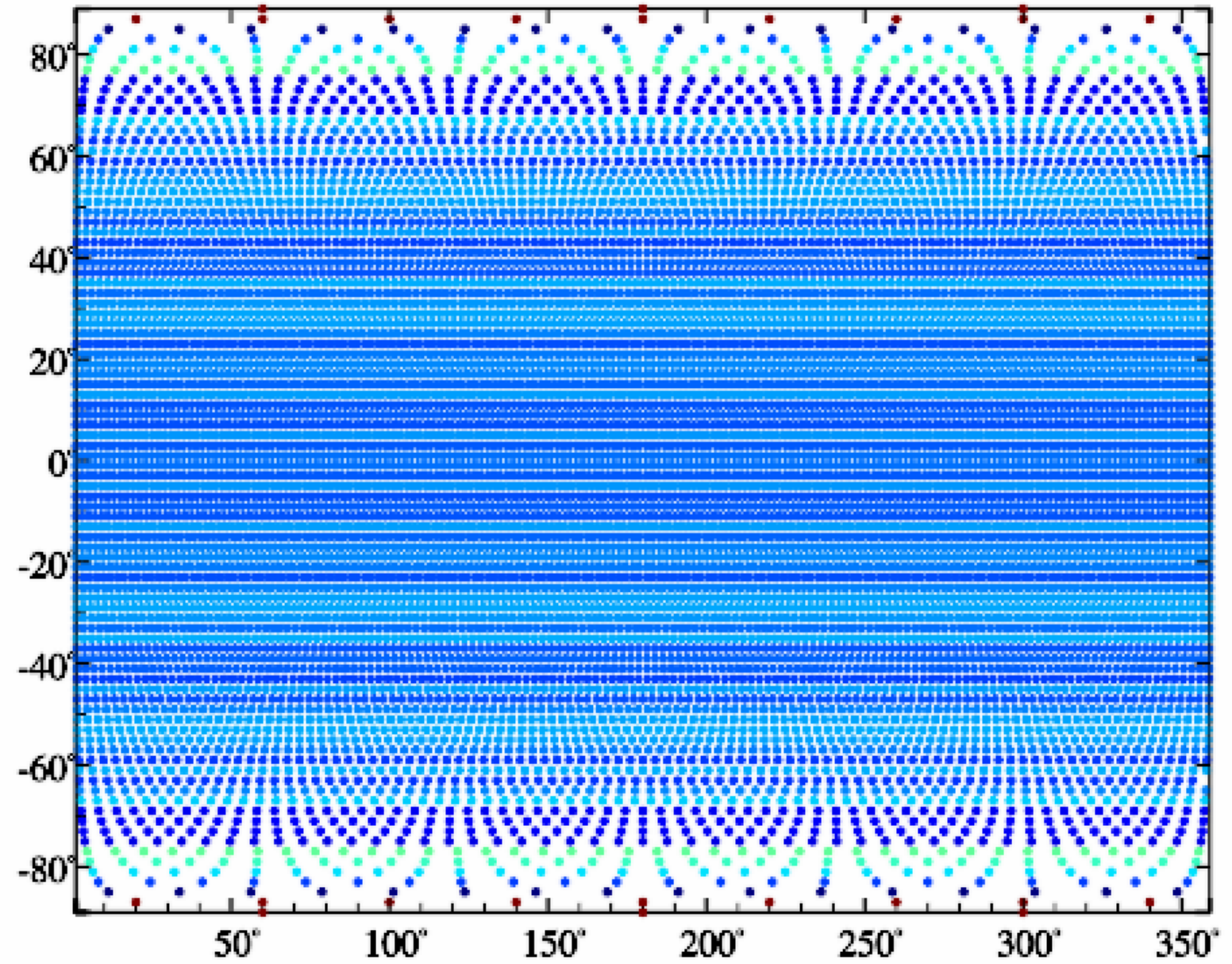
Plot mode longitude, latitude and area of the center of cell grid

Calculation and save

Extract plot data

Reuter grid plot →

Save current plot as



Reuter spatial grid results file

10300	60.000000	87.000000	4.67	0.026168	0.045324	0.998630
10301	100.000000	87.000000	4.67	-0.009088	0.051541	0.998630
10302	140.000000	87.000000	4.67	-0.040092	0.033641	0.998630
10303	180.000000	87.000000	4.67	-0.052336	0.000000	0.998630
10304	220.000000	87.000000	4.67	-0.040092	-0.033641	0.998630
10305	260.000000	87.000000	4.67	-0.009088	-0.051541	0.998630
10306	300.000000	87.000000	4.67	0.026168	-0.045324	0.998630
10307	340.000000	87.000000	4.67	0.049180	-0.017900	0.998630
10308	60.000000	89.000000	4.71	0.008726	0.015114	0.999848
10309	180.000000	89.000000	4.71	-0.017452	0.000000	0.999848
10310	300.000000	89.000000	4.71	0.008726	-0.015114	0.999848

Minimum Maximum geocentric latitude

-90.0°

90.0°

Minimum Maximum longitude

0.0°

360°

Set Reuter level K 90

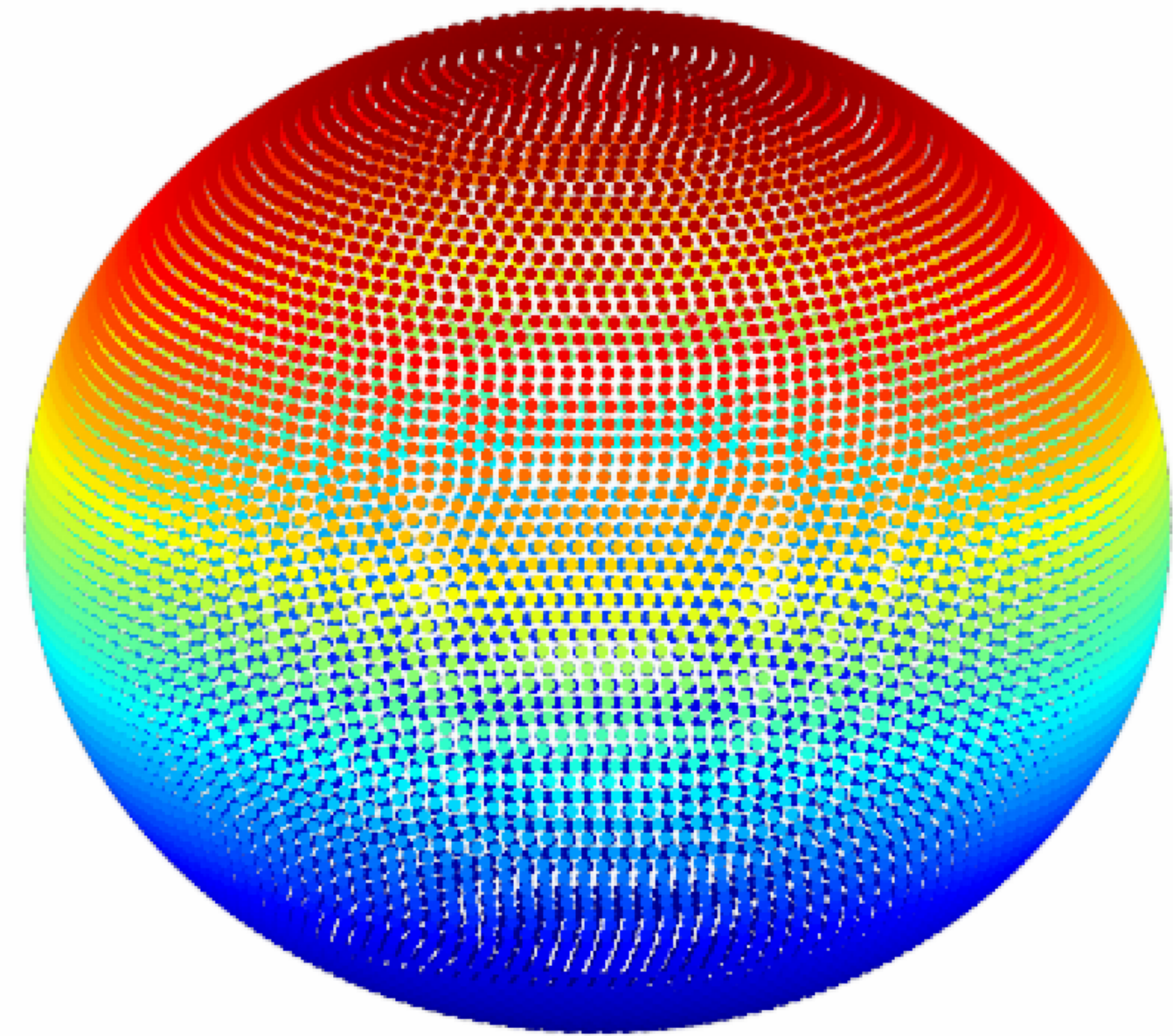
Plot mode Cartesian space coordinates of the center of cell grid

Calculation and save

Extract plot data

Reuter grid plot →

Save current plot as



Reuter spatial grid results file

10300	60.000000	87.000000	4.67	0.026168	0.045324	0.998630
10301	100.000000	87.000000	4.67	-0.009088	0.051541	0.998630
10302	140.000000	87.000000	4.67	-0.040092	0.033641	0.998630
10303	180.000000	87.000000	4.67	-0.052336	0.000000	0.998630
10304	220.000000	87.000000	4.67	-0.040092	-0.033641	0.998630
10305	260.000000	87.000000	4.67	-0.009088	-0.051541	0.998630
10306	300.000000	87.000000	4.67	0.026168	-0.045324	0.998630
10307	340.000000	87.000000	4.67	0.049180	-0.017900	0.998630
10308	60.000000	89.000000	4.71	0.008726	0.015114	0.999848
10309	180.000000	89.000000	4.71	-0.017452	0.000000	0.999848
10310	300.000000	89.000000	4.71	0.008726	-0.015114	0.999848

Minimum Maximum geocentric latitude

28.0° 34.0°

Minimum Maximum longitude

96.0° 104°

Set Reuter level K 1800

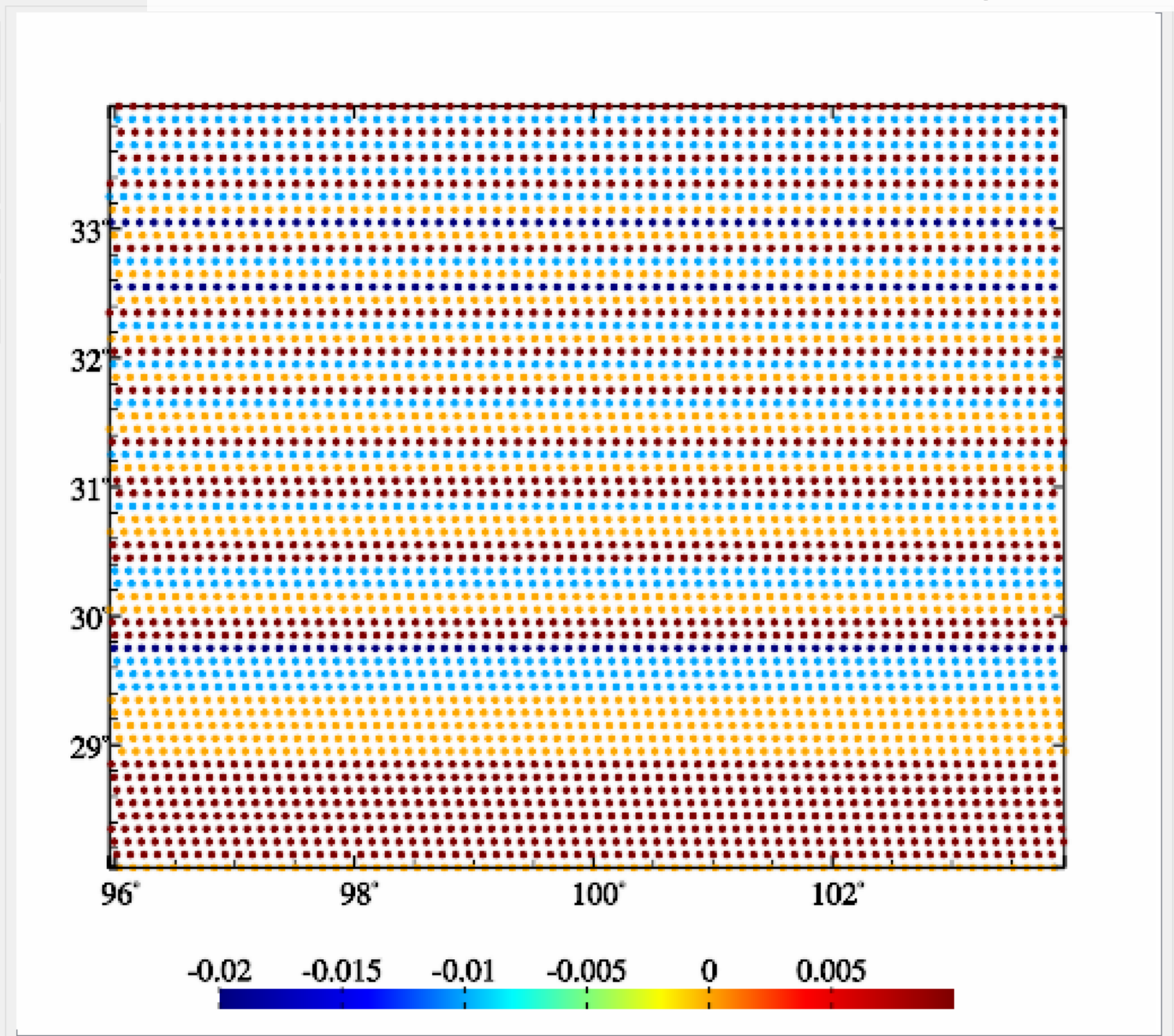
Plot mode longitude, latitude and area of the center of cell grid

Calculation and save

Extract plot data

Reuter grid plot →

Save current plot as



Reuter spatial grid results file

4097	102.659076	33.950000	0.01	-0.181790	0.809361	0.558469
4098	102.779638	33.950000	0.01	-0.183493	0.808976	0.558469
4099	102.900201	33.950000	0.01	-0.185194	0.808588	0.558469
4100	103.020764	33.950000	0.01	-0.186895	0.808197	0.558469
4101	103.141326	33.950000	0.01	-0.188596	0.807802	0.558469
4102	103.261889	33.950000	0.01	-0.190295	0.807403	0.558469
4103	103.382451	33.950000	0.01	-0.191994	0.807001	0.558469
4104	103.503014	33.950000	0.01	-0.193691	0.806595	0.558469
4105	103.623577	33.950000	0.01	-0.195388	0.806186	0.558469
4106	103.744139	33.950000	0.01	-0.197084	0.805773	0.558469
4107	103.864702	33.950000	0.01	-0.198779	0.805356	0.558469

Gravity field approach performance using SRBFs - gravity disturbance → height anomaly



Open the discrete residual anomalous field element observation file

Select type of observations: gravity disturbance (mGal)

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of the gravity disturbance: 7

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observations mean, standard deviation, minimum, maximum. Record format: point no, longitude, latitude, ellipsoidal height, weight, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 11:50:41
>> Complete the computation!
>> Computation end time: 2024-09-25 11:51:02
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.4113 standard deviation 21.8940 minimum -141.1997 maximum 112.4878 of the source observations.
** mean -0.0216 standard deviation 1.9088 minimum -54.0885 maximum 53.0770 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

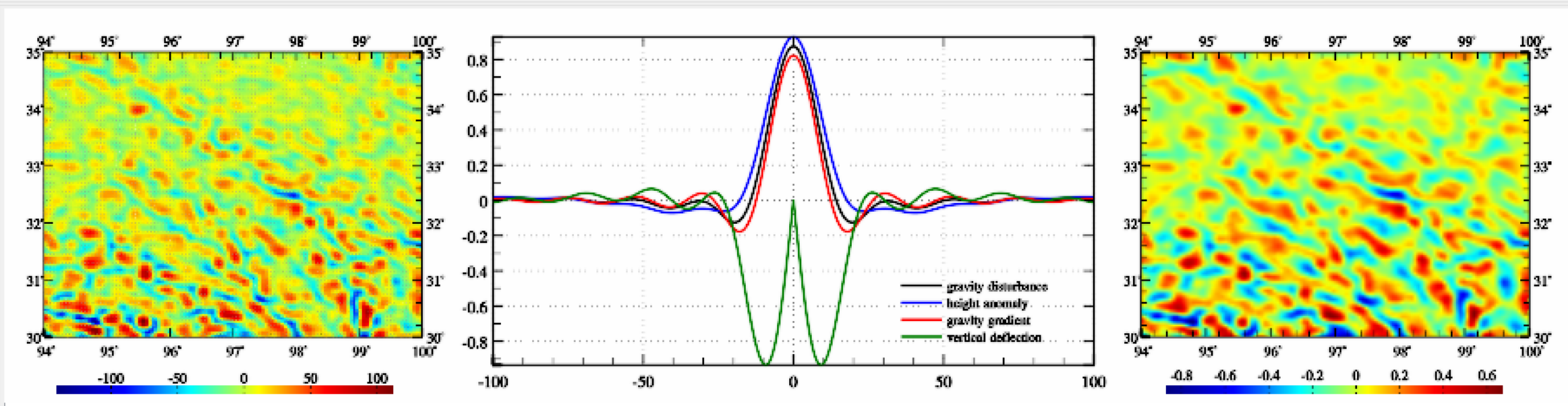
Type of target element: height anomaly (m)

Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-0.4934	-0.4466	-0.3004	-0.1309	-0.0358	0.0254	0.0649	0.0679	0.0223	-0.0732
0.1289	0.2125	0.1641	-0.0056	-0.2094	-0.2817	-0.1712	0.0125	0.1665	0.2722
0.0273	-0.2539	-0.4608	-0.4318	-0.2215	0.0453	0.2281	0.2436	0.1685	0.0364
0.2761	0.2306	0.1674	0.1678	0.1902	0.2424	0.2110	0.0717	-0.1042	-0.2823
-0.5242	-0.5674	-0.6053	-0.6055	-0.5592	-0.4309	-0.2461	-0.0668	0.0980	0.2084
0.3092	0.2309	0.0920	-0.1759	-0.4433	-0.5361	-0.3991	-0.1534	0.0430	0.1449
0.0486	-0.0206	-0.1177	-0.1556	-0.0826	0.0628	0.2036	0.2324	0.0729	-0.1942

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→



SRBF approach algorithms

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs – once cumulative approach



Open the discrete residual anomalous field element observation file

Select type of observations: gravity disturbance (mGal)

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 5

column ordinal number of the gravity disturbance: 7

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 540

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 6.0km

Action distance of SBRF center: 75km

Reuter network level K: 3600

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 11:54:21
>> Complete the computation!
>> Computation end time: 2024-09-25 11:55:50
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.0216 standard deviation 1.9088 minimum -54.0885 maximum 53.0770 of the source observations.
** mean -0.0044 standard deviation 0.6536 minimum -28.2780 maximum 11.2439 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

Type of target element: height anomaly (m)

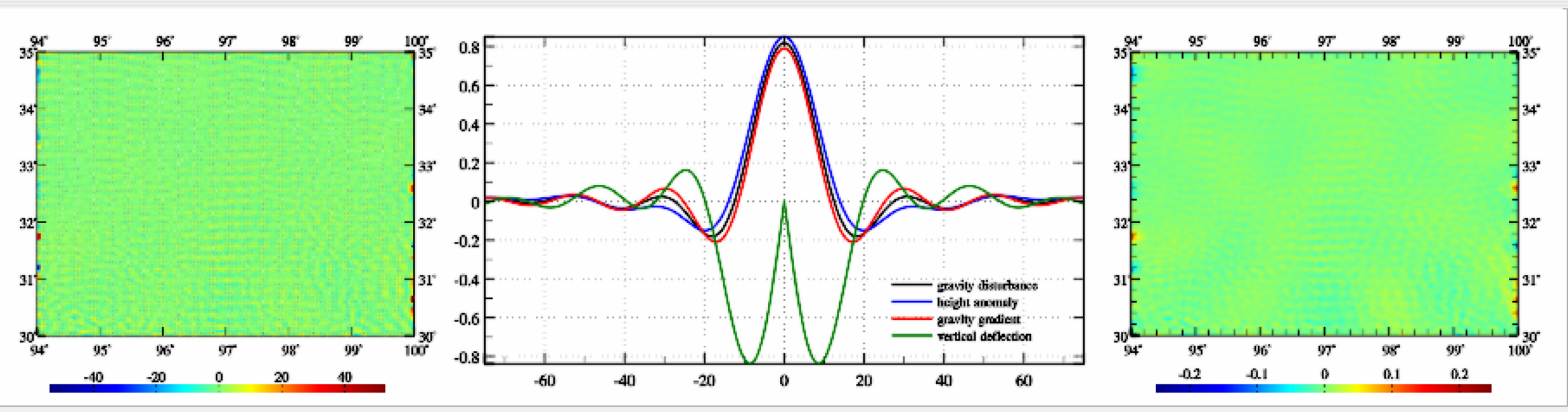
Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
0.0062	0.0156	0.0198	0.0140	0.0131	0.0070	0.0129	0.0219	0.0341	0.0222
-0.0377	-0.0595	-0.0418	-0.0222	-0.0199	-0.0378	-0.0153	-0.0140	-0.0054	-0.0043
-0.0170	-0.0175	-0.0034	0.0075	0.0119	0.0092	0.0314	0.0430	0.0474	0.0319
0.0164	0.0141	0.0022	-0.0088	0.0031	0.0067	0.0020	-0.0066	-0.0183	-0.0052
0.0253	0.0220	0.0056	0.0005	0.0232	0.0116	0.0053	-0.0034	-0.0063	0.0051
0.0154	0.0094	-0.0055	-0.0026	0.0034	-0.0012	0.0021	0.0186	0.0390	0.0388
0.0018	0.0060	0.0081	0.0129	0.0031	0.0015	0.0101	0.0183	0.0214	-0.0066

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→

SRBF approach algorithms



observed residual gravity disturbance (mGal) | spherical radial basis function spatial curve | target residual height anomaly (m)

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - vertical deflection → height anomaly



Open the discrete residual anomalous field element observation file

Select type of observations: vertical deflection vector (")

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of vertical deflection westward: 8

column ordinal number of vertical deflection southward: 9

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observations mean, standard deviation, minimum, maximum. Record format: point no, longitude, latitude, ellipsoidal height, weight, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 11:58:13
>> Complete the computation!
>> Computation end time: 2024-09-25 11:58:47
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.0129 standard deviation 3.2354 minimum -19.8241 maximum 23.1114 of the source observations.
** mean 0.0039 standard deviation 0.3118 minimum -9.2421 maximum 10.5513 of the result residuals.
```

Type of target element: height anomaly (m)

Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-0.4808	-0.4329	-0.2845	-0.1120	-0.0144	0.0492	0.0874	0.1029	0.0741	-0.0079
0.1176	0.2158	0.1885	0.0295	-0.1768	-0.2662	-0.1820	-0.0265	0.1247	0.2425
0.0318	-0.2592	-0.4819	-0.4693	-0.2501	0.0327	0.2356	0.2747	0.2107	0.0684
0.2274	0.1964	0.1420	0.1525	0.1764	0.2116	0.1653	0.0179	-0.1573	-0.3123
-0.4060	-0.4720	-0.5360	-0.5683	-0.5500	-0.4631	-0.3231	-0.1673	-0.0224	0.0857
0.3073	0.2396	0.0991	-0.1836	-0.4707	-0.5827	-0.4539	-0.2076	-0.0068	0.1091
0.0690	-0.0055	-0.1059	-0.1323	-0.0382	0.1303	0.2883	0.3127	0.1212	-0.1934

Open the ellipsoidal height grid file of calculation surface

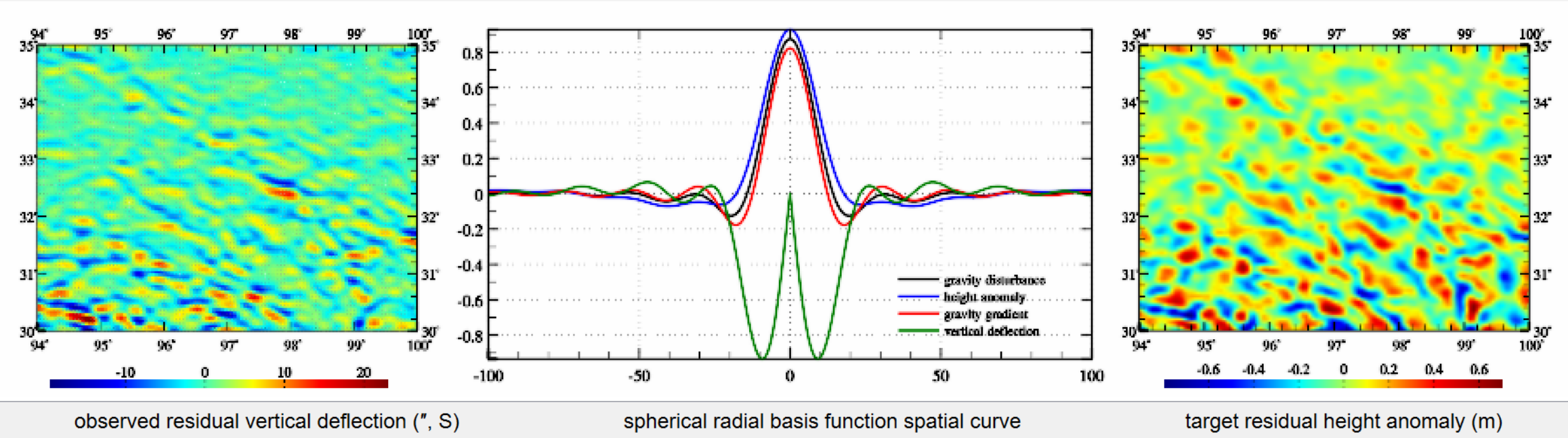
Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→

SRBF approach algorithms



After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.

The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - height anomaly → gravity disturbance



Open the discrete residual anomalous field element observation file

Select type of observations: height anomaly (m)

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of the height anomaly: 5

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 12:02:43
>> Complete the computation!
>> Computation end time: 2024-09-25 12:03:01
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.0020 standard deviation 0.1590 minimum -0.8621 maximum 0.6546 of the source observations.
** mean -0.0011 standard deviation 0.0135 minimum -0.3763 maximum 0.4258 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

Type of target element: gravity disturbance (mGal)

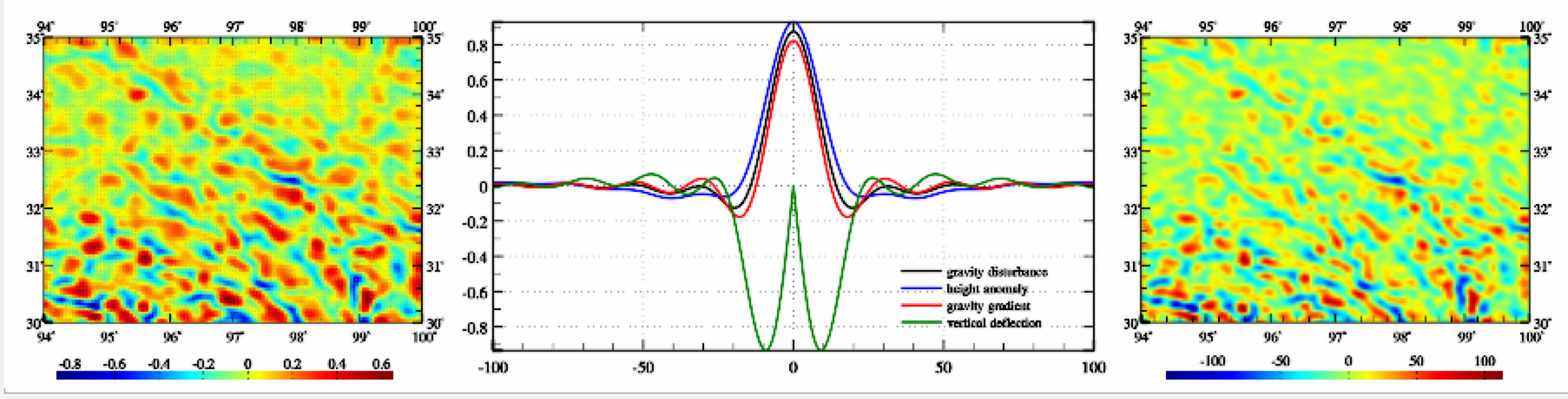
Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-65.3591	-58.7649	-35.2841	-10.0337	2.9287	7.2438	10.2652	13.5926	12.0766	-0.3089
6.4548	29.7980	29.7832	2.0592	-35.7794	-53.6309	-39.0541	-13.1329	4.8602	14.6182
6.6296	-41.4182	-73.4118	-66.0062	-26.5807	24.2028	57.9004	58.5887	36.5839	5.0106
29.0963	26.0823	17.9708	17.4266	24.1063	32.7800	24.6379	-1.1940	-30.9331	-51.1497
-15.4188	-22.7403	-39.5771	-54.8616	-60.0889	-51.9314	-35.2718	-19.3994	-3.8652	7.7557
39.4309	43.6354	26.5751	-17.0100	-64.3688	-82.8843	-60.8164	-21.0537	7.6201	16.2492
14.0937	-0.1259	-20.0057	-28.6960	-14.6046	17.8789	51.0941	61.0445	34.1631	-19.7100

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→

SRBF approach algorithms



observed residual height anomaly (m) | spherical radial basis function spatial curve | target residual gravity disturbance (mGal)

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - gravity disturbance → disturbing gravity gradient

Open the discrete residual anomalous field element observation file

Select type of observations **gravity disturbance (mGal)**

Set observations file format

number of rows of file header **1**

column ordinal number of ellipsoidal height in the record **4**

column ordinal number of weight **0**

column ordinal number of the gravity disturbance **7**

Select SRBF **radial multipole kernel**

Set SRBF parameters

Order m **1**

Minimum degree **360**

Maximum degree **1800**

Burial depth of Bjerhammar sphere **10.0km**

Action distance of SBRF center **100km**

Reuter network level K **1800**

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation **LU triangular decomposition**

Synchronous calculation of elements at discrete points

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot

Plot→

SRBF approach algorithms

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observations mean, standard deviation, minimum, maximum. Record format: point no, longitude, latitude, ellipsoidal height, weight, residual observation, where * is the output file name.
```

```
>> The parameter settings have been entered into the system!
```

```
** Click the [Start Computation] control button, or the [Start Computation] tool button...
```

```
>> Computation start time: 2024-09-25 12:06:29
```

```
>> Complete the computation!
```

```
>> Computation end time: 2024-09-25 12:06:50
```

```
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
```

```
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
```

```
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
```

```
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
```

```
>> Mean -0.4113 standard deviation 21.8940 minimum -141.1997 maximum 112.4878 of the source observations.
```

```
** mean -0.0216 standard deviation 1.9088 minimum -54.0885 maximum 53.0770 of the result residuals.
```

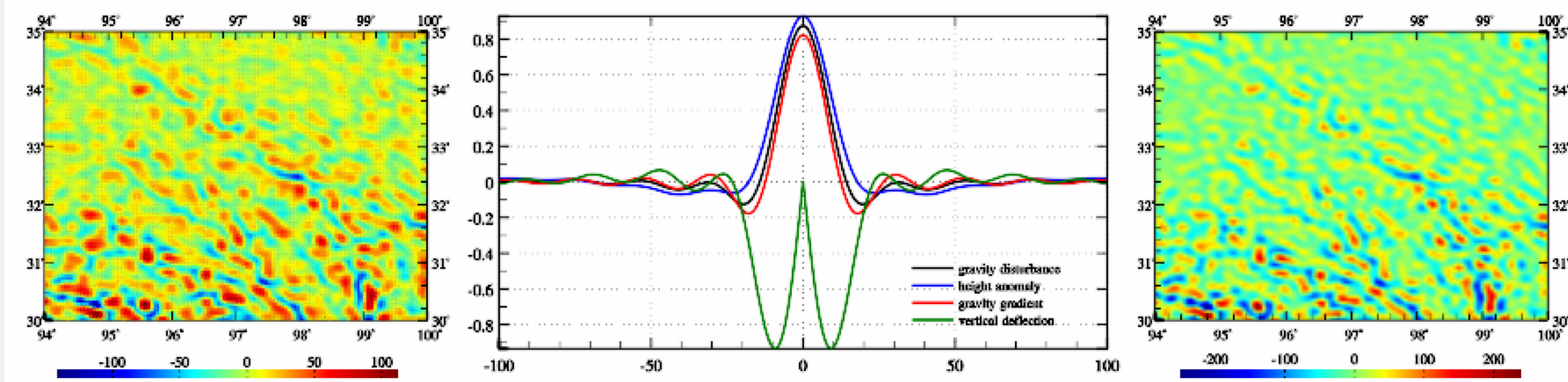
Type of target element **disturbing gradient (E, radial)**

Save the results as

Import setting parameters

Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-137.4913	-128.5689	-75.7644	-21.5254	-1.7301	0.0090	7.5791	20.3746	19.7973	-10.7891
-9.5433	43.9876	47.6359	-6.5605	-77.1569	-94.1416	-42.8307	15.0738	31.2255	9.8689
47.3224	-44.9296	-109.9247	-94.9134	-16.2553	76.4291	124.0372	104.8406	50.7895	-8.2329
45.1466	28.4229	2.7440	1.0298	24.3953	52.6813	41.2375	-13.0719	-74.3834	-113.3740
-26.6862	-32.8644	-62.8344	-90.7690	-98.7158	-80.0600	-48.4845	-19.0314	9.7789	27.5468
42.6806	66.7283	56.5979	-11.6138	-100.5078	-141.9563	-101.0767	-22.5800	28.7053	30.8881
31.6836	13.7471	-27.2075	-63.3576	-59.2446	-7.3958	63.8511	103.3469	71.7308	-18.6093



observed residual gravity disturbance (mGal)

spherical radial basis function spatial curve

target residual disturbing gradient (E, R)

🟢 After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.

🟢 The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - disturbing gravity gradient → height anomaly



Open the discrete residual anomalous field element observation file

Select type of observations: **disturbing gradient (E, radial)**

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of disturbing gravity gradient: 10

Select SRBF: **radial multipole kernel**

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 12:09:06
>> Complete the computation!
>> Computation end time: 2024-09-25 12:09:25
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.8635 standard deviation 38.2935 minimum -262.7565 maximum 232.6519 of the source observations.
** mean -0.0373 standard deviation 3.7041 minimum -90.4115 maximum 78.2329 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: **LU triangular decomposition**

Synchronous calculation of elements at discrete points

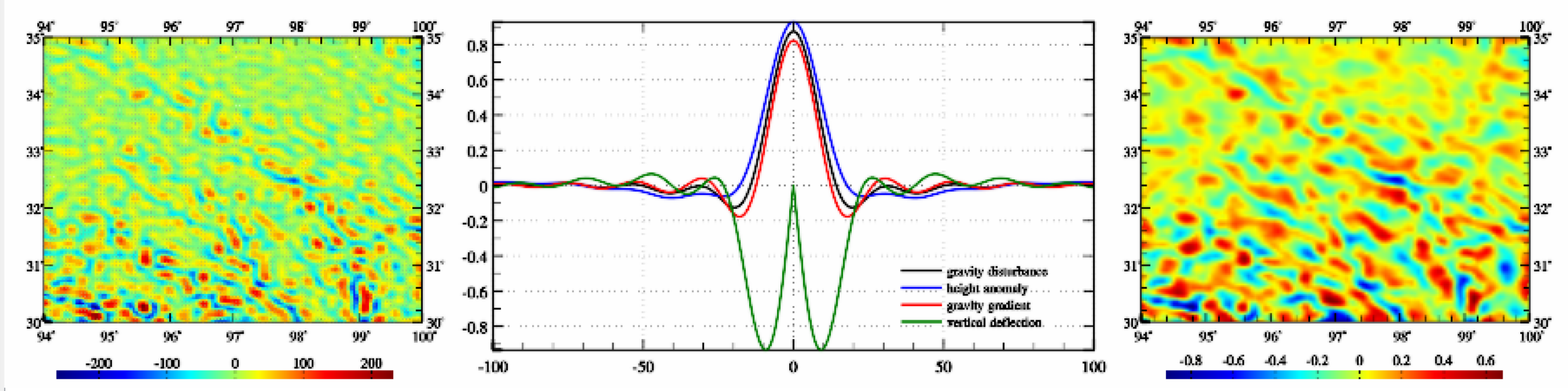
Type of target element: **height anomaly (m)**

Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-0.5445	-0.5102	-0.3560	-0.1739	-0.0708	-0.0012	0.0419	0.0482	-0.0085	-0.1114
0.1839	0.2645	0.1883	0.0030	-0.2013	-0.2539	-0.1254	0.0529	0.1988	0.2703
0.1064	-0.1544	-0.3614	-0.3513	-0.1629	0.0673	0.2065	0.1871	0.0870	-0.0395
0.2908	0.2241	0.1481	0.1425	0.1681	0.2248	0.2043	0.0655	-0.1207	-0.3326
-0.7192	-0.7325	-0.7358	-0.6986	-0.6140	-0.4451	-0.2224	-0.0131	0.1616	0.2708
0.2893	0.2072	0.0790	-0.1720	-0.4170	-0.5050	-0.3697	-0.1306	0.0615	0.1578
0.0520	-0.0110	-0.1084	-0.1595	-0.1227	-0.0041	0.1167	0.1545	0.0335	-0.1824

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→



SRBF approach algorithms

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - disturbing gravity gradient → gravity disturbance



Open the discrete residual anomalous field element observation file

Select type of observations: disturbing gradient (E, radial)

Set observations file format
 number of rows of file header: 1
 column ordinal number of ellipsoidal height in the record: 4
 column ordinal number of weight: 0
 column ordinal number of disturbing gravity gradient: 10

Select SRBF: radial multipole kernel

Set SRBF parameters
 Order m: 1
 Minimum degree: 360
 Maximum degree: 1800
 Burial depth of Bjerhammar sphere: 10.0km
 Action distance of SBRF center: 100km
 Reuter network level K: 1800

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition
 Synchronous calculation of elements at discrete points

⚠ If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

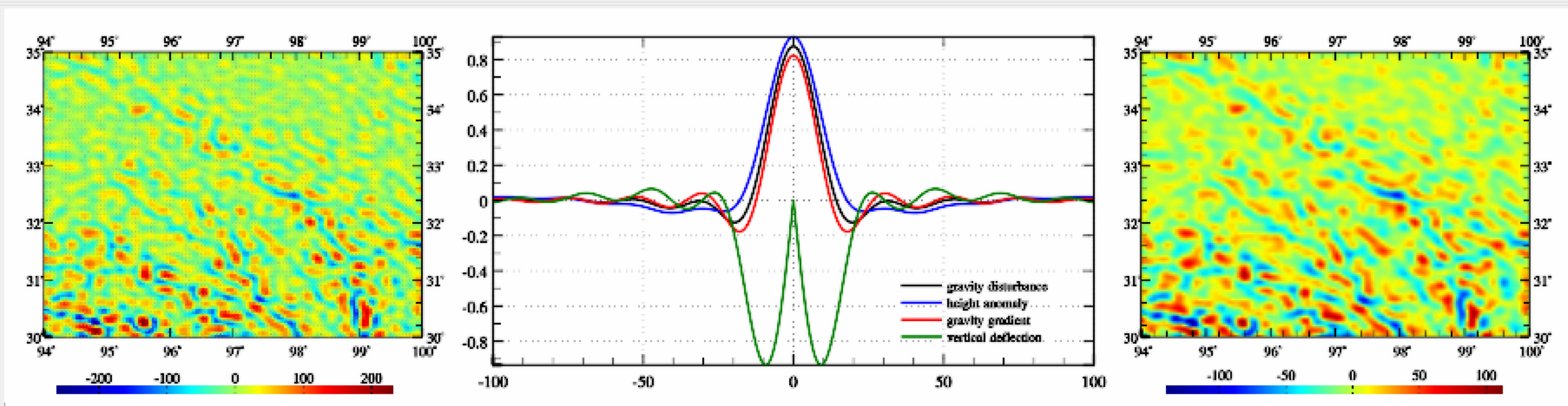
Extract data to be plot | Plot→

SRBF approach algorithms

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 12:10:29
>> Complete the computation!
>> Computation end time: 2024-09-25 12:10:48
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.8635 standard deviation 38.2935 minimum -262.7565 maximum 232.6519 of the source observations.
** mean -0.0373 standard deviation 3.7041 minimum -90.4115 maximum 78.2329 of the result residuals.
```

Type of target element: gravity disturbance (mGal) | Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-86.0957	-82.4429	-54.2835	-22.6428	-7.0178	-1.1718	3.1876	6.8333	2.1125	-15.3716
19.5807	39.6239	29.9655	-4.2432	-41.1459	-48.6841	-22.7812	7.2624	21.6418	19.1479
24.1767	-19.6837	-52.4652	-47.9595	-12.0423	31.0213	53.7371	44.2942	17.0412	-11.6750
32.6849	20.3425	5.5606	3.6310	13.4996	27.5139	25.4570	2.5238	-27.7038	-55.1547
-58.4705	-59.5539	-68.7171	-75.0853	-71.2172	-53.1640	-27.0058	-2.5787	17.3225	28.2437
32.7498	34.0782	21.5186	-14.9527	-56.5772	-75.1354	-54.6346	-15.1664	14.0448	21.2175
11.7707	2.5332	-15.4607	-29.5430	-27.0644	-5.0157	23.2032	37.5784	21.5201	-18.7909



observed residual disturbing gradient (E, R) | spherical radial basis function spatial curve | target residual gravity disturbance (mGal)

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - disturbing gravity gradient → vertical deflection



Open the discrete residual anomalous field element observation file

Select type of observations: **disturbing gradient (E, radial)**

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of disturbing gravity gradient: 10

Select SRBF: **radial multipole kernel**

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 12:12:08
>> Complete the computation!
>> Computation end time: 2024-09-25 12:12:26
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.8635 standard deviation 38.2935 minimum -262.7565 maximum 232.6519 of the source observations.
** mean -0.0373 standard deviation 3.7041 minimum -90.4115 maximum 78.2329 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: **LU triangular decomposition**

Synchronous calculation of elements at discrete points

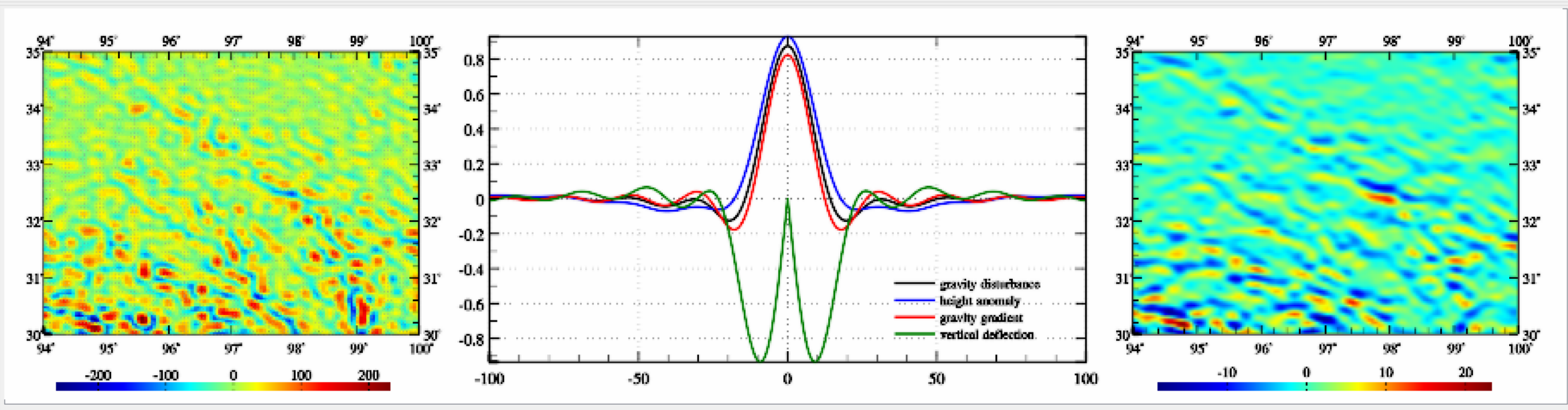
Type of target element: **vertical deflection vector (")**

Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-4.5854	-5.1192	-5.1277	-4.5604	-3.2649	-1.5760	0.1493	1.5548	2.2531	1.9720
-13.0641	-13.7256	-11.4734	-7.2443	-2.4898	1.0888	2.4705	1.4576	-1.3255	-4.5001
5.4203	6.3758	7.8360	9.0473	9.0195	7.8777	6.5432	5.7170	5.3042	4.4329
-2.7174	-0.9445	0.3396	0.5304	-0.1437	-1.8812	-3.9199	-5.5399	-6.5380	-6.4282
3.4789	3.4859	3.1237	2.8089	2.2345	0.9410	-0.8284	-2.4133	-3.5322	-4.1473
-2.8039	-1.5847	0.1984	2.1158	2.7072	1.2931	-1.1958	-3.1622	-4.1861	-4.7232
0.6454	1.0979	0.3951	-1.5137	-3.4993	-4.2271	-3.1416	-1.1754	0.1605	-0.0969

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→



SRBF approach algorithms

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Gravity field approach performance using SRBFs - vertical deflection → disturbing gravity gradient



Open the discrete residual anomalous field element observation file

Select type of observations: vertical deflection vector (")

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of vertical deflection westward: 8

column ordinal number of vertical deflection southward: 9

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

```
>> The program outputs the residual observation file *.chs into the current directory. The file header format: source observations mean, standard deviation, minimum, maximum, residual observation, where * is the output file name.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 12:14:01
>> Complete the computation!
>> Computation end time: 2024-09-25 12:14:32
>> The program also outputs various field elements' SRBF spatial curve file *spc.rbf, various field elements' SRBF spectral curve files *dgr.rbf and SRBF center file* center.txt into the current directory.
** *spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** The file header of *dgr.rbf is the same as *spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.
** *center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Mean -0.0129 standard deviation 3.2354 minimum -19.8241 maximum 23.1114 of the source observations.
** mean 0.0039 standard deviation 0.3118 minimum -9.2421 maximum 10.5513 of the result residuals.
```

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

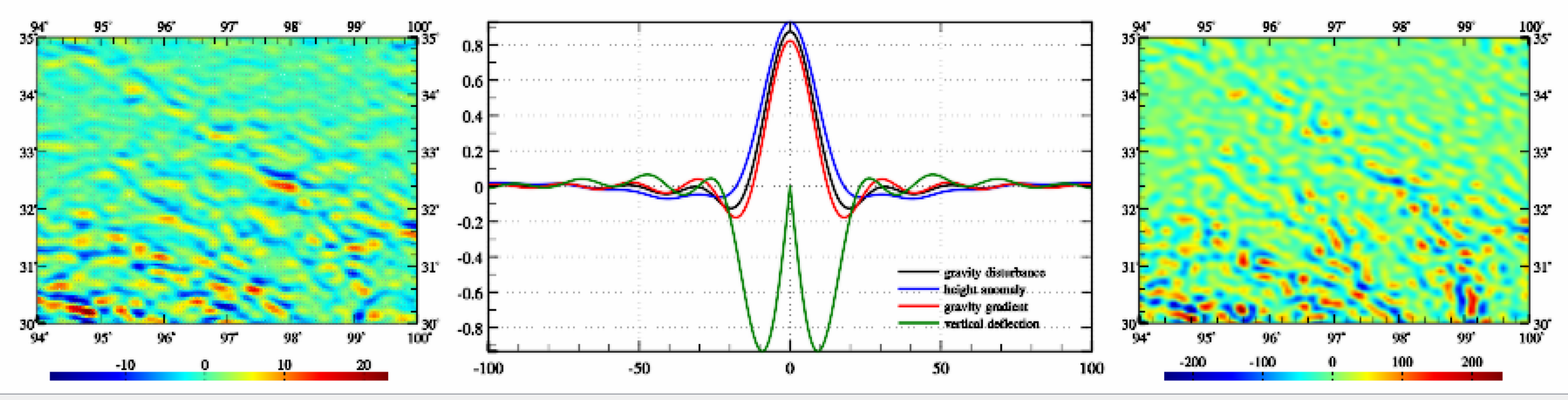
Type of target element: disturbing gradient (E, radial)

Save the results as | Import setting parameters | Start Computation

94.00000000	100.00000000	30.00000000	35.00000000	0.05000000	0.05000000	0.0000			
-131.5563	-121.2759	-68.2304	-15.2280	2.8825	4.9227	13.5714	28.3154	28.5758	-1.9308
-20.5629	37.0549	50.9059	4.0181	-65.4929	-87.5943	-45.4304	5.3181	21.8382	5.4180
49.8439	-43.1920	-110.4821	-99.4924	-20.8064	74.7930	127.9823	116.0991	66.5645	5.4139
38.8682	24.1678	-1.4172	-1.5540	23.2691	49.4169	34.1032	-24.8001	-89.4196	-125.3868
-4.0226	-15.5614	-50.6659	-82.7878	-94.7657	-84.2882	-63.3140	-40.0268	-14.1636	6.7163
45.7625	71.6289	58.8982	-13.4971	-105.9081	-149.7673	-110.3400	-32.7756	18.5034	23.2139
37.2386	16.2392	-27.4959	-63.2113	-55.3159	3.3591	82.1004	124.5486	86.5544	-18.3114

🔔 If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Extract data to be plot | Plot→



SRBF approach algorithms

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Detection of observation gross errors and measurement of external accuracy indexes using SRBFs



Open the discrete residual anomalous field element observation file

Select type of observations: gravity disturbance (mGal)

Set observations file format

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 4

column ordinal number of weight: 0

column ordinal number of the gravity disturbance: 7

Select SRBF: radial multipole kernel

Set SRBF parameters

Order m: 1

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

Open the ellipsoidal height grid file of calculation surface

Solution of normal equation: LU triangular decomposition

Synchronous calculation of elements at discrete points

If the measuring points of the target observations to be evaluated are taken as the calculation points, the field element at the measuring point can be estimated from the observations input by the program, and then we can effectively detect the gross error of the target observations to be evaluated and measure their external accuracy indexes.

Open the calculation point space location file

Extract data to be plot | Plot

SRBF approach algorithms

maximum, residual observations mean, standard deviation, minimum, maximum. Record format: point no, longitude, latitude, ellipsoidal height, weight, residual observation, where * is the output file name.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-25 14:13:09
 >> Complete the computation!
 >> Computation end time: 2024-09-25 14:13:35

>> The program outputs the target type of field element file *.tgt of the calculation points into the current directory, where & is the output file name.
 >> The program also outputs various field elements' SRBF spatial curve file *.spc.rbf, various field elements' SRBF spectral curve files *.dgr.rbf and SRBF center file *.center.txt into the current directory.

** *.spc.rbf file header format: SRBF type (0-radial multipole kernel function, 1-Poisson wavelet kernel function), order of SRBF, Minimum and maximum degree of SRBF Legendre expansion, Bjerhammar sphere buried depth (km). The record format: spherical distance (km), the normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.

** The file header of *.dgr.rbf is the same as *.spc.rbf. The record format: the degree n of SRBF Legendre expansion, degree n normalized SRBF values from the gravity disturbance, height anomaly, disturbing gravity gradient and total vertical deflection.

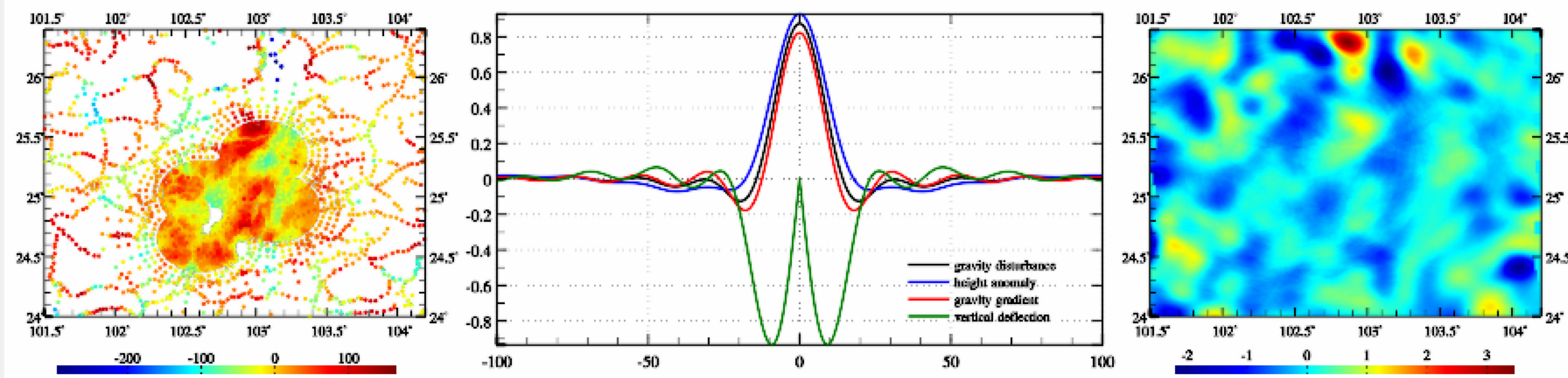
** *.center.txt file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: point no, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Mean 0.3186 standard deviation 42.1772 minimum -296.0915 maximum 165.2611 of the source observations.
 ** mean -0.4365 standard deviation 16.8116 minimum -96.1056 maximum 86.3113 of the result residuals.

Type of target element: height anomaly (m)

Save the results as | Import setting parameters | Start Computation

101.500000	104.200000	24.000000	26.400000	8.333333333E-03	8.333333333E-03					
-0.4912	-0.5786	-0.6274	-0.6591	-0.7090	-0.7608	-0.8090	-0.8661	-0.9124	-0.9433	
-1.1649	-1.1867	-1.2073	-1.2110	-1.2162	-1.2077	-1.1991	-1.1762	-1.1479	-1.0960	
-0.6807	-0.5738	-0.4708	-0.3505	-0.2356	-0.1163	0.0023	0.1311	0.2527	0.3708	
1.0154	1.0716	1.1368	1.1921	1.2511	1.2863	1.3079	1.3179	1.3200	1.3026	
1.0660	0.9977	0.9349	0.8780	0.7992	0.7183	0.6436	0.5732	0.4894	0.4073	
-0.0221	-0.0980	-0.1504	-0.1790	-0.2310	-0.2657	-0.2762	-0.3251	-0.3318	-0.2904	
-0.2487	-0.2257	-0.2066	-0.1937	-0.1782	-0.1227	-0.0995	-0.0813	-0.0580	-0.0299	



observed residual gravity disturbance (mGal) | spherical radial basis function spatial curve | target residual height anomaly (m)

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observations file again to refine target field elements by the multiple cumulative SRBF approach. Generally, the stable solution can be achieved by accumulating 1-3 times SRBF approaches, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) the target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Detection of observation gross errors and measurement of external accuracy indexes using SRBFs

Open file Save as Import parameters Start Computation

Gross error detection on observations based on low-pass reference surface

The discrete point file to be detect

Number of rows of file header: 1

Column ordinal number of the attribute to be detect: 7

Beyond multiples of the standard deviation n: 3.0

Open low-pass reference surface grid file

Save the results as

Save gross error as

Import setting parameters

Start Computation

```
>> [Function] value at the difference
** The reference also be the space
>> Open the discrete point file
** Look at the input file information
>> Open low-pass reference surface grid file
>> Save the results as
>> Save gross error as
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2023-03-20 16:19:14
>> Complete the computation!
>> Computation end time: 2023-03-20 16:19:14
```

Simple and direct calculation on geodetic data files

Open file Save as Import parameters Start computation Save process Follow example

Weighted operation on two specified attributes in record file

Weighted operation on two geodetic grid files

Weighted operation on two vector grid files

Weighted operation on two harmonic coefficient files

Open a discrete point file

The file format parameters

Number of rows of the file header: 1

Column ordinal number of attribute 1: 5

Column ordinal number of attribute 2: 6

Select operation mode: Minus -

Set weight

The first weight: 1.00

The second weight: 1.00

Save the results as

Import setting parameters

Start computation

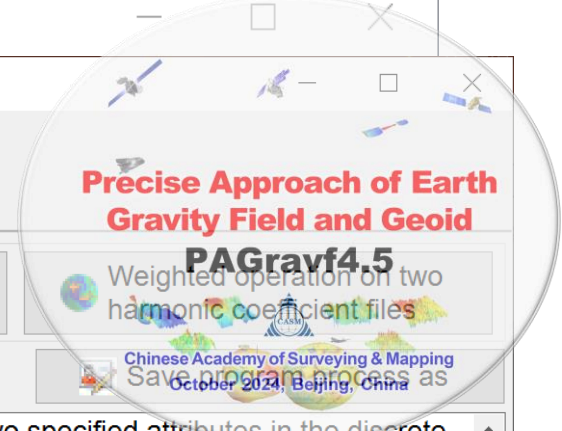
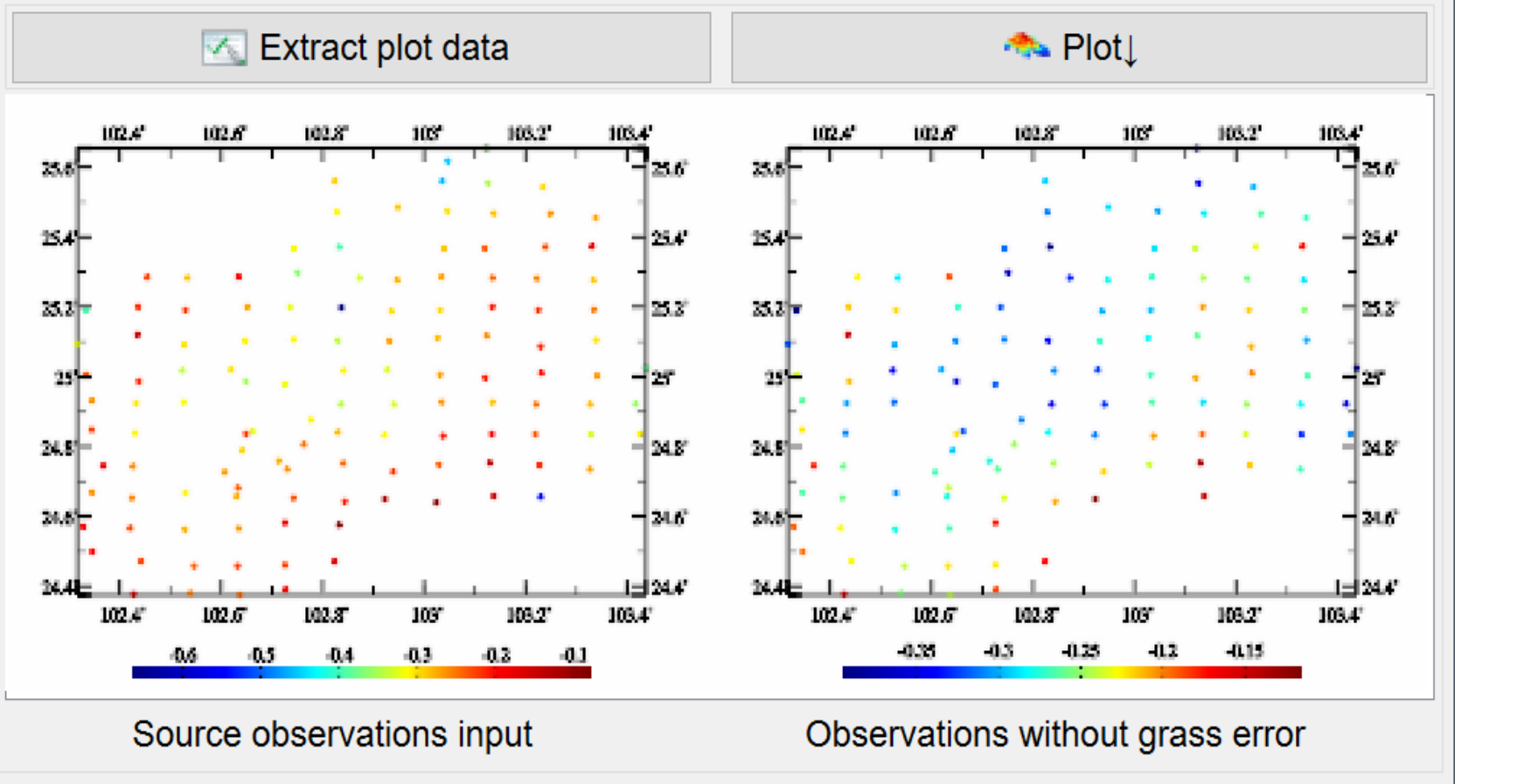
Save data in the text box as

Display of the input-output file↓

ID	lon(degree decimal)	lat	ellpH(m)	rnt/ssi(m)	0.1227	-0.2283
1	102.4424	24.4717	-32.7581	-0.1056	0.1227	-0.2283
2	102.5467	24.4580	-32.9577	-0.4237	-0.1831	-0.2406
3	102.6324	24.4582	-32.5792	-0.1359	0.0863	-0.2222
4	102.7259	24.4605	-32.3917	-0.0593	0.1645	-0.2238
5	102.4208	24.5663	-32.6038	-0.0304	0.1975	-0.2279
6	102.5286	24.5627	-32.5636	-0.1397	0.1393	-0.2790
7	102.6344	24.5656	-32.3822	-0.0694	0.1970	-0.2664
8	102.7258	24.5819	-32.2197	-0.0128	0.1639	-0.1767
9	102.8326	24.5755	-32.5408	-0.4474	-0.3691	-0.0783
10	102.3455	24.6689	-32.9297	-0.2903	-0.0256	-0.2647

-0.2651	0.0557	0.3951	0.1154			
9	102.8326	24.5755	-32.5408	-0.4474	-0.3691	-0.0783
70	102.8371	25.1980	-32.3637	-0.6940	-0.0300	-0.6640
93	103.0359	25.5603	-30.9594	0.3435	0.8044	-0.4609
100	103.0470	25.6173	-30.9519	0.3086	0.7617	-0.4531
112	103.2299	24.6558	-32.3789	-0.8314	-0.2773	-0.5541
113	103.0244	24.6400	-32.2768	-0.4286	-0.3414	-0.0872

The measured external accuracy of GNSS-leveling



All-element modelling on gravity field using SRBFs from gravity disturbance + disturbing gradient



Open the discrete heterogeneous residual observations file

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 6

column ordinal number of weight: 7

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

Select the adjustable observations: gravity disturbance (mGal)

Contribution rate κ of adjustable observations: 1.00

Open the ellipsoidal height grid file of calculation surface

of file header, whose format: observation type (0~5), source observation mean, standard deviation, minimum, maximum, residual observation, standard deviation, minimum, maximum. The record format: ID, longitude, latitude, ellipsoidal height, residual observation, source observation, observation type, weight.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-25 14:55:21
 >> Complete the computation!
 >> Computation end time: 2024-09-25 14:56:21

>> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.

>> The program also outputs SRBF center file *.center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Type 0 of source observations: mean -0.4107 standard deviation 21.8478 minimum -140.9351 maximum 112.3153
 ** Residual observations: mean -0.0148 standard deviation 2.0501 minimum -53.9731 maximum 52.9464
 >> Type 3 of source observations: mean -0.8635 standard deviation 38.2935 minimum -262.7565 maximum 232.6519
 ** Residual observations: mean -0.0493 standard deviation 4.1038 minimum -90.4115 maximum 78.2329

Solution of normal equation LU triangular decomposition

Save the results as Import setting parameters Start Computation

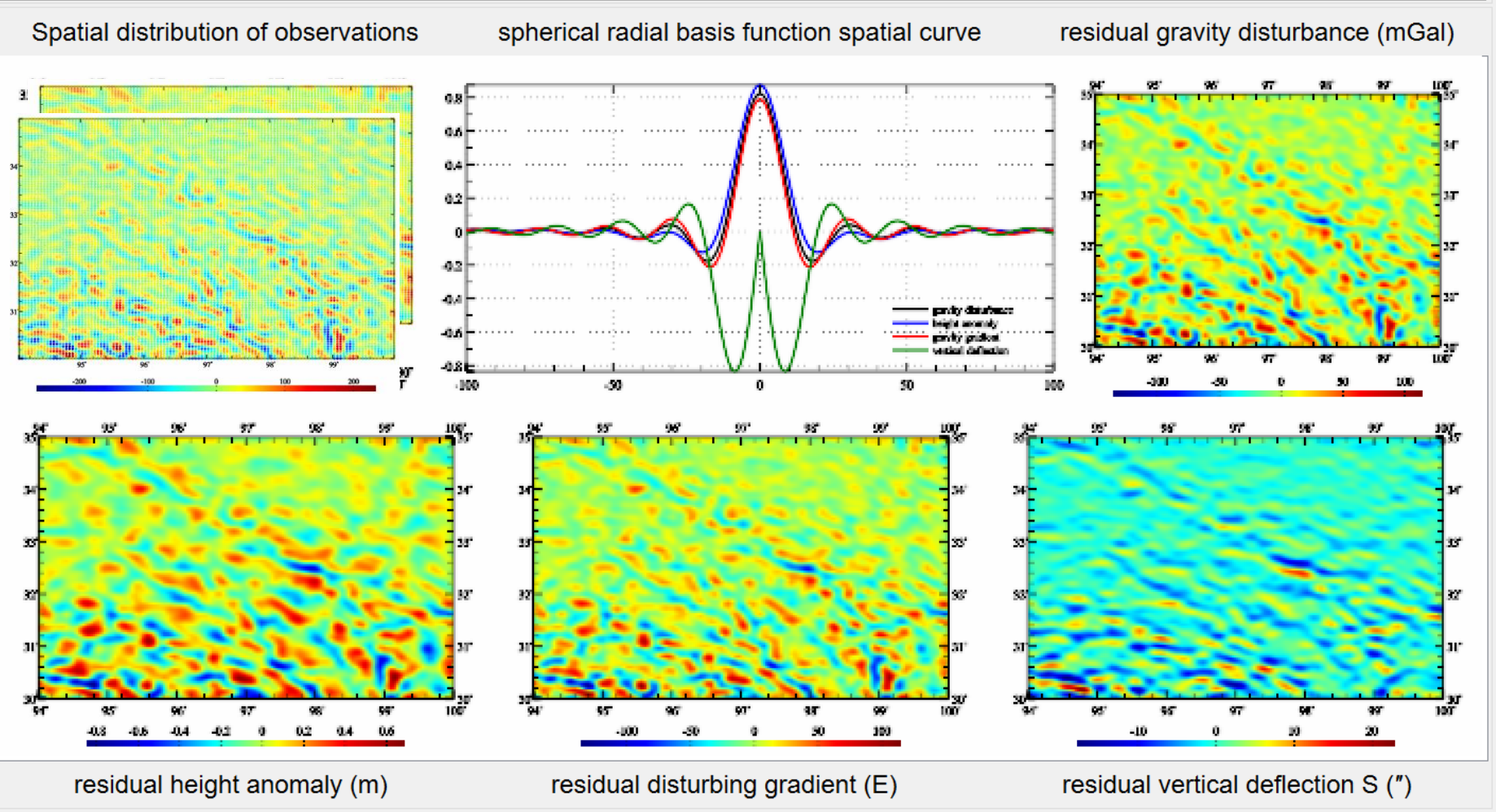
ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection	
1	94.02500	30.02500	3984.353	-77.2207	-0.4408	-77.0852	-150.4377	-2.8342	-0.6793
2	94.07500	30.02500	4226.989	-74.8346	-0.4200	-74.7056	-146.1030	-3.3732	1.4633
3	94.12500	30.02500	4461.719	-47.1390	-0.2763	-47.0541	-86.6200	-3.6689	-0.0672
4	94.17500	30.02500	4422.914	-15.6446	-0.1040	-15.6126	-22.1136	-3.6631	-0.9335
5	94.22500	30.02500	4335.893	-2.5174	-0.0125	-2.5136	-3.1028	-3.0189	-0.6005
6	94.27500	30.02500	4463.689	0.4754	0.0286	0.4666	-3.8129	-1.9210	1.1791

Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot Plot →

- The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.
- The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



All-element modelling on gravity field using SRBFs from heterogeneous observations – once cumulative approach

Open the discrete heterogeneous residual observations file

number of rows of file header: 2

column ordinal number of ellipsoidal height in the record: 7

column ordinal number of weight: 8

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 540

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 6.0km

Action distance of SBRF center: 60km

Reuter network level K: 3600

Select the adjustable observations: gravity disturbance (mGal)

Contribution rate κ of adjustable observations: 1.00

Open the ellipsoidal height grid file of calculation surface

of file header, whose format: observation type (0~5), source observation mean, standard deviation, minimum, maximum, residual observation mean, standard deviation, minimum, maximum. The record format: ID, longitude, latitude, ellipsoidal height, residual observation, source observation, observation type, weight.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-25 15:03:00
 >> Complete the computation!
 >> Computation end time: 2024-09-25 15:05:06

>> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.

>> The program also outputs SRBF center file *center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Type 0 of source observations: mean -0.0148 standard deviation 2.0501 minimum -53.9731 maximum 52.9464
 ** Residual observations: mean -0.0123 standard deviation 0.8907 minimum -34.4772 maximum 15.8370
 >> Type 3 of source observations: mean -0.0493 standard deviation 4.1038 minimum -90.4115 maximum 78.2329
 ** Residual observations: mean -0.0136 standard deviation 1.7897 minimum -66.0681 maximum 18.3159

Solution of normal equation: LU triangular decomposition

Save the results as Import setting parameters Start Computation

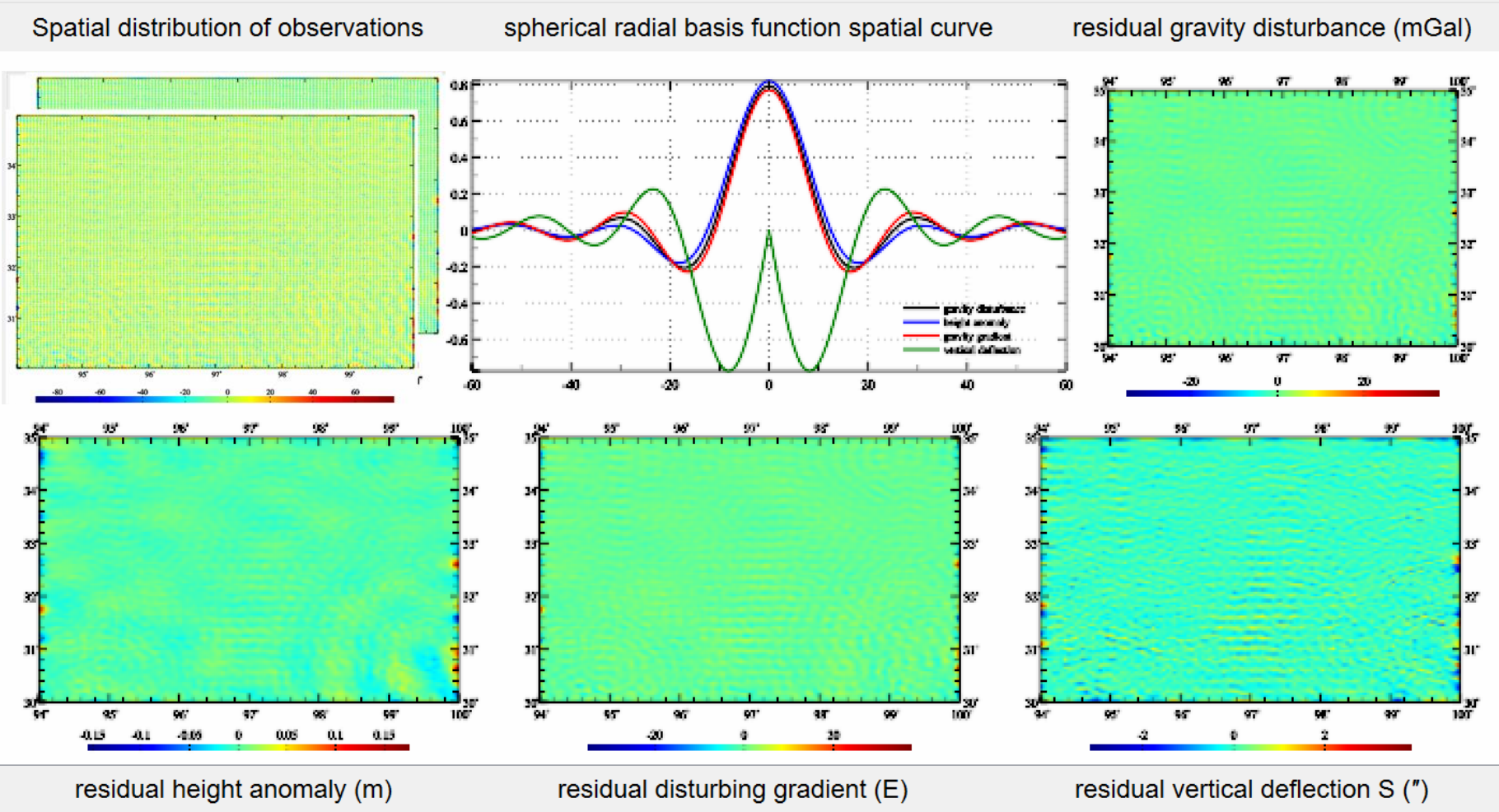
ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	94.02500	30.02500	3984.353	-2.8418	-0.0040	-2.8405	-10.4854	0.7989
2	94.07500	30.02500	4226.989	2.6628	0.0202	2.6565	2.8107	1.2960
3	94.12500	30.02500	4461.719	3.9362	0.0234	3.9290	6.8500	1.5126
4	94.17500	30.02500	4422.914	-0.0825	0.0103	-0.0856	-4.2421	0.6514
5	94.22500	30.02500	4335.893	-2.0002	-0.0002	-2.0002	-7.6845	-0.2314
6	94.27500	30.02500	4463.689	-0.6296	-0.0023	-0.6289	-1.0404	-0.2130

Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot Plot →

- The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.
- The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



All-element modelling on gravity field using SRBFs from gravity disturbance + vertical deflection



Open the discrete heterogeneous residual observations file

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 6

column ordinal number of weight: 7

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 360

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 1800

Select the adjustable observations: gravity disturbance (mGal)

Contribution rate κ of adjustable observations: 1.00

Open the ellipsoidal height grid file of calculation surface

```

type, weight.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-25 15:15:40
>> Complete the computation!
>> Computation end time: 2024-09-25 15:16:55
>> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.
>> The program also outputs SRBF center file *.center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').
>> Type 0 of source observations: mean -0.4107 standard deviation 21.8478 minimum -140.9351 maximum 112.3153
** Residual observations: mean -0.0783 standard deviation 2.1591 minimum -53.9731 maximum 52.9464
>> Type 4 of source observations: mean -0.0159 standard deviation 3.2930 minimum -19.5319 maximum 23.1114
** Residual observations: mean -0.0120 standard deviation 0.3816 minimum -9.0685 maximum 10.5513
>> Type 5 of source observations: mean -0.0098 standard deviation 3.1766 minimum -19.8241 maximum 17.6561
** Residual observations: mean -0.0023 standard deviation 0.2819 minimum -5.4896 maximum 6.1347
    
```

Solution of normal equation: LU triangular decomposition

Save the results as | Import setting parameters | Start Computation

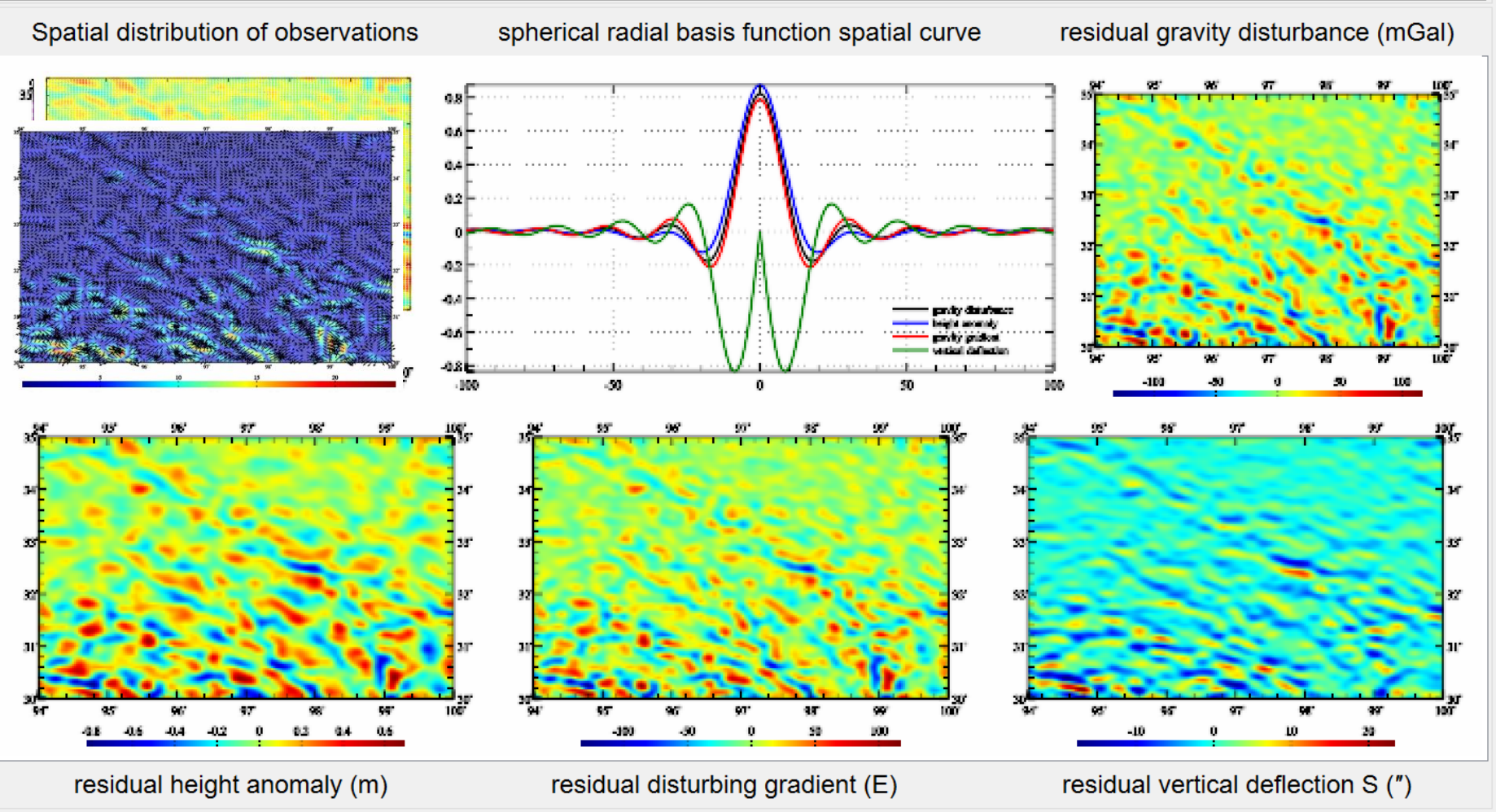
ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	94.02500	30.02500	3984.353	-73.8960	-0.4243	-73.7656	-143.5062	-1.5218
2	94.07500	30.02500	4226.989	-69.8020	-0.3950	-69.6807	-135.4588	-2.3945
3	94.12500	30.02500	4461.719	-42.5672	-0.2523	-42.4897	-77.5395	-3.0883
4	94.17500	30.02500	4422.914	-12.5740	-0.0847	-12.5480	-16.8624	-3.4064
5	94.22500	30.02500	4335.893	-0.4201	0.0041	-0.4213	0.0790	-2.8971
6	94.27500	30.02500	4463.689	2.9502	0.0470	2.9357	0.7663	-1.7248

Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot | Plot →

- The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.
- The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



All-element modelling on gravity field using SRBFs from gravity disturbance + height anomaly

+ vertical deflection + disturbing gravity gradient Follow example



Open the discrete heterogeneous residual observations file

number of rows of file header 1

column ordinal number of ellipsoidal height in the record 6

column ordinal number of weight 7

Select SRBF radial multipole kernel

Order m 3

Minimum degree 360

Maximum degree 1800

Burial depth of Bjerhammar sphere 10.0km

Action distance of SBRF center 100km

Reuter network level K 1800

Select the adjustable observations height anomaly (m)

Contribution rate κ of adjustable observations 1.00

Open the ellipsoidal height grid file of calculation surface

```
>> Complete the computation!
>> Computation end time: 2024-09-25 15:23:44
>> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" , SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.
>> The program also outputs SRBF center file *.center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ("). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (").
>> Type 0 of source observations: mean -0.4107 standard deviation 21.8478 minimum -140.9351 maximum 112.3153
** Residual observations: mean -0.0528 standard deviation 2.0522 minimum -53.9731 maximum 52.9464
>> Type 1 of source observations: mean -0.0020 standard deviation 0.1590 minimum -0.8621 maximum 0.6546
** Residual observations: mean 0.0003 standard deviation 0.0156 minimum -0.3763 maximum 0.4258
>> Type 3 of source observations: mean -0.8635 standard deviation 38.2935 minimum -262.7565 maximum 232.6519
** Residual observations: mean -0.1380 standard deviation 4.7873 minimum -90.4115 maximum 78.2329
>> Type 4 of source observations: mean -0.0159 standard deviation 3.2930 minimum -19.5319 maximum 23.1114
** Residual observations: mean -0.0140 standard deviation 0.4045 minimum -9.0195 maximum 10.5513
>> Type 5 of source observations: mean -0.0098 standard deviation 3.1766 minimum -19.8241 maximum 17.6561
** Residual observations: mean -0.0009 standard deviation 0.3000 minimum -5.4896 maximum 6.1347
```

Solution of normal equation LU triangular decomposition

Save the results as Import setting parameters Start Computation

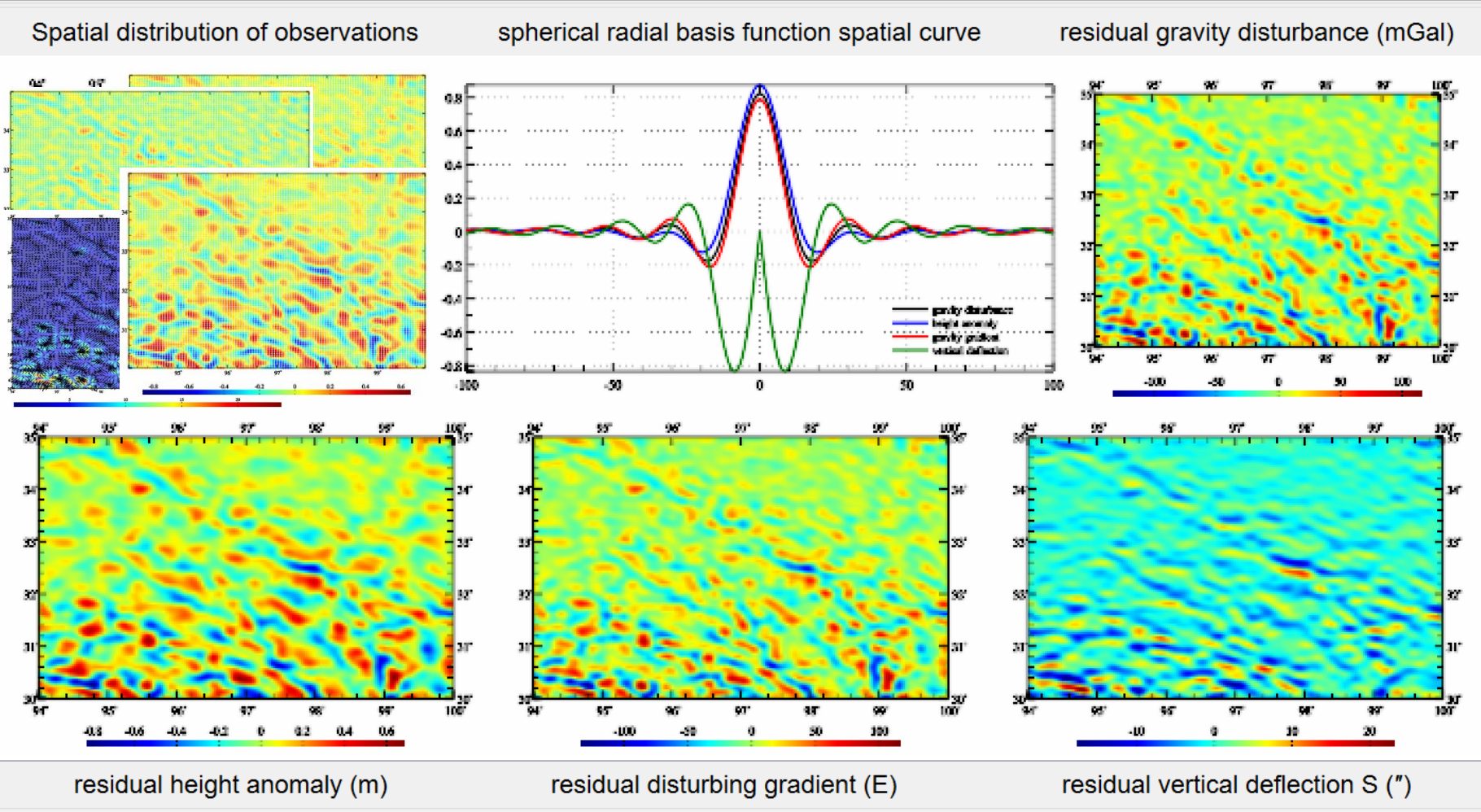
ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	94.02500	30.02500	3984.353	-75.3276	-0.4299	-75.1955	-146.9135	-1.9322
2	94.07500	30.02500	4226.989	-71.6500	-0.4020	-71.5266	-139.8571	-2.6832
3	94.12500	30.02500	4461.719	-43.8418	-0.2569	-43.7629	-80.4556	-3.2131
4	94.17500	30.02500	4422.914	-12.8478	-0.0850	-12.8217	-17.3550	-3.4320
5	94.22500	30.02500	4335.893	-0.2777	0.0058	-0.2795	0.3683	-2.9123
6	94.27500	30.02500	4463.689	2.7811	0.0482	2.7663	-0.0568	-1.8134

Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot Plot →

- The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.
- The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



Gross error detection on gravity field observations using SRBFs



Open the discrete heterogeneous residual observations file

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 6

column ordinal number of weight: 7

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 240

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 3600

Select the adjustable observations: height anomaly (m)

Contribution rate κ of adjustable observations: 0.00

Open the ellipsoidal height grid file of calculation surface

of file header, whose format: observation type (0~5), source observation mean, standard deviation, minimum, maximum, residual observation, observation type, weight.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-25 16:25:00
 >> Complete the computation!
 >> Computation end time: 2024-09-25 16:29:50
 >> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.
 >> The program also outputs SRBF center file *center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Type 0 of source observations: mean 0.3186 standard deviation 42.1772 minimum -296.0915 maximum 165.2611
 ** Residual observations: mean -0.4618 standard deviation 14.2512 minimum -105.2839 maximum 114.8811
 >> Type 1 of source observations: mean -0.3510 standard deviation 0.2774 minimum -0.9982 maximum 0.3435
 ** Residual observations: mean -0.0071 standard deviation 0.0304 minimum -0.2012 maximum 0.0560

Solution of normal equation: LU triangular decomposition

Save the results as | Import setting parameters | Start Computation

ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	101.50417	24.00417	-35.528	-26.2771	-0.4064	-26.1521	-10.5599	9.6630
2	101.51250	24.00417	-35.519	-36.4613	-0.4660	-36.3179	-30.7007	10.6422
3	101.52083	24.00417	-35.510	-43.6889	-0.5135	-43.5309	-43.1617	11.1978
4	101.52917	24.00417	-35.501	-52.5093	-0.5673	-52.3348	-59.6165	11.9721
5	101.53750	24.00417	-35.491	-63.5877	-0.6289	-63.3943	-82.2191	12.7411
6	101.54583	24.00417	-35.481	-64.5397	-0.6507	-64.3395	-78.0353	12.4595

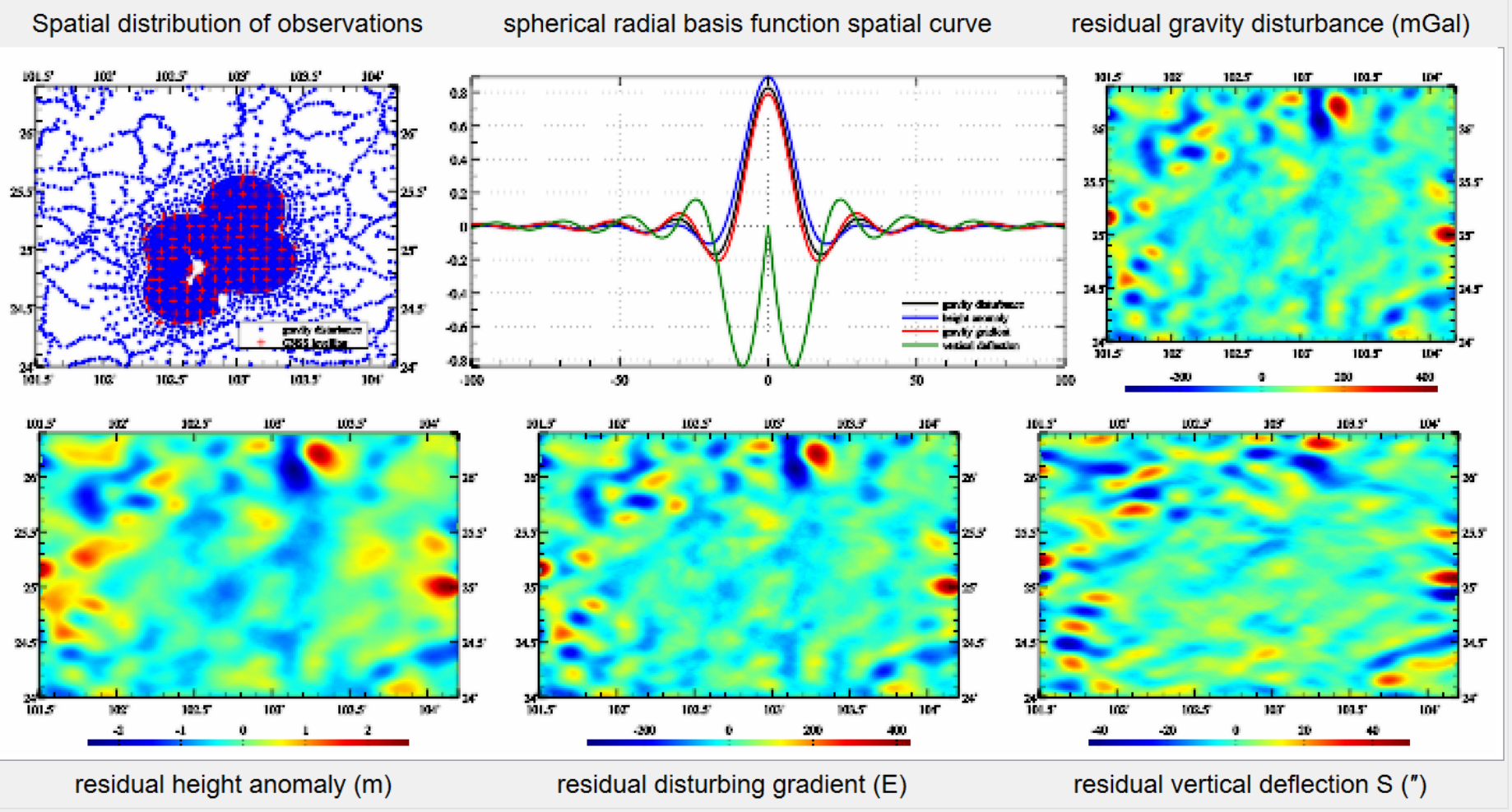
Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot | Plot →

The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.

The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



Measurement of height datum difference using SRBFs



Open the discrete heterogeneous residual observations file

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 6

column ordinal number of weight: 7

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 240

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 3600

Select the adjustable observations: height anomaly (m)

Contribution rate κ of adjustable observations: 0.00

Open the ellipsoidal height grid file of calculation surface

of file header, whose format: observation type (0~5), source observation mean, standard deviation, minimum, maximum, residual observation, observation standard deviation, minimum, maximum. The record format: ID, longitude, latitude, ellipsoidal height, residual observation, source observation, observation type, weight.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-25 16:34:12
 >> Complete the computation!
 >> Computation end time: 2024-09-25 16:39:29
 >> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.
 >> The program also outputs SRBF center file *center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Type 0 of source observations: mean 0.3071 standard deviation 42.0482 minimum -296.0915 maximum 165.2611
 ** Residual observations: mean -0.4584 standard deviation 13.6071 minimum -61.1040 maximum 64.8276
 >> Type 1 of source observations: mean -0.3443 standard deviation 0.2745 minimum -0.9982 maximum 0.3435
 ** Residual observations: mean -0.0070 standard deviation 0.0214 minimum -0.0729 maximum 0.0577

Solution of normal equation: LU triangular decomposition

Save the results as | Import setting parameters | Start Computation

ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	101.50417	24.00417	-35.528	-25.8111	-0.4050	-25.6865	-10.5496	9.1444
2	101.51250	24.00417	-35.519	-34.2343	-0.4580	-34.0934	-25.9194	10.0077
3	101.52083	24.00417	-35.510	-41.6971	-0.5069	-41.5412	-38.8251	10.6429
4	101.52917	24.00417	-35.501	-50.3166	-0.5602	-50.1443	-54.5962	11.4401
5	101.53750	24.00417	-35.491	-61.0024	-0.6207	-60.8115	-75.9916	12.2335
6	101.54583	24.00417	-35.481	-62.1031	-0.6435	-61.9052	-72.0511	12.0208

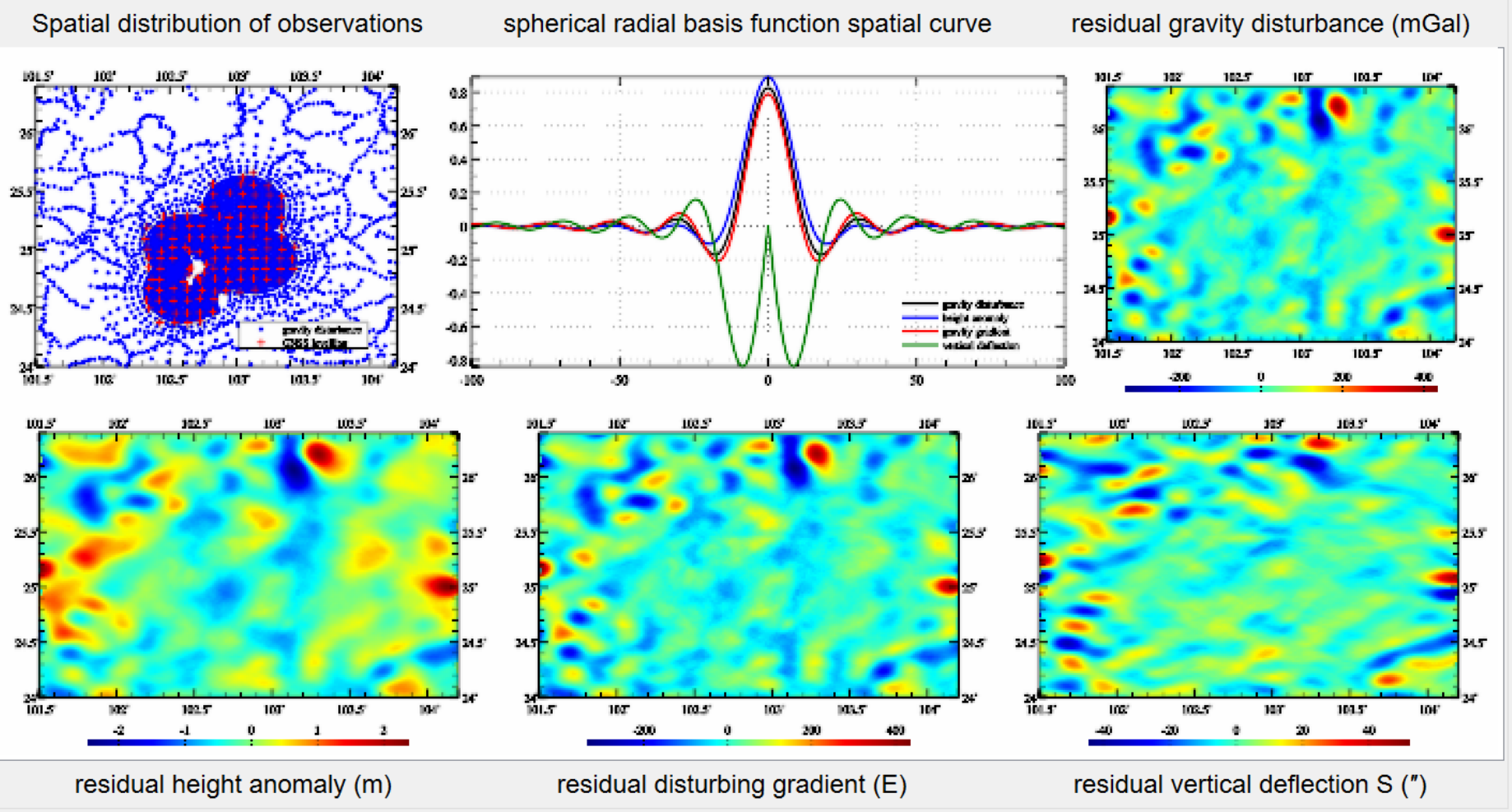
Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot | Plot →

The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.

The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



All-element modelling on gravity filed From observed gravity disturbance and GNSS-levelling geoidal height using SRBFs



Open the discrete heterogeneous residual observations file

number of rows of file header: 1

column ordinal number of ellipsoidal height in the record: 6

column ordinal number of weight: 7

Select SRBF: radial multipole kernel

Order m: 3

Minimum degree: 240

Maximum degree: 1800

Burial depth of Bjerhammar sphere: 10.0km

Action distance of SBRF center: 100km

Reuter network level K: 3600

Select the adjustable observations: height anomaly (m)

Contribution rate κ of adjustable observations: 1.00

Open the ellipsoidal height grid file of calculation surface

of file header, whose format: observation type (0~5), source observation mean, standard deviation, minimum, maximum, residual observation mean, standard deviation, minimum, maximum. The record format: ID, longitude, latitude, ellipsoidal height, residual observation, source observation, observation type, weight.

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-25 16:42:57
 >> Complete the computation!
 >> Computation end time: 2024-09-25 16:48:19
 >> The program outputs the all-element grid files into the current directory. These grid files include the residual gravity disturbance *.rga (mGal), residual height anomaly *.ksi (m), residual gravity anomaly *.gra (mGal), residual disturbing gravity gradient *.grr (E, radial) and residual vertical deflection vector *.dft (" SW), where * is the output file name, and whose grid specification are the same as the input ellipsoidal height grid of calculation surface.
 >> The program also outputs SRBF center file *center.txt into the current directory. The file header format: Reuter grid level, SRBF center number, cell grid number in meridian circle direction, maximum cell grid number in prime vertical circle direction, latitude interval ('). The record format: ID, longitude (degree decimal), geocentric latitude, cell grid area deviation percentage, longitude interval of cell grid in prime vertical circle direction (').

>> Type 0 of source observations: mean 0.3071 standard deviation 42.0482 minimum -296.0915 maximum 165.2611
 ** Residual observations: mean -0.2139 standard deviation 12.7187 minimum -60.1001 maximum 64.8276
 >> Type 1 of source observations: mean -0.0070 standard deviation 0.2745 minimum -0.6609 maximum 0.6808
 ** Residual observations: mean -0.0003 standard deviation 0.0232 minimum -0.0794 maximum 0.0535

Solution of normal equation LU triangular decomposition

Save the results as Import setting parameters Start Computation

ID	lon	lat	ellipshgt	gravity disturbance(mGal)	height anomaly(m)	gravity anomaly(mGal)	gravity gradient(E)	vertical deflection
1	101.50417	24.00417	-35.528	-36.3117	-0.3491	-36.2043	-45.0818	7.8888
2	101.51250	24.00417	-35.519	-43.6862	-0.3963	-43.5642	-57.7869	8.6648
3	101.52083	24.00417	-35.510	-50.4192	-0.4407	-50.2837	-68.8737	9.2166
4	101.52917	24.00417	-35.501	-58.7040	-0.4911	-58.5529	-83.8445	9.9607
5	101.53750	24.00417	-35.491	-68.0315	-0.5449	-67.8639	-101.6327	10.5899
6	101.54583	24.00417	-35.481	-69.9342	-0.5694	-69.7590	-99.7716	10.4463

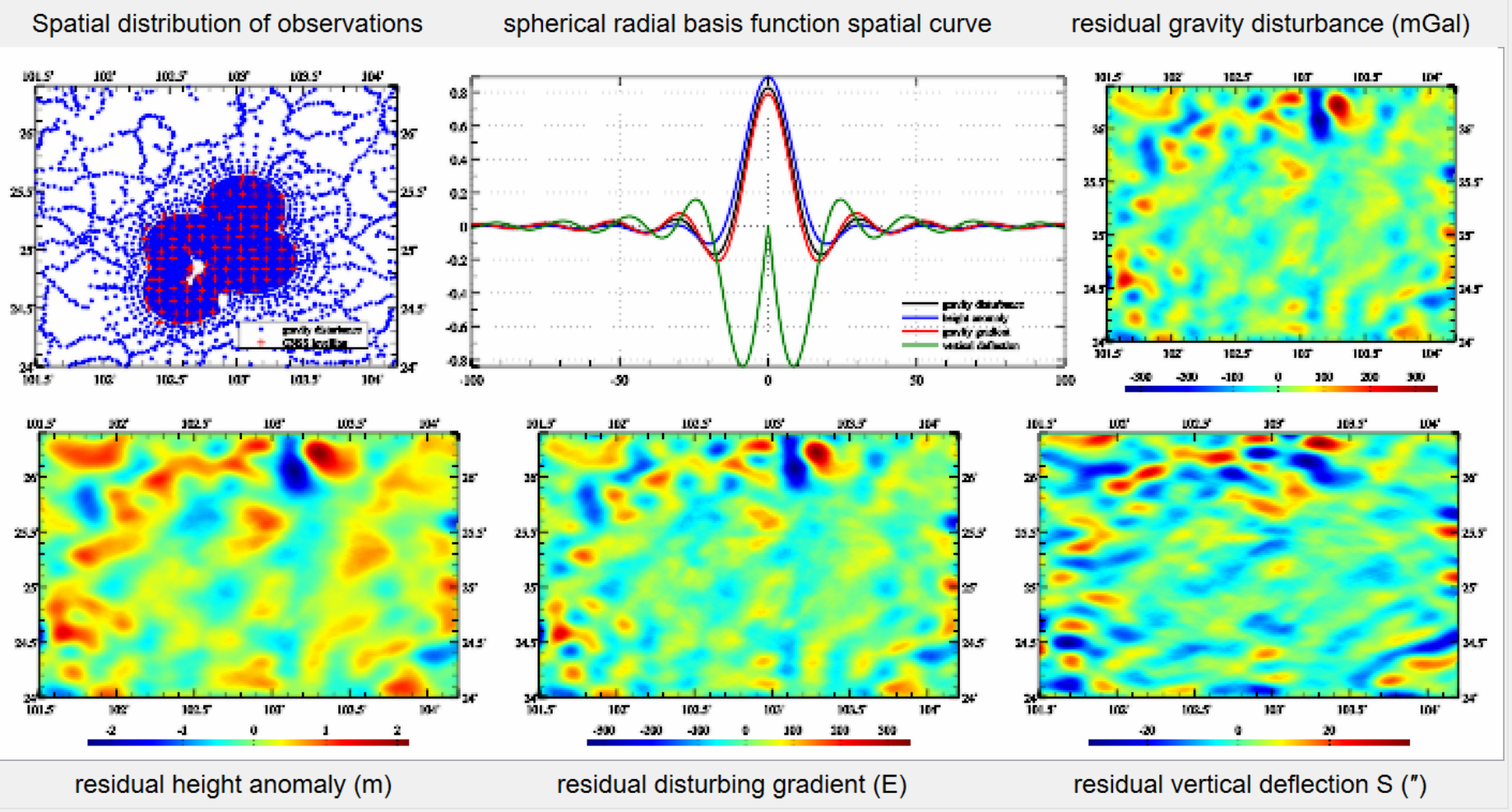
Algorithm of gravity field approach using SRBFs

- After the first estimation is completed, it is recommended to employ the output residual observation file *.chs as the input observation file again to refine target field elements. Generally, the stable solution can be achieved by 1 to 3 times cumulative SRBF approach, and the target field elements are equal to the sum of these SRBF approach solutions.
- The validity principle of once SRBF approach: (1) The residual target field element grid are continuous and differentiable, and whose standard deviation is as small as possible. (2) The statistical mean of residuals tends to zero with the increase of cumulative approach times, and there is no obvious reverse sign.

Extract data to be plot Plot →

The program is a high performance and adaptable modelling tool on local gravity field. Various observations with heterogeneity, different altitudes, cross-distribution and land-sea coexisting can be directly employed to estimate the all-element models of gravity field without reduction, continuation and gridding.

The program has strong capacity on the detection of observation gross errors, measurement of external accuracy indexes and control of computation performance.



Calculation of height difference correction of height anomaly from the geopotential model

Refinement of the height difference correction of height anomaly from regional observations

Calculation of the measured adjustment of height difference correction of height anomaly

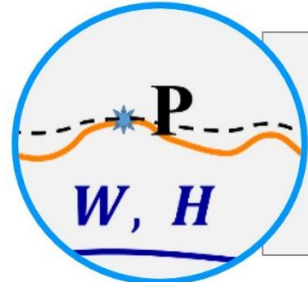
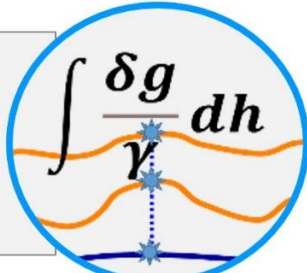
Assessment of gravimetric geoid using GNSS-levelling data

Calculation of geopotential of the zero-height surface for regional height datum

GNSS-levelling data fusion with constraints of the Poisson integral

Leveling network quasi-stable adjustment with remaining GNSS-levelling residuals

Calculation of height difference correction of height anomaly and height system difference



Construction and refinement of the equipotential surface passing through the specified point

Construction of the gravity equipotential surface from global geopotential model

Refinement of ellipsoidal height of the equipotential surface by local gravity field approach

Calculation of the model geopotential of the normal or orthometric equiheight surface

Refinement of the normal equiheight surface passing through specified point

Summation of the model values and residual values



Optimization, unification, and application computation for regional height datum

Construction of terrain equiheight surface passing through the specified point



GNSS replaces leveling to calculate the orthometric or normal height

Precise Approach of Earth Gravity Field and Geoid

PAGrav4.5

Chinese Academy of Surveying & Mapping

October 2024, Beijing, China

Calculation of height difference correction of height anomaly from the geopotential model

Calculation points Save as Import parameters Start Computation Save process Follow example

Calculation of height difference correction of height anomaly from the geopotential model

Refinement of the height difference correction of height anomaly from regional observations

Calculation of the measured adjustment of height difference correction of height anomaly

Analytic relationship between height systems

Open the calculation point position file

Set input point file format

number of rows of file header

column ordinal number of ellipsoidal height in the record

column ordinal number of target ellipsoidal height in the record

Open the geopotential coefficient model file

Maximum calculation degree for the geopotential model

>> Computation Process ** Operation Prompts

** Select the calculation mode from the three control buttons at the top of the interface.

>> [Function] From the ellipsoidal height of the calculation point and target point in near-Earth space, calculate the model value of radial gradient (cm/km) and height difference correction (m) of height anomaly using the reference geopotential model.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/calcpnt.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Open the geopotential coefficient model file C:/PAGravf4.5_win64en/data/EGM2008.gfc.

** The window below only shows the geopotential coefficients data with no more than 2000 rows in it

>> Save the results as C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/mdldiffst.txt.

** Behind the source calculation point file record, appends a column of radial gradient of height anomaly and a column of model height difference correction of height anomaly, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-29 14:40:55

>> Complete to Calculate the model height difference correction of height anomaly!

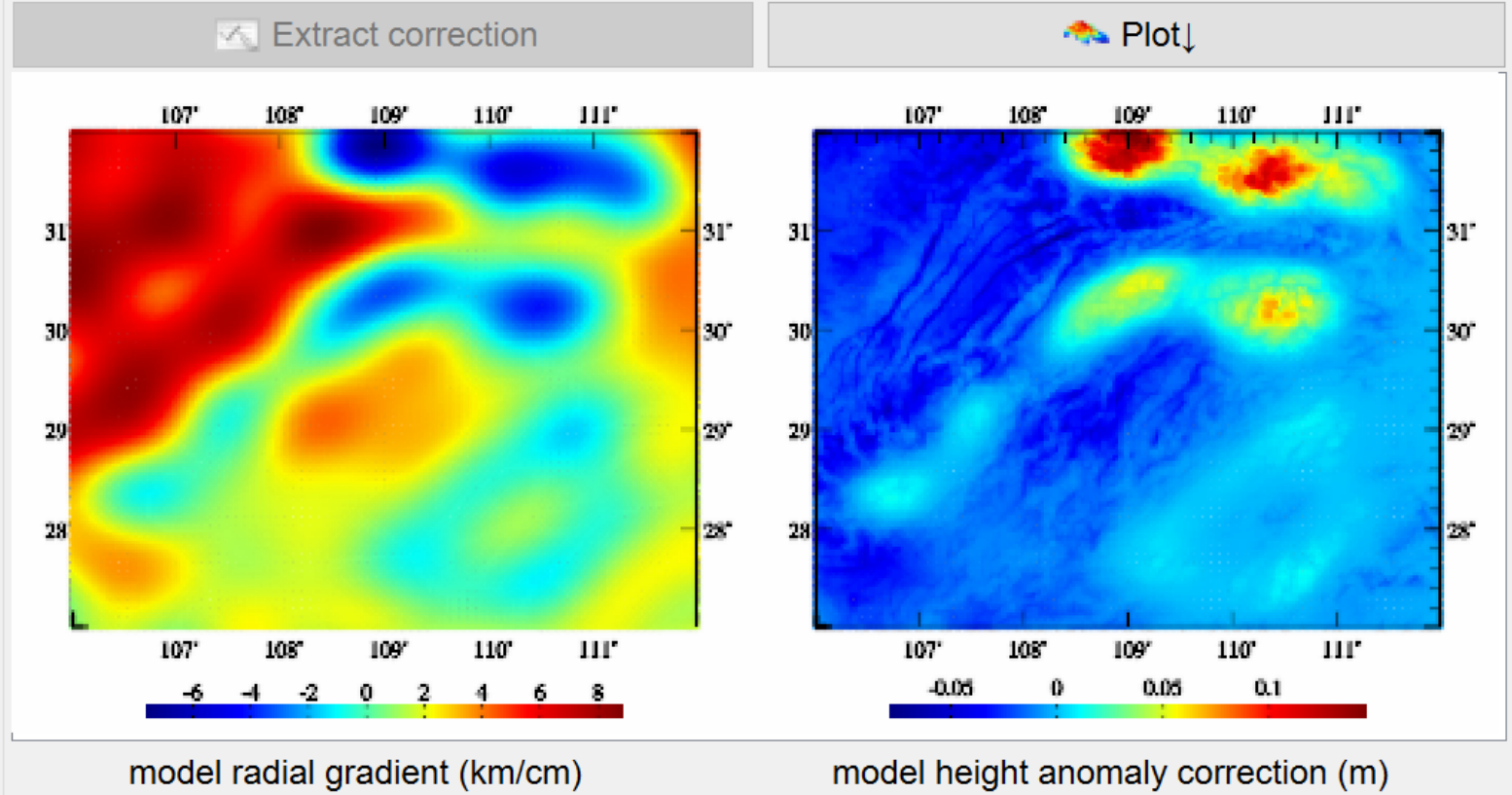
>> Computation end time: 2024-09-29 14:43:24

Save the results as

Import setting parameters

Start Computation

on (degree/decimal)	lat	ellipHeight (m)	geoidheight (m)		
11569	106.020833	27.020833	1217.221	-30.8082	0.6721 -0.0084
11570	106.062500	27.020833	1201.227	-30.8052	0.8284 -0.0102
11571	106.104167	27.020833	1185.247	-30.7849	0.9847 -0.0120
11572	106.145833	27.020833	1210.287	-30.7411	1.1368 -0.0141
11573	106.187500	27.020833	1228.340	-30.6802	1.2800 -0.0161
11574	106.229167	27.020833	1247.396	-30.6183	1.4102 -0.0180
11575	106.270833	27.020833	1244.440	-30.5729	1.5240 -0.0194
11576	106.312500	27.020833	1199.469	-30.5503	1.6184 -0.0199
11577	106.354167	27.020833	1183.494	-30.5360	1.6906 -0.0205
11578	106.395833	27.020833	1109.535	-30.4998	1.7396 -0.0198
11579	106.437500	27.020833	1000.613	-30.4157	1.7646 -0.0182
11580	106.479167	27.020833	1135.735	-30.2841	1.7631 -0.0206
11581	106.520833	27.020833	1249.869	-30.1357	1.7393 -0.0223
11582	106.562500	27.020833	1251.986	-30.0096	1.6959 -0.0217
11583	106.604167	27.020833	1289.077	-29.9216	1.6347 -0.0216
11584	106.645833	27.020833	1292.154	-29.8523	1.5599 -0.0206
11585	106.687500	27.020833	1228.242	-29.7662	1.4754 -0.0186
11586	106.729167	27.020833	1211.352	-29.6471	1.3857 -0.0172
11587	106.770833	27.020833	1339.471	-29.5138	1.2962 -0.0177
11588	106.812500	27.020833	1366.572	-29.4022	1.2100 -0.0160



- When the calculation point is on the ground and the target point is on the geoid, the program calculates the difference between the normal height and orthometric height, that is, the difference between the geoidal height and height anomaly.
- Height difference correction of height anomaly (m) = model correction, or model correction + residual correction, or model correction + residual correction + measured adjustment.
- Radial gradient of height anomaly (cm/km) = model radial gradient, or model radial gradient+ residual radial gradient, or model radial gradient+ residual radial gradient + measured adjustment.

Refinement of the height difference correction of height anomaly from regional observations

Calculation points Save as Import parameters Start Computation Save process Follow example

Calculation of height difference correction of height anomaly from the geopotential model

Refinement of the height difference correction of height anomaly from regional observations

Calculation of the measured adjustment of height difference correction of height anomaly

Analytic relationship between height systems

Open the calculation point position file

>> Computation Process ** Operation Prompts

Save computation process as

Set input point file format

number of rows of file header

column ordinal number of ellipsoidal height in the record

column ordinal number of target ellipsoidal height in the record

>> [Function] From the ellipsoidal height of the equipotential surface and residual gravity disturbance grid on the surface, calculate the residual radial gradient (cm/km) of the height anomaly at the current calculation point and residual height difference correction (m) of height anomaly at the target point relative to the current point.

** The residual gravity disturbance should be calculated using the remove-restore scheme with the geopotential model and terrain effects in advance.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/mdldiffrst.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Open residual gravity disturbance grid file on equipotential surface C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/dwmchrga.dat.

>> Open the ellipsoidal height grid file of the equipotential surface C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/dwmhgt150s.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/rntdiffrst.txt.

** Behind the record of the source calculation point file, appends a column of the residual radial gradient and a column of the residual height difference correction, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-29 14:49:23

>> Complete to Calculate residual height difference correction of height anomaly!

Open residual gravity disturbance grid file on the equipotential surface

Open the ellipsoidal height grid file of the equipotential surface

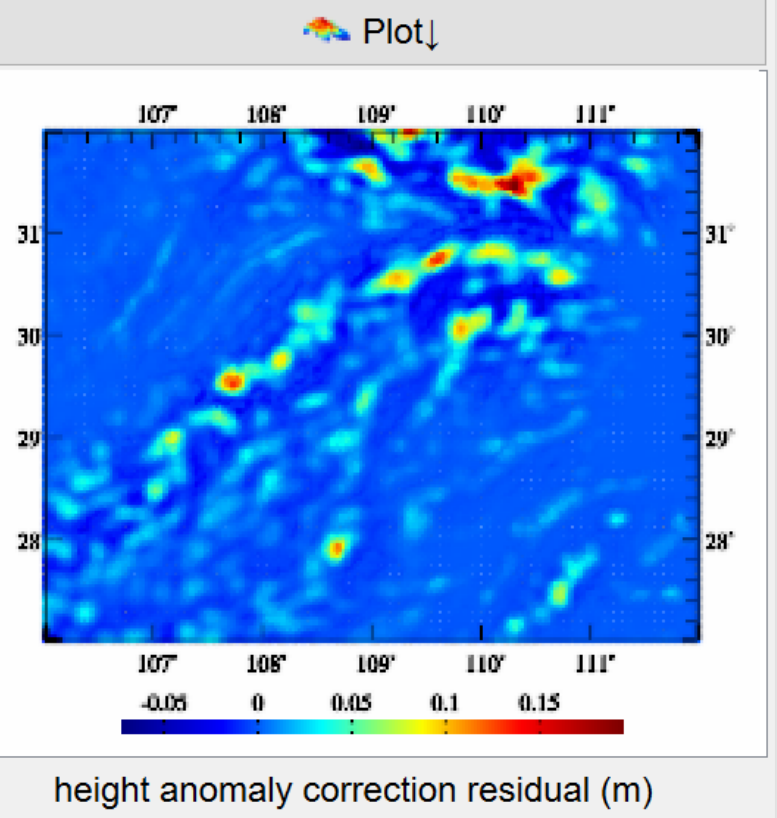
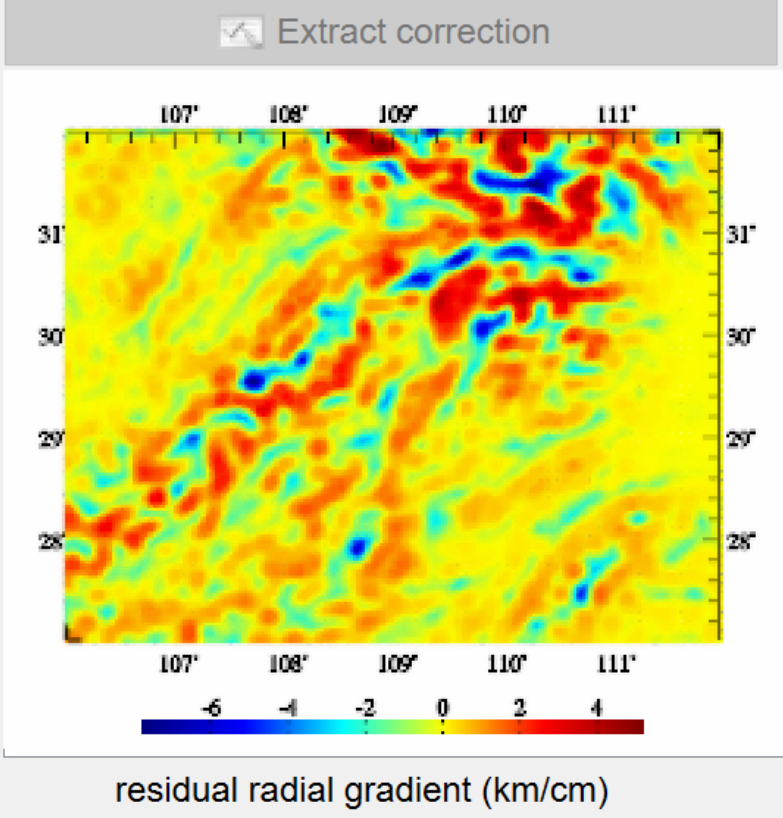
Residual integral radius

Save the results as

Import setting parameters

Start Computation

lipHeight (m)	geoidheight (m)				
0833	1217.221	-30.8082	0.6721	-0.0084	1.0239
0833	1201.227	-30.8052	0.8284	-0.0102	1.1014
0833	1185.247	-30.7849	0.9847	-0.0120	1.0145
0833	1210.287	-30.7411	1.1368	-0.0141	0.7312
0833	1228.340	-30.6802	1.2800	-0.0161	0.3232
0833	1247.396	-30.6183	1.4102	-0.0180	-0.0278
0833	1244.440	-30.5729	1.5240	-0.0194	-0.1268
0833	1199.469	-30.5503	1.6184	-0.0199	0.0985
0833	1183.494	-30.5360	1.6906	-0.0205	0.4995
0833	1109.535	-30.4998	1.7396	-0.0198	0.7431
0833	1000.613	-30.4157	1.7646	-0.0182	0.5545
0833	1135.735	-30.2841	1.7631	-0.0206	-0.0312
0833	1249.869	-30.1357	1.7393	-0.0223	-0.7351
0833	1251.986	-30.0096	1.6959	-0.0217	-1.1215
0833	1289.077	-29.9216	1.6347	-0.0216	-1.0465
0833	1292.154	-29.8523	1.5599	-0.0206	-0.7523
0833	1228.242	-29.7662	1.4754	-0.0186	-0.6524
0833	1211.352	-29.6471	1.3857	-0.0172	-0.9549
0833	1339.471	-29.5138	1.2962	-0.0177	-1.4728



- When the calculation point is on the ground and the target point is on the geoid, the program calculates the difference between the normal height and orthometric height, that is, the difference between the geoidal height and height anomaly.
- Height difference correction of height anomaly (m) = model correction, or model correction + residual correction, or model correction + residual correction + measured adjustment.
- Radial gradient of height anomaly (cm/km) = model radial gradient, or model radial gradient+ residual radial gradient, or model radial gradient+ residual radial gradient + measured adjustment.

Calculation of the measured adjustment of height difference correction of height anomaly

Calculation of height difference correction of height anomaly from the geopotential model

Refinement of the height difference correction of height anomaly from regional observations

Calculation of the measured adjustment of height difference correction of height anomaly

Analytic relationship between height systems

Open the calculation point position file

>> Computation Process ** Operation Prompts

Save computation process as

Set input point file format

number of rows of file header

column ordinal number of ellipsoidal height in the record

column ordinal number of target ellipsoidal height in the record

column ordinal number of remaining residual gravity disturbance

disturbance at the calculation point, respectively, to obtain the remaining residual measured gravity disturbance, and then calculate the measured adjustment (cm/km) for radial gradient correction at the calculation point and measured adjustment (m) for the height difference correction at the target point relative to the current calculation point.

** When there is the measured gravity data at the calculation point, this function can furtherly refine the radial gradient and the height difference correction of height anomaly.

>> Open the calculation point position file C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/calcpnt1.txt.

** Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5_win64en/examples/AppHgtsysdifferent/msrdiffadj.txt.

** Behind the record of the source calculation point file, appends a column of the adjustment of radial gradient of the height anomaly (cm/km) and a column of the adjustment of residual height anomaly difference (m), and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-29 14:55:34

>> Complete to Calculate measured adjustment for height anomaly difference correction!

>> Computation end time: 2024-09-29 14:55:35

Save the results as

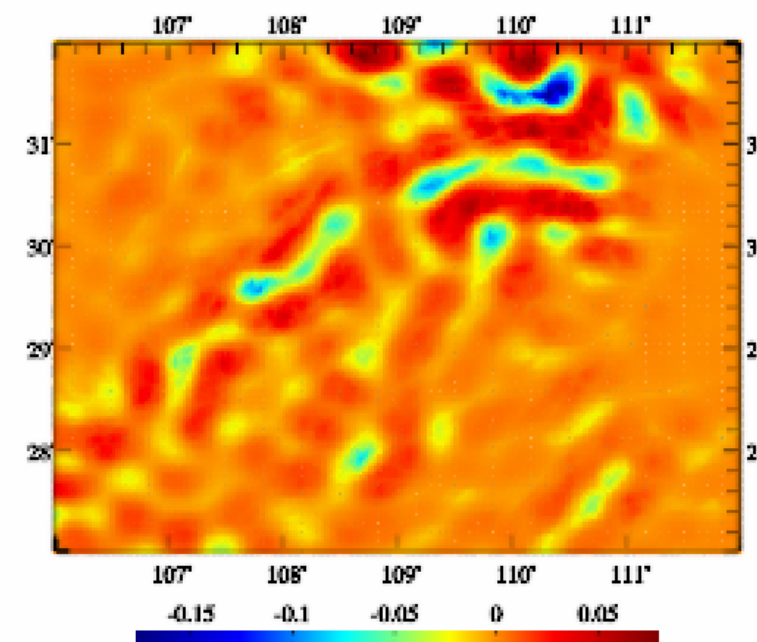
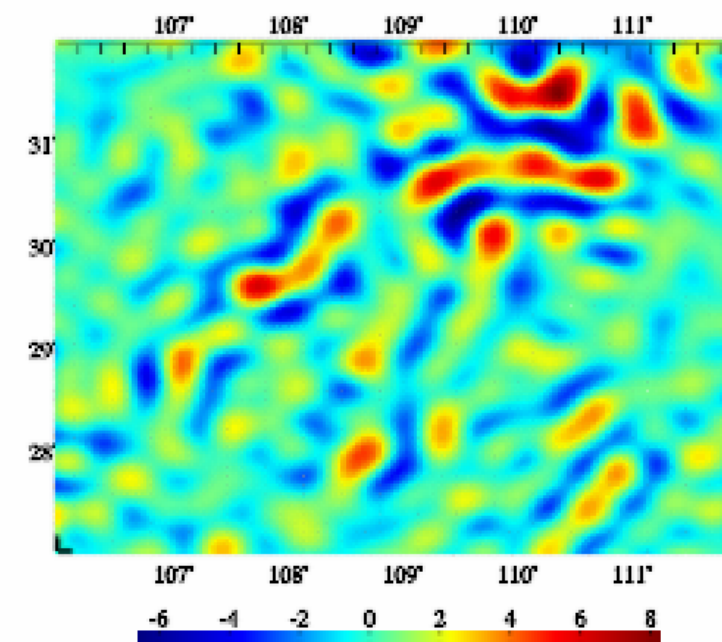
Import setting parameters

Start Computation

imal)	lat	ellipHeight(m)	geoidheight(m)			
0833	27.020833	1217.221	-30.8082	-2.9245	-0.2988	0.0037
2500	27.020833	1201.227	-30.8052	-3.4086	-0.3483	0.0043
4167	27.020833	1185.247	-30.7849	-4.4859	-0.4583	0.0056
5833	27.020833	1210.287	-30.7411	-5.8152	-0.5942	0.0074
7500	27.020833	1228.340	-30.6802	-7.0104	-0.7163	0.0090
9167	27.020833	1247.396	-30.6183	-7.7486	-0.7917	0.0101
0833	27.020833	1244.440	-30.5729	-7.8581	-0.8029	0.0102
2500	27.020833	1199.469	-30.5503	-7.3323	-0.7492	0.0092
4167	27.020833	1183.494	-30.5360	-6.2472	-0.6383	0.0077
5833	27.020833	1109.535	-30.4998	-4.8362	-0.4941	0.0056
7500	27.020833	1000.613	-30.4157	-3.2595	-0.3330	0.0034
9167	27.020833	1135.735	-30.2841	-1.5451	-0.1579	0.0018
0833	27.020833	1249.869	-30.1357	0.1969	0.0201	-0.0003
2500	27.020833	1251.986	-30.0096	2.0516	0.2096	-0.0027
4167	27.020833	1289.077	-29.9216	4.1339	0.4224	-0.0056
5833	27.020833	1292.154	-29.8523	6.4704	0.6611	-0.0087
7500	27.020833	1228.242	-29.7662	8.9864	0.9182	-0.0116
9167	27.020833	1211.352	-29.6471	11.3191	1.1565	-0.0144
0833	27.020833	1339.471	-29.5138	12.8393	1.3119	-0.0180

Extract correction

Plot



measured adjustment (km/cm) for radial gradient measured adjustment (m) for height anomaly correction

When the calculation point is on the ground and the target point is on the geoid, the program calculates the difference between the normal height and orthometric height, that is, the difference between the geoidal height and height anomaly.

Height difference correction of height anomaly (m) = model correction, or model correction + residual correction, or model correction + residual correction + measured adjustment.

Radial gradient of height anomaly (cm/km) = model radial gradient, or model radial gradient+ residual radial gradient, or model radial gradient+ residual radial gradient + measured adjustment.

Construction of the gravity equipotential surface from global geopotential model

Grid range Save as Import parameters Start Computation Save process Follow example



Construction of the gravity equipotential surface from global geopotential model

Refinement of ellipsoidal height of the equipotential surface by local gravity field approach

Save computation process as **PAGrav4.5**

- Open the equipotential surface range grid file
- Open the geopotential coefficient model file

Input geodetic coordinates of the specified point

longitude	110.24560000°
latitude	27.46720000°
ellipsoidal height	1346.0240 m

Maximum calculation degree for the geopotential model: 360

Save the model gravity grid as

Save model ellipsoidal height as

>> [Purpose] Firstly, calculate the model ellipsoidal height value of the gravity equipotential surface from the reference geopotential model, and then furtherly refine the ellipsoidal height grid of the equipotential surface from the anomalous field element grid using the remove-restore scheme.

** Select the function module the two control buttons at the top left of the interface...

>> [Function] From the geopotential coefficient model, calculate the model gravity (mGal) and model ellipsoidal height (m) grid of the gravity equipotential surface passing through the specified points (B, L, H).

>> The equipotential surface range grid file is only employed to give the latitude and longitude range and resolution of the surface grid.

>> Open the equipotential surface range grid file C:/PAGrav4.5_win64en/examples/AppEquipotentialhgt/areagrid.dat.

>> Open the geopotential coefficient model file C:/PAGrav4.5_win64en/data/EGM2008.gfc.

** The window below only shows the geopotential coefficients data with no more than 2000 rows in it

>> Save the model gravity grid as C:/PAGrav4.5_win64en/examples/AppEquipotentialhgt/eqpmdlgrav.dat.

>> Save model ellipsoidal height as C:/PAGrav4.5_win64en/examples/AppEquipotentialhgt/eqpmdlhgt.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

** The program needs to iteratively calculate the model ellipsoidal height grid of the equipotential surface, please wait...

>> Computation start time: 2024-09-26 10:12:29

>> Complete to calculate the model equipotential surface!

>> Computation end time: 2024-09-26 10:18:35

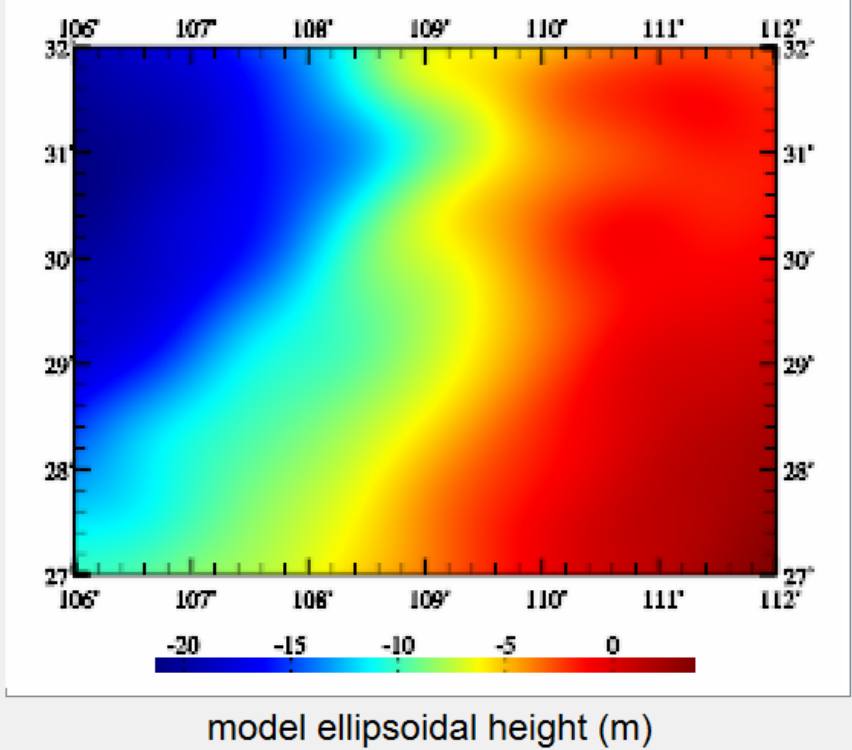
Import setting parameters

Start Computation

Extract results

Plot

106.000000	112.000000	27.000000	32.000000	0.04166667	0.04166667	110.245600	27.467200	1346.0240
-10.0529	-10.0392	-10.0236	-10.0051	-9.9829	-9.9563	-9.9245	-9.8870	-9.8433
-9.3656	-9.2779	-9.1876	-9.0958	-9.0034	-8.9112	-8.8202	-8.7311	-8.6444
-8.1236	-8.0587	-7.9944	-7.9300	-7.8645	-7.7974	-7.7277	-7.6550	-7.5785
-6.9202	-6.8099	-6.6966	-6.5808	-6.4632	-6.3442	-6.2243	-6.1039	-5.9834
-5.1467	-5.0271	-4.9068	-4.7855	-4.6630	-4.5390	-4.4135	-4.2863	-4.1574
-3.2228	-3.0881	-2.9540	-2.8210	-2.6891	-2.5586	-2.4296	-2.3020	-2.1759
-1.3199	-1.1990	-1.0782	-0.9572	-0.8364	-0.7157	-0.5956	-0.4763	-0.3582
0.3964	0.4892	0.5776	0.6616	0.7415	0.8176	0.8903	0.9602	1.0279
1.5026	1.5788	1.6585	1.7421	1.8295	1.9208	2.0157	2.1139	2.2152
2.9668	3.0750	3.1826	3.2896	3.3960	3.5020	3.6078	3.7138	3.8203
-10.1508	-10.1392	-10.1255	-10.1090	-10.0889	-10.0642	-10.0344	-9.9988	-9.9570
-9.4888	-9.4016	-9.3115	-9.2195	-9.1264	-9.0333	-8.9409	-8.8500	-8.7611
-8.2166	-8.1476	-8.0794	-8.0110	-7.9419	-7.8712	-7.7983	-7.7226	-7.6435
-6.9784	-6.8686	-6.7561	-6.6413	-6.5249	-6.4072	-6.2886	-6.1696	-6.0504
-5.2172	-5.0969	-4.9755	-4.8528	-4.7286	-4.6026	-4.4747	-4.3449	-4.2131
-3.2540	-3.1156	-2.9780	-2.8415	-2.7063	-2.5726	-2.4406	-2.3102	-2.1816
-1.3138	-1.1921	-1.0706	-0.9492	-0.8281	-0.7073	-0.5871	-0.4679	-0.3500



The ellipsoidal height on the equipotential surface = ellipsoidal height cell grid value + the 9th number of the file header.

The reference geopotential model and truncation degree should be consistent with that employed in the gravity field approach and modeling. The degree of the model should not be too large, since the program adopts the iterative approach method, which need take a long time.

Refinement of ellipsoidal height of the equipotential surface by local gravity field approach

Grid range Save as Import parameters Start Computation Save process Follow example



Construction of the gravity equipotential surface from global geopotential model

Refinement of ellipsoidal height of the equipotential surface by local gravity field approach

Save computation process as PAGravf4.5

Open the ellipsoidal height grid file of equipotential boundary surface

Open residual gravity disturbance grid file on equipotential boundary surface

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 ** The program needs to iteratively calculate the model ellipsoidal height grid of the equipotential surface, please wait...
 >> Computation start time: 2024-09-26 10:12:29
 >> Complete to calculate the model equipotential surface!
 >> Computation end time: 2024-09-26 10:18:35
 >> [Function] From the ellipsoidal height of some an equipotential boundary surface and residual gravity disturbance as well as the calculated model gravity and model ellipsoidal height grid, refine the ellipsoidal height grid of the equipotential surface passing through the specified points (B, L, H) by the Hotine integral.

Input geodetic coordinates of the specified point

longitude	110.24560000°
latitude	27.46720000°
ellipsoidal height	1346.0240 m

>> Open the ellipsoidal height grid file of equipotential boundary surface C:/PAGravf4.5_win64en/examples/AppEquipotentialhgt/dwmhgt150s.dat.
 >> Open residual gravity disturbance grid file on equipotential boundary surface C:/PAGravf4.5_win64en/examples/AppEquipotentialhgt/dwmchrqa.dat.
 >> Save the refined ellipsoidal height as C:/PAGravf4.5_win64en/examples/AppEquipotentialhgt/equiphgt.dat.

Residual integral radius 150 km

>> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-26 10:20:31
 >> Complete to refine the equipotential surface!
 >> Computation end time: 2024-09-26 10:21:26

Save the refined ellipsoidal height as

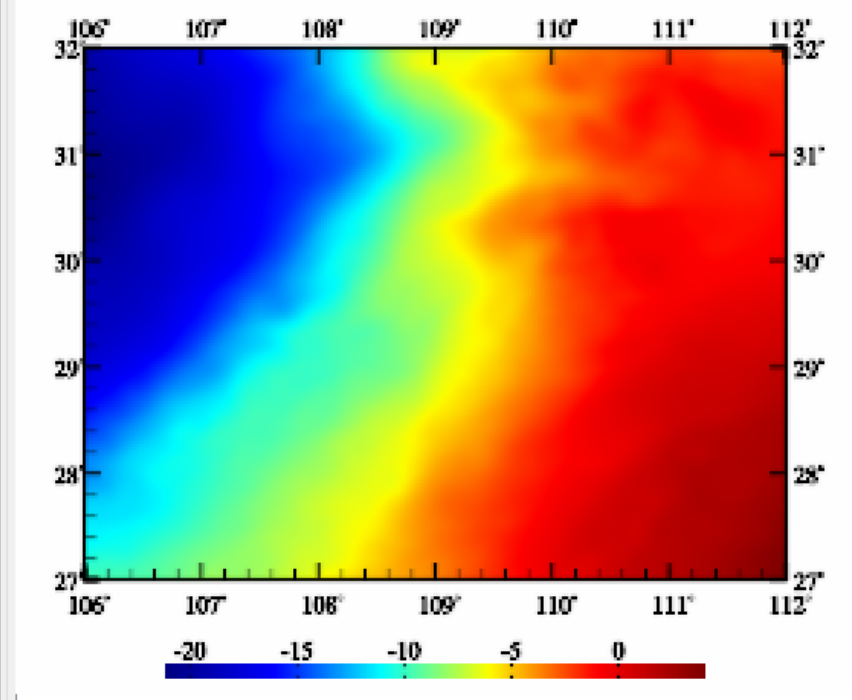
Import setting parameters

Start Computation

Extract results

Plot↓

106.000000	112.000000	27.000000	32.000000	0.04166667	0.04166667	110.245600	27.467200	1346.0240
-9.6403	-9.6443	-9.6467	-9.6462	-9.6406	-9.6273	-9.6032	-9.5669	-9.5208
-9.1660	-9.0790	-8.9978	-8.9173	-8.8238	-8.7084	-8.5749	-8.4350	-8.2981
-7.9639	-7.9709	-7.9473	-7.9062	-7.8620	-7.8149	-7.7491	-7.6488	-7.5115
-6.5600	-6.4462	-6.3183	-6.1804	-6.0460	-5.9275	-5.8257	-5.7279	-5.6184
-4.7827	-4.6604	-4.5335	-4.4115	-4.3023	-4.2089	-4.1285	-4.0531	-3.9727
-3.0571	-2.9117	-2.7694	-2.6272	-2.4820	-2.3336	-2.1854	-2.0406	-1.9001
-1.0710	-0.9617	-0.8332	-0.6892	-0.5431	-0.4106	-0.3046	-0.2279	-0.1726
0.5669	0.7171	0.8630	1.0002	1.1257	1.2382	1.3365	1.4183	1.4814
1.8049	1.8752	1.9554	2.0440	2.1346	2.2210	2.3026	2.3850	2.4751
3.1803	3.2720	3.3713	3.4850	3.6114	3.7393	3.8539	3.9489	4.0316
-9.7964	-9.7842	-9.7745	-9.7686	-9.7638	-9.7548	-9.7352	-9.7004	-9.6513
-9.2316	-9.1478	-9.0730	-9.0001	-8.9140	-8.8060	-8.6794	-8.5442	-8.4073
-8.0621	-8.0694	-8.0356	-7.9777	-7.9178	-7.8617	-7.7956	-7.7013	-7.5729
-6.6486	-6.5430	-6.4234	-6.2909	-6.1590	-6.0421	-5.9438	-5.8519	-5.7471
-4.8237	-4.7029	-4.5764	-4.4504	-4.3332	-4.2313	-4.1455	-4.0694	-3.9921
-3.1132	-2.9632	-2.8161	-2.6711	-2.5251	-2.3761	-2.2254	-2.0753	-1.9266
-1.0365	-0.9339	-0.8088	-0.6635	-0.5123	-0.3728	-0.2580	-0.1718	-0.1090



ellipsoidal height refined (m)

- The ellipsoidal height on the equipotential surface = ellipsoidal height cell grid value + the 9th number of the file header.
- The reference geopotential model and truncation degree should be consistent with that employed in the gravity field approach and modeling. The degree of the model should not be too large, since the program adopts the iterative approach method, which need take a long time.

Calculation of the model geopotential of the normal or orthometric equiheight surface



Input position of the specified point

longitude: 110.24560000°
 latitude: 27.46720000°
 normal or orthometric height: 1346.0240 m

Maximum calculation degree for the geopotential model: 360

Height system: normal height system

>> [Purpose] Firstly, calculate the model geopotential of the normal or orthometric equiheight surface from the reference gravity field model, and then furtherly refine the geopotential from the anomalous field element grid using the remove-restore scheme.

** Select the function module the 3 control buttons at the top of the interface...

>> [Function] From the geopotential coefficient model, calculate the model geopotential, model ellipsoidal height (m) and model gravity (mGal) grid of the normal or orthometric equiheight surface passing through the specified point (B, L).

>> The equiheight surface range grid file is only employed to give the latitude and longitude range and resolution of the surface grid.

>> Open the equiheight surface range grid file C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/areagrid.dat.

>> Open the geopotential coefficient model file C:/PAGravf4.5_win64en/data/EGM2008.gfc.

** The window below only shows the geopotential coefficients data with no more than 2000 rows in it

>> Save the model gravity grid as C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/eqhgtmdlgrav.dat.

>> Save the model geopotential grid as C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/eqhmpotential.dat.

>> Save the model ellipsoidal height as C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/eqhgtmdlhgt.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

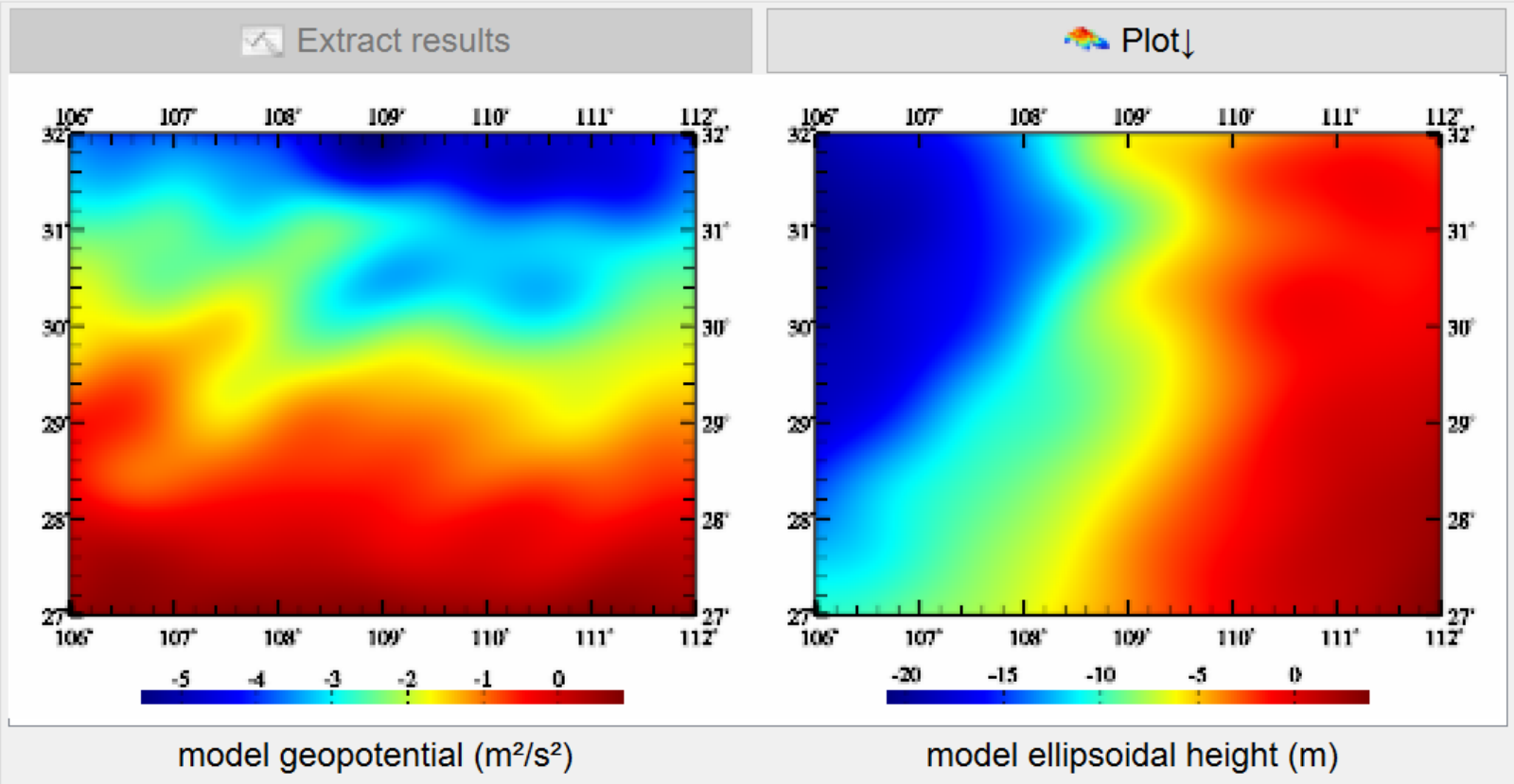
** The program needs to iteratively calculate the model geopotential grid of the equiheight surface, please wait...

>> Computation start time: 2024-09-26 10:29:19

>> Complete to calculate the model equiheight surface!

>> Computation end time: 2024-09-26 10:37:47

106.000000	112.000000	27.000000	32.000000	0.04166667	0.04166667
-47.0779	-48.5710	-50.0626	-51.5117	-52.8773	-54.1205
-55.6160	-54.8211	-53.9773	-53.1293	-52.3217	-51.5968
-53.7911	-54.8783	-56.0160	-57.1638	-58.2815	-59.3310
-61.6286	-61.0857	-60.4887	-59.8692	-59.2583	-58.6846
-57.8114	-58.0957	-58.3711	-58.6137	-58.8012	-58.9143
-54.9842	-54.2986	-53.6328	-53.0050	-52.4305	-51.9211
-50.1814	-50.1167	-50.0220	-49.8912	-49.7219	-49.5160
-48.2901	-48.6244	-49.0894	-49.6836	-50.3996	-51.2246
-59.9952	-60.3345	-60.5051	-60.5073	-60.3479	-60.0403
-54.5244	-54.3209	-54.2460	-54.2972	-54.4654	-54.7357
-43.9476	-45.5158	-47.0858	-48.6168	-50.0682	-51.4013
-53.8577	-53.1327	-52.3463	-51.5418	-50.7621	-50.0484
-51.4914	-52.4531	-53.4667	-54.4949	-55.5002	-56.4472
-58.5753	-58.0995	-57.5792	-57.0436	-56.5213	-56.0383
-55.7158	-55.9891	-56.2396	-56.4438	-56.5801	-56.6301
-51.6479	-50.8404	-50.0538	-49.3070	-48.6162	-47.9938
-45.3853	-45.2636	-45.1176	-44.9411	-44.7319	-44.4920
-43.3261	-43.7170	-44.2496	-44.9224	-45.7282	-46.6537
-56.7661	-57.2295	-57.5125	-57.6128	-57.5353	-57.2914



The model ellipsoidal height = the cell grid value in the model ellipsoidal height grid file + 9th number of the file header. The model gravity = the cell grid value in the model gravity grid file + 10th number of the file header. The ellipsoidal height = the model ellipsoidal height + correction of the height. The gravity = the model gravity + correction of the gravity.

Refinement of the normal equiheight surface passing through specified point



Input position of the specified point

longitude 110.24560000°
 latitude 27.46720000°
 normal or orthometric height 1346.0240 m

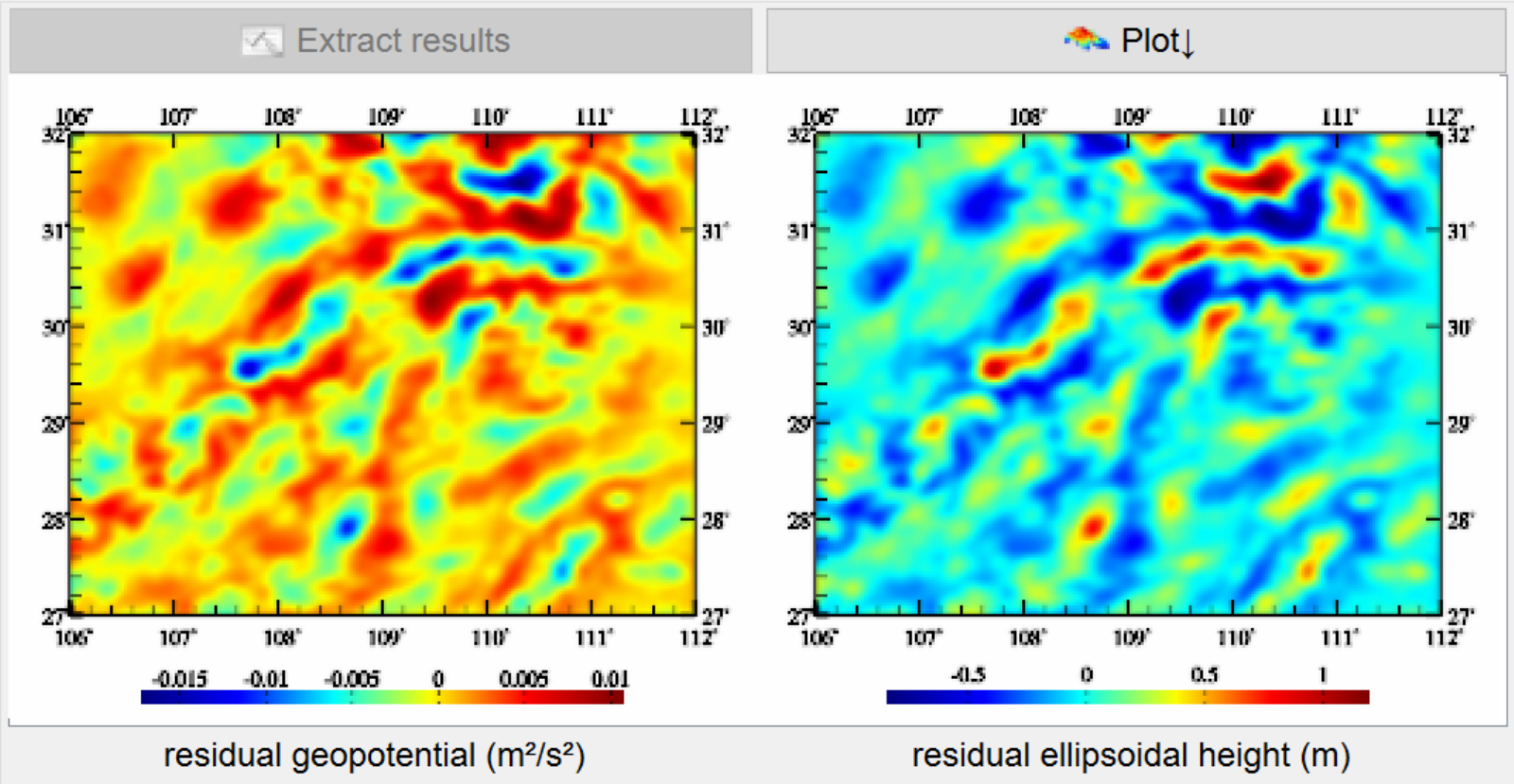
Residual integral radius 150 km

Height system normal height system

```

** The program needs to iteratively calculate the model geopotential grid of the equiheight surface, please wait...
>> Computation start time: 2024-09-26 10:29:19
>> Complete to calculate the model equiheight surface!
>> Computation end time: 2024-09-26 10:37:47
>> [Function] From the ellipsoidal height of some an equipotential boundary surface and residual gravity disturbance on the surface as well as the calculated model gravity and model ellipsoidal height grid, refine the ellipsoidal height grid of the normal or orthometric equiheight surface passing through the specified point (B, L) by the Hotine integral.
>> Open the ellipsoidal height grid file of equipotential boundary surface C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/dwmhgt150s.dat.
>> Open residual gravity disturbance grid file on equipotential boundary surface C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/dwmchrga.dat.
>> Save geopotential correction grid as C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/eqhpotentadj.dat.
>> Save ellipsoidal height corrections as C:/PAGravf4.5_win64en/examples/AppEquihgtpotential/eqhgtadj.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-26 10:41:14
>> Complete to refine the equiheight surface!
>> Computation end time: 2024-09-26 10:42:34
    
```

106.000000	112.000000	27.000000	32.000000	0.04166667	0.04166667
-47.0779	-48.5710	-50.0626	-51.5117	-52.8773	-54.1205
-55.6160	-54.8211	-53.9773	-53.1293	-52.3217	-51.5968
-53.7911	-54.8783	-56.0160	-57.1638	-58.2815	-59.3310
-61.6286	-61.0857	-60.4887	-59.8692	-59.2583	-58.6846
-57.8114	-58.0957	-58.3711	-58.6137	-58.8012	-58.9143
-54.9842	-54.2986	-53.6328	-53.0050	-52.4305	-51.9211
-50.1814	-50.1167	-50.0220	-49.8912	-49.7219	-49.5160
-48.2901	-48.6244	-49.0894	-49.6836	-50.3996	-51.2246
-59.9952	-60.3345	-60.5051	-60.5073	-60.3479	-60.0403
-54.5244	-54.3209	-54.2460	-54.2972	-54.4654	-54.7357
-43.9476	-45.5158	-47.0858	-48.6168	-50.0682	-51.4013
-53.8577	-53.1327	-52.3463	-51.5418	-50.7621	-50.0484
-51.4914	-52.4531	-53.4667	-54.4949	-55.5002	-56.4472
-58.5753	-58.0995	-57.5792	-57.0436	-56.5213	-56.0383
-55.7158	-55.9891	-56.2396	-56.4438	-56.5801	-56.6301
-51.6479	-50.8404	-50.0538	-49.3070	-48.6162	-47.9938
-45.3853	-45.2636	-45.1176	-44.9411	-44.7319	-44.4920
-43.3261	-43.7170	-44.2496	-44.9224	-45.7282	-46.6537
-56.7661	-57.2295	-57.5125	-57.6128	-57.5353	-57.2914



The model ellipsoidal height = the cell grid value in the model ellipsoidal height grid file + 9th number of the file header. The model gravity = the cell grid value in the model gravity grid file + 10th number of the file header. The ellipsoidal height = the model ellipsoidal height + correction of the height. The gravity = the model gravity + correction of the gravity.

Assessment of gravimetric geoid using GNSS-levelling data

GNSS-levelling data Save as Import parameters Start Computation Save process Follow example

Precise Approach of Earth Gravity Field and Geoid
PAGrav4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Open GNSS-levelling residual height anomaly file

number of rows of file header

column ordinal number of residual height anomaly in the record

Input GNSS-levelling network parameters

mean distance between GNSS benchmarks

constant error of ellipsoidal height difference of the GNSS baseline

proportional error of ellipsoidal height difference of GNSS baseline

Set the error curve parameters

number of groups in the GNSS benchmarks combined in pairs

maximum distance of distance-error curve

distance interval for distance-error curve

>> Computation Process ** Operation Prompts

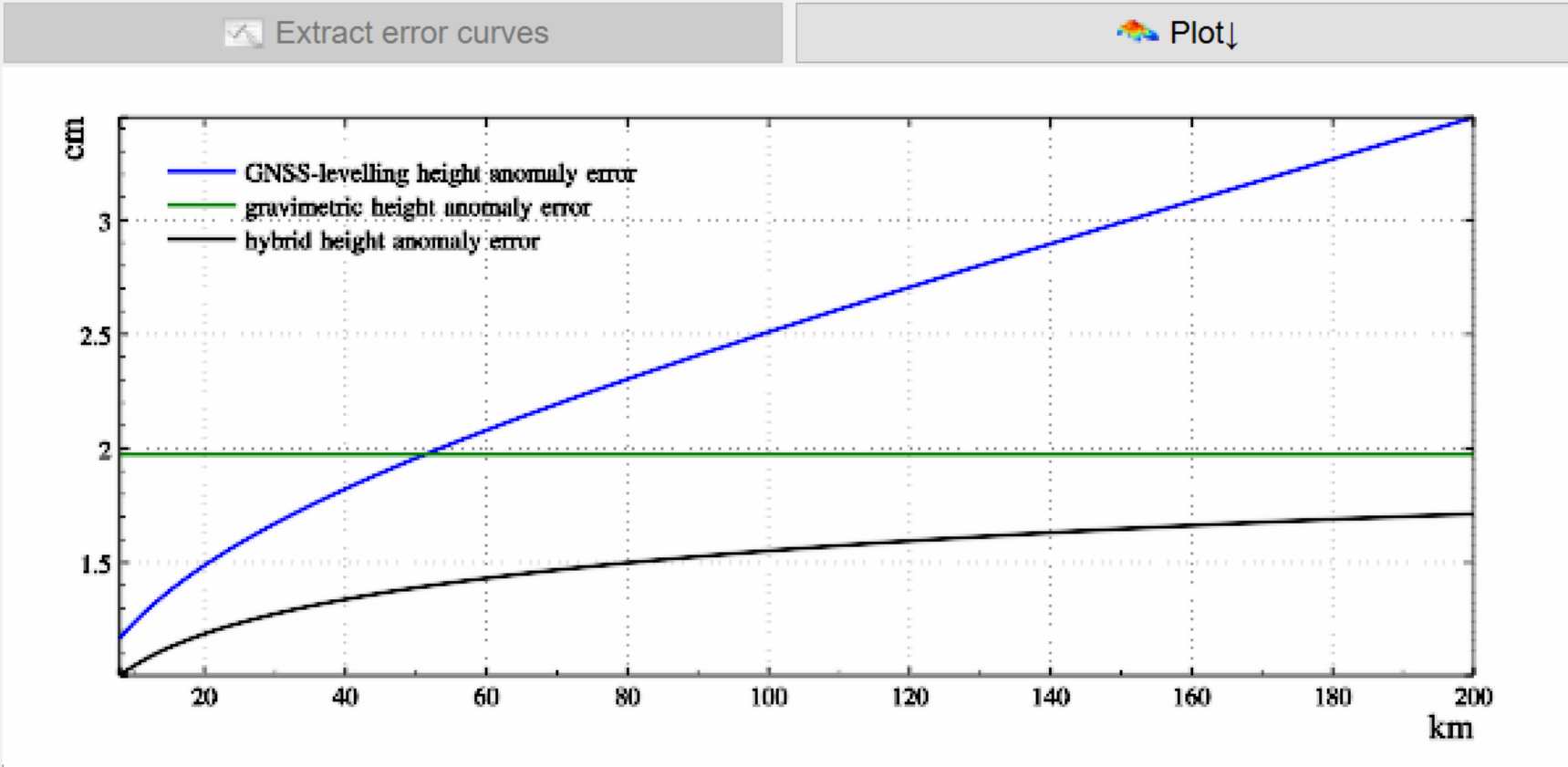
>> [Function] According to the spectral domain error characteristics of GNSS-levelling height anomaly and gravity field, statistically analyze the GNSS-levelling residual height anomalies (m), and then estimate the error (cm) of gravimetric height anomalies, inner coincidence error of hybrid height anomalies, error of hybrid height anomaly differences and error of GNSS-levelling height anomaly differences. Replacing the ground height anomaly with the geoidal height, the program can evaluate the gravimetric geoid of the orthometric system.

>> Open discrete GNSS-levelling residual height anomaly file C:/PAGrav4.5_win64en/examples/AppGeoiderrorestim/GNSSIksirent.txt.
** Look at the file information in the window below and set the discrete point file format parameters...

>> Save the results as C:/PAGrav4.5_win64en/examples/AppGeoiderrorestim/result.txt.
>> The file header consists of 5 parameters, which are the standard deviation of the GNSS-levelling residual height anomalies (cm), standard deviation of the differences of GNSS-levelling residual height anomalies after pairwise combination (cm), error of gravimetric height anomaly (cm), inner coincidence error (cm) of hybrid height anomaly differences, and normal (orthometric) height difference error per kilometer (cm/km).
>> The file record is employed to express 3 error curves: the first column is the distance (km, independent variable), the second column is the GNSS-levelling height anomaly error (cm), the third column is the gravimetric height anomaly error (cm, constant), and the fourth column is the coincidence error (cm) within the hybrid height anomalies.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-26 11:04:30
>> Complete the assessment of gravimetric geoid!

Save the error curves as Import setting parameters Start Computation

3.07963	4.32820	1.97371	1.56767	0.56426
8	1.16838	1.97371	1.00542	
9	1.20333	1.97371	1.02743	
10	1.23594	1.97371	1.04751	
11	1.26659	1.97371	1.06597	
12	1.29556	1.97371	1.08307	
13	1.32308	1.97371	1.09900	
14	1.34933	1.97371	1.11390	
15	1.37447	1.97371	1.12792	
16	1.39860	1.97371	1.14114	
17	1.42185	1.97371	1.15366	
18	1.44428	1.97371	1.16555	
19	1.46599	1.97371	1.17687	
20	1.48702	1.97371	1.18767	
21	1.50745	1.97371	1.19800	
22	1.52732	1.97371	1.20790	
23	1.54667	1.97371	1.21741	
24	1.56555	1.97371	1.22655	
25	1.58398	1.97371	1.23535	
26	1.60199	1.97371	1.24384	
27	1.61963	1.97371	1.25204	
28	1.63690	1.97371	1.25996	



- GNSS-levelling residuals: the differences between the measured GNSS-levelling height anomalies and the gravimetric height anomalies in the normal height system, and the differences between the measured GNSS-levelling geoidal heights and the gravimetric geoidal heights in the orthometric system.
- The basis for the accuracy evaluation of the geoid here: the error of the differences of the GNSS-levelling measured height anomalies between two points increases with the increase of the distance, while the error of the differences of the gravimetric height anomalies between the two points does not change significantly with the change of the distance.

Calculation of geopotential of the zero-height surface for regional height datum

GNSS-levelling residuals Save as Import parameters Start Computation Save process Follow example

Calculation of geopotential of the zero-height surface for regional height datum

GNSS-levelling data fusion with constraints of the Poisson integral

Leveling network quasi-stable adjustment with remaining GNSS-levelling residuals



Open discrete GNSS-levelling residuals file

Set input file format

number of rows of file header

Column ordinal number of the GNSS-levelling observation

column ordinal number of GNSS-levelling residual

column ordinal number of weight

Input geopotential of global zero-height surface (m^2/s^2)

>> Computation Process ** Operation Prompts

>> Open discrete GNSS-levelling residual file C:/PAGrav4.5_win64en/examples/AppGNSSlvhgtdatum/GNSSlrntksi.txt.

** Look at the file information in the window below and set the discrete point file format parameters...

>> Save the remaining GNSS-levelling residuals as C:/PAGrav4.5_win64en/examples/AppGNSSlvhgtdatum/rntksich.txt.

** The file header has 6 attributes, namely W_r , U_0 , W_0 , $W_r - U_0$, $W_r - W_0$ and $U_0 - W_0$, where W_r is the zero-height surface geopotential of the regional height datum, U_0 is the normal geopotential of the level ellipsoidal surface which is equal to the geopotential of the gravimetric geoid, and W_0 is the geopotential of the global geoid considered as the global orthometric (normal) zero-height surface.

** Behind the record of the GNSS-levelling residual file, appends a column of correction after reduction to gravimetric geoid, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-26 11:14:15

Geopotential of regional zero-height surface $W_r = 62636850.846m^2/s^2$
 Geopotential of global gravimetric geoid $U_0 = 62636858.709m^2/s^2$
 Geopotential of global zero-height surface $W_0 = 62636853.400m^2/s^2$
 Geopotential difference of regional zero-height surface relative to global geoid $W_r - U_0 = -7.863m^2/s^2$
 Geopotential difference of regional zero-height surface relative to global zero-height surface $W_r - W_0 = -2.554m^2/s^2$
 Geopotential difference of global gravimetric geoid relative to global zero-height $U_0 - W_0 = 5.309m^2/s^2$

>> Complete to calculate the geopotential differences of height datum!

Save the remaining GNSS-levelling residuals as

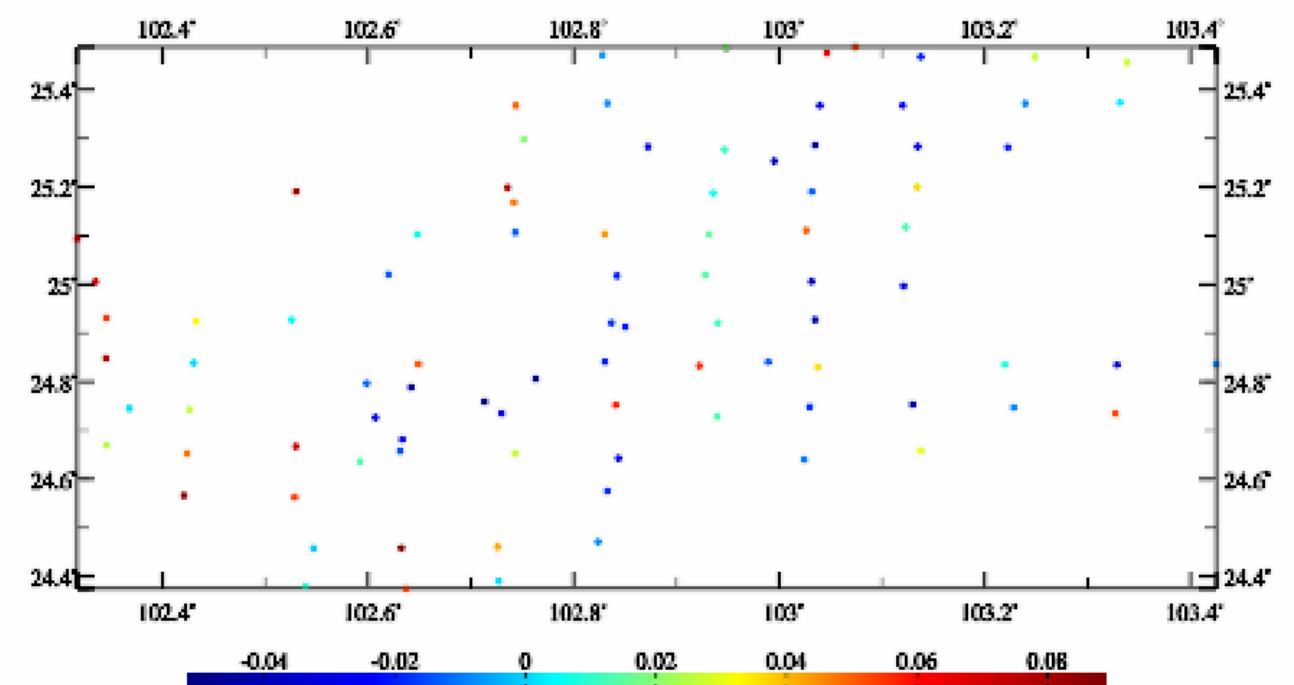
Import setting parameters

Start Computation

no	lon(degree/decimal)	lat	ellipHeight(m)	geoidheight(m)	resksi	weight
	62636850.846	62636858.709	62636853.400	-7.8630	-2.5542	5.3088
2	102.546777	24.458002	1659.0410	-33.6150	-0.8046	0.94
3	102.632412	24.458211	2120.2558	-33.3212	-0.7142	1.23
4	102.725921	24.460578	2111.3872	-33.2058	-0.7612	1.68
5	102.420803	24.566357	1990.6386	-33.5334	-0.7157	1.95
6	102.528697	24.562786	1936.4260	-33.3720	-0.7491	2.93
9	102.832641	24.575505	1977.4949	-33.1581	-0.8223	1.04
10	102.345532	24.668953	1919.7825	-33.7565	-0.7782	3.53
11	102.423972	24.652933	1959.3369	-33.4781	-0.7548	2.02
12	102.529771	24.667079	2157.7877	-33.2933	-0.7317	1.46
13	102.631063	24.657055	1906.3415	-33.3155	-0.8185	3.53
14	102.742718	24.652871	1935.7882	-33.1128	-0.7767	3.39
15	102.843573	24.642787	1880.7707	-33.1133	-0.8319	0.81
16	103.137778	24.658224	1838.4387	-32.7463	-0.7730	0.53
17	102.426305	24.743284	1929.0475	-33.4575	-0.7771	1.48
20	102.729945	24.734909	1856.2213	-33.2087	-0.8356	6.12
21	102.840819	24.752018	2117.8582	-32.8948	-0.7459	1.56
22	102.939253	24.728089	2050.9590	-32.8500	-0.7907	0.81
23	103.029713	24.748496	2034.1986	-32.8194	-0.8217	0.88
24	103.129600	24.753135	1575.0654	-32.8486	-0.8477	1.41

Extract remaining residuals

Plot



The data fusion surface for the normal height system is the ground, and the ground ellipsoidal height grid file should be input. The data fusion surface for the orthometric system is the geoid, and the geoidal height grid file should be input.

The remaining GNSS-levelling residual file after GNSS-levelling data fusion can be employed to evaluate the quality of the measured GNSS-levelling data.

GNSS-levelling data fusion with constraints of the Poisson integral

GNSS-levelling residuals Save as Import parameters Start Computation Save process Follow example

Calculation of geopotential of the zero-height surface for regional height datum

GNSS-levelling data fusion with constraints of the Poisson integral

Leveling network quasi-stable adjustment with remaining GNSS-levelling residuals



Open discrete GNSS-levelling residuals file

Set input file format

number of rows of file header

Column ordinal number of the ellipsoidal height

column ordinal number of GNSS-levelling residual

column ordinal number of weight

Open the ellipsoidal height grid file of the data fusion surface

Set calculation parameters

Iterative calculation times

Residual integral radius

Set Laplace operator parameter

Edge effect suppressing parameter

>> Computation Process ** Operation Prompts

```
>> Open discrete GNSS-levelling residual file C:/PAGravf4.5_win64en/examples/AppGNSSlvhgtdatum/rntksich.txt.
** Look at the file information in the window below and set the discrete point file format parameters...
>> Open the ellipsoidal height grid file of the data fusion surface C:/PAGravf4.5_win64en/examples/AppGNSSlvhgtdatum/GeoidEGM150s.dat.
>> Save the remaining GNSS-levelling residuals as C:/PAGravf4.5_win64en/examples/AppGNSSlvhgtdatum/rntksich01.txt.
>> Save the remaining residual grid results as C:/PAGravf4.5_win64en/examples/AppGNSSlvhgtdatum/residualgeoid.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
** The iterative calculation process needs to wait... During the period, you can open the file C:/PAGravf4.5_win64en/examples/AppGNSSlvhgtdatum/rntksich01.txt and look at the iterative calculation progress!
>> Computation start time: 2024-09-26 11:25:11
>> GNSS-levelling residuals: mean, standard deviation, minimum, maximum
>> Source GNSS-levelling residuals: -0.7932 0.0369 -0.8550 -0.7142
>> the 1th iterative remaining residuals: 0.0024 0.0254 -0.0401 0.0663
>> the 2th iterative remaining residuals: 0.0024 0.0224 -0.0419 0.0655
>> the 3th iterative remaining residuals: 0.0022 0.0204 -0.0412 0.0607
>> the 4th iterative remaining residuals: 0.0020 0.0188 -0.0400 0.0557
>> the 5th iterative remaining residuals: 0.0018 0.0175 -0.0387 0.0511
>> Complete GNSS-levelling data fusion!
```

Save the remaining GNSS-levelling residuals as

Save the remaining residual grid results as

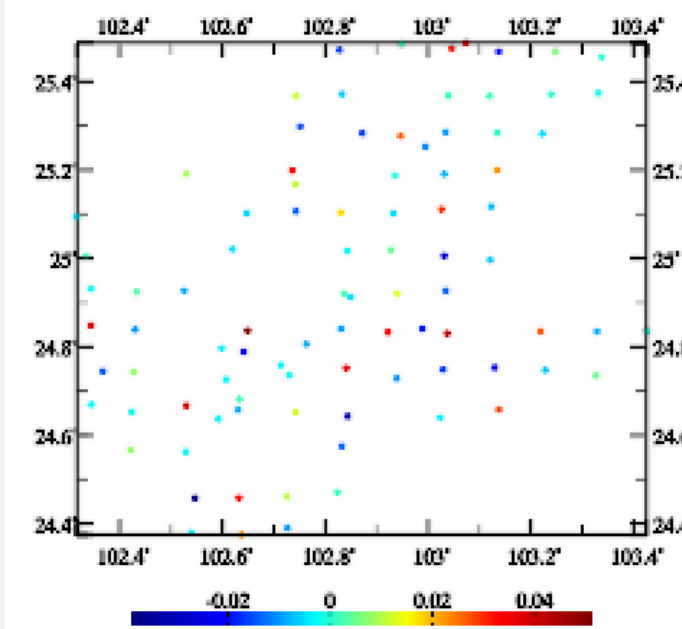
Import setting parameters

Start Computation

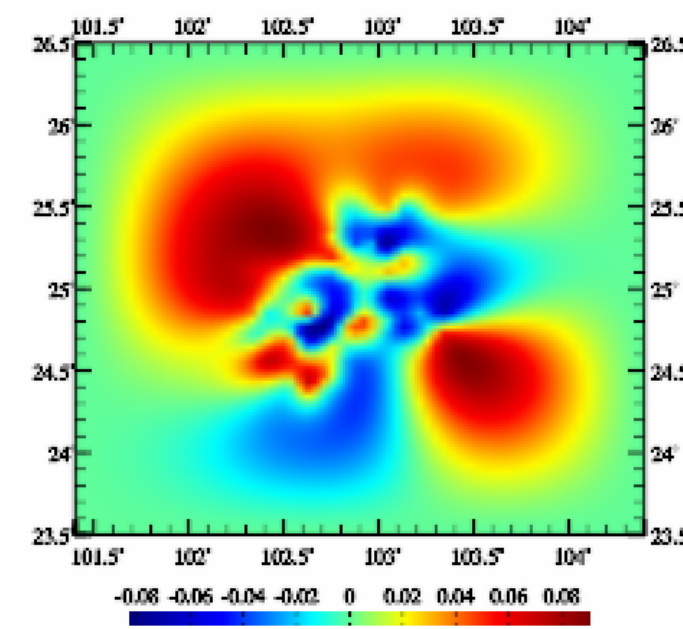
101.400000	104.400000	23.500000	26.500000	0.04166667	0.04166667	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000
-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000
0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000
-0.0003	-0.0004	-0.0004	-0.0005	-0.0005	-0.0006	-0.0006
-0.0009	-0.0009	-0.0009	-0.0009	-0.0009	-0.0008	-0.0007
0.0002	0.0003	0.0004	0.0005	0.0005	0.0006	0.0006
0.0004	0.0004	0.0003	0.0002	0.0002	0.0001	0.0001
0.0000	-0.0000	-0.0000	-0.0000	-0.0001	-0.0001	-0.0001
-0.0009	-0.0010	-0.0012	-0.0013	-0.0015	-0.0016	-0.0018
-0.0026	-0.0026	-0.0026	-0.0025	-0.0024	-0.0022	-0.0020
0.0005	0.0008	0.0011	0.0013	0.0015	0.0016	0.0017
0.0012	0.0010	0.0009	0.0007	0.0006	0.0004	0.0003
0.0000	-0.0000	-0.0000	-0.0001	-0.0001	-0.0002	-0.0003
-0.0017	-0.0020	-0.0022	-0.0025	-0.0028	-0.0031	-0.0034
-0.0050	-0.0049	-0.0048	-0.0047	-0.0045	-0.0042	-0.0038
0.0011	0.0016	0.0020	0.0024	0.0028	0.0031	0.0033

Extract fusion result grid

Plot



remaining residuals (m)



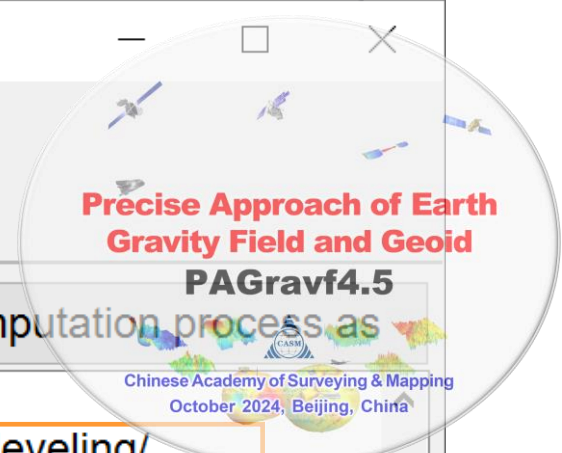
residual height anomaly (m)

The data fusion surface for the normal height system is the ground, and the ground ellipsoidal height grid file should be input. The data fusion surface for the orthometric system is the geoid, and the geoidal height grid file should be input.

The remaining GNSS-levelling residual file after GNSS-levelling data fusion can be employed to evaluate the quality of the measured GNSS-levelling data.

GNSS replaces leveling to calculate the orthometric (normal) height

Import parameters Start Computation Save process Follow example



Select height system

normal (orthometric) height

Multipoint calculation

Open ground height anomaly grid file

Open ground ellipsoidal height grid file

Open ground gravity disturbance grid file

Open the geoidal height grid file

>> Computation Process

>> GNSS replaces leveling to calculate both the normal height and orthometric height...

>> Open ground height anomaly grid file C:/PAGrav4.5_win64en/examples/AppGNSSreleveling/dbmGM1800150sksi.dat.

>> Open ground ellipsoidal height grid file C:/PAGrav4.5_win64en/examples/AppGNSSreleveling/dbmhgt150s.dat.

>> Open ground gravity disturbance grid file C:/PAGrav4.5_win64en/examples/AppGNSSreleveling/dbmGM1800150srga.dat.

>> Open the geoidal height grid file C:/PAGrav4.5_win64en/examples/AppGNSSreleveling/dwmGM1800150sksi.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-26 11:42:09

>> Computation end time: 2024-09-26 11:42:09

Input geodetic coordinates of GNSS positioning point

longitude 106.2500000°

latitude 28.4200000°

ellipsoidal height 321.0000m

The normal (orthometric) height calculated

normal height 355.3384m

orthometric height 355.3301m

Start Computation

Display of the input-output file ↓

104.000000	114.000000	25.000000	34.000000	0.04166667	0.04166667				
-30.3888	-30.3353	-30.2474	-30.1782	-30.1695		-30.4928	-30.6097	-30.6	
-30.5079	-30.4773	-30.4178	-30.3818	-30.4241		-30.8459	-30.8988	-30.8	
-30.9666	-30.9265	-30.8488	-30.7279	-30.56		-30.1897	-30.2039	-30.2	
-30.7087	-30.7124	-30.6640	-30.5747	-30		-30.2657	-30.1592	-30.0	
-29.4489	-29.3199	-29.2045	-29.0906	-28.6941		-28.6379	-28.6437	-28.6	
-28.0546	-27.9933	-27.9349	-27.8688	-27.5190		-27.3588	-27.2144	-27.1	
-26.6019	-26.6005	-26.6046	-26.601	-26.5548		-26.5268	-26.4927	-26.4	
-25.5602	-25.4324	-25.2871	-25.2	-24.4445		-24.3811	-24.3680	-24.3	
-24.0863	-23.9551	-23.8277	-23.7	-23.3871		-23.1946	-22.9939	-22.8	
-21.7590	-21.6183	-21.4670	-21.29	-20.9343		-20.9193	-20.9265	-20.9	
-20.2280	-20.0810	-19.9070	-19.72	-19.3250		-19.0671	-18.7527	-18.1	
-17.5519	-17.2803	-17.0668	-16.9249	-16.8241		-16.7266	-16.6149	-16.2	
-15.2983	-15.0905	-14.8649	-14.6429	-14.4439		-14.2719	-14.112	-13.5	
-12.8449	-12.8349	-12.7969	-12.7235	-12.6087		-12.4577	-12.2738	-11.9	
-10.8914	-10.7385	-10.5461	-10.2937	-10.1034		-9.8083	-9.6879	-9.4	

Save data in the text box as

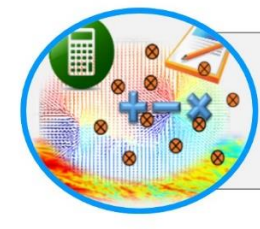
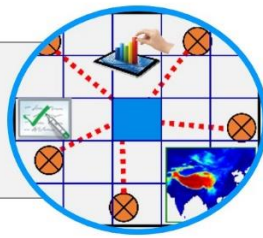
Changing of grid resolution by interpolation

Interpolating of geodetic site attribute from grid

Selecting of records based on an attribute condition

Separating of (vector) grid data to two different regions

Data interpolation, extracting and separation of land and sea



Simple and direct calculation on geodetic data files

Weighted operation on two specified attributes in record file

Weighted operation on two geodetic grid files

Weighted operation on two vector grid files

Weighted operation on two harmonic coefficient files



Gridding of discrete geodetic data by simple interpolation

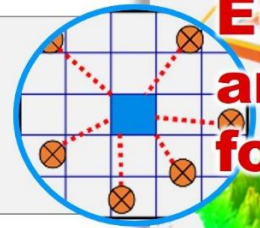
Gridding of high-resolution record attributes by direct averaging

Interpolation of vector grid from two attributes in geodetic records

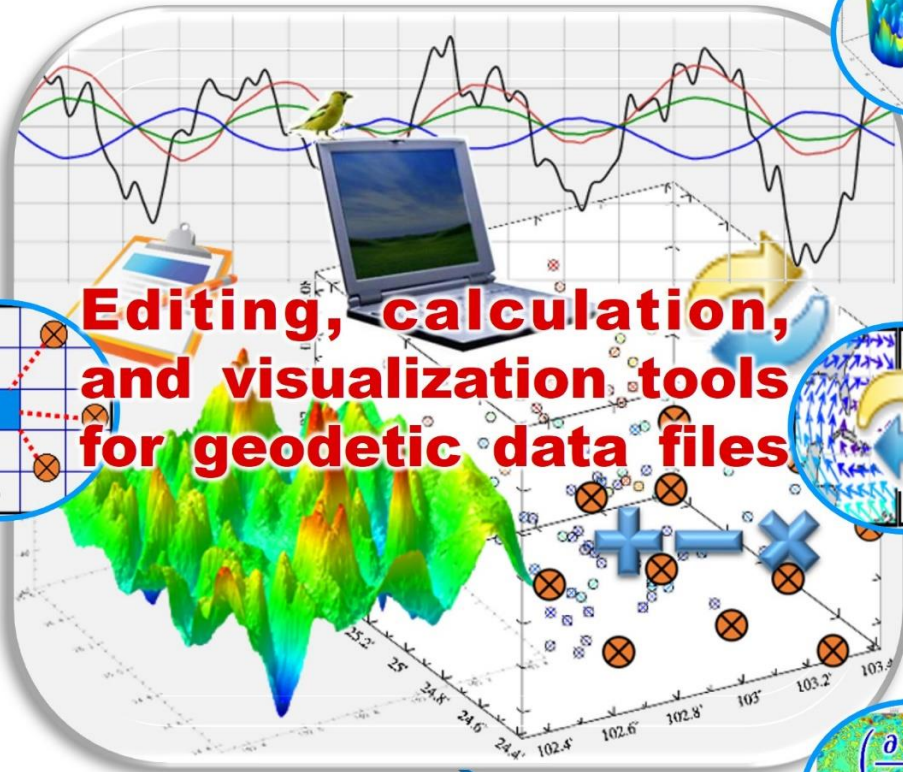
Constructing of general geodetic grid file

Extracting of data according to latitude and longitude range

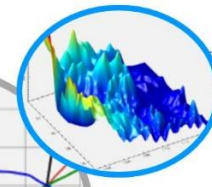
Simple gridding and regional geodetic grid construction



Editing, calculation, and visualization tools for geodetic data files



Low-pass filtering operation on geodetic grid file



Constructing and transforming of vector grid file

Combining of two grid files into a vector grid file

Decomposing of vector grid file into two grid files

Transforming of vector form for vector grid file

Converting of vector grid file into discrete point file

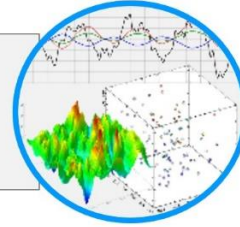
Visualization of multi-attributes curves from 2D geodetic data

Visualization for specified attribute in discrete point record file

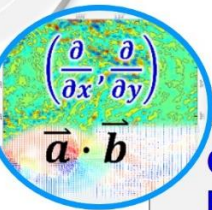
Visualization for the geodetic grid file

Visualization for the geodetic vector grid file

Visualization plot tools for various geodetic data files



Calculation of grid horizontal gradient and vector grid inner product



Horizontal gradient calculation on geodetic grid

Inner product operation on two vector grids

Converting of general ASCII records into PAGravf4.5 format 80



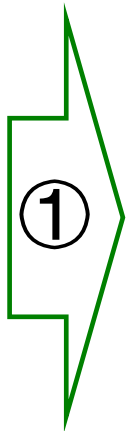
Statistical analysis on various geodetic data file



Converting of general ASCII records into PAGravf4.5 format

Open text file Save as Save process Follow example

62636844.042	62636851.905	62636853.400	-7.8630	-9.3578	-1.4948		
2	102.546777	24.458002	1659.0410	-33.6150	-0.8046	0.94	-0.0014
3	102.632412	24.458211	2120.2558	-33.3212	-0.7142	1.23	0.0890
4	102.725921	24.460578	2111.3872	-33.2058	-0.7612	1.68	0.0420
5	102.420803	24.566357	1990.6386	-33.5334	-0.7157	1.95	0.0875
6	102.528697	24.562786	1936.4260	-33.3720	-0.7491	2.93	0.0541
9	102.832641	24.575505	1977.4949	-33.1581	-0.8223	1.04	-0.0191
10	102.345532	24.668953	1919.7825	-33.7565	-0.7782	3.53	0.0250
11	102.423972	24.652933	1959.3369	-33.4781	-0.7548	2.02	0.0484
12	102.529771	24.667079	2157.7877	-33.2933	-0.7317	1.46	0.0715
13	102.631063	24.657055	1906.3415	-33.3155	-0.8185	3.53	-0.0153
14	102.742718	24.652871	1935.7882	-33.1128	-0.7767	3.39	0.0265
15	102.843573	24.642787	1880.7707	-33.1133	-0.8319	0.81	-0.0287
16	103.137778	24.658224	1838.4387	-32.7463	-0.7730	0.53	0.0302
17	102.426305	24.743284	1929.0475	-33.4575	-0.7771	1.48	0.0261
20	102.729945	24.734909	1856.2213	-33.2087	-0.8356	6.12	-0.0324
21	102.840819	24.752018	2117.8582	-32.8948	-0.7459	1.56	0.0573
22	102.939253	24.728089	2050.9590	-32.8500	-0.7907	0.81	0.0125
23	103.029713	24.748496	2034.1986	-32.8194	-0.8217	0.88	-0.0185
24	103.129600	24.753135	1575.0654	-32.8486	-0.8477	1.41	-0.0445
25	103.227846	24.747081	1668.7801	-32.6509	-0.8116	3.06	-0.0084
26	103.327056	24.734505	1829.6718	-32.3302	-0.7499	3.77	0.0533



Open the source ASCII text file Number of rows of the file header 1 Exact and edit data Organize and display results

Exact and edit data from the source text file

The record attributes of source file

```
2
102.546777
24.458002
1659.0410
-33.6150
-0.8046
0.94
-0.0014
```

Add attribute

Insert>>>

Delete---

Clear all

The record attributes of target file

```
2
102.546777
24.458002
1659.0410
-0.8046
0.94
```

Set the target file header/Editable
62636844.042 62636851.905 62636853.400 -7.8630 -9.3578 -1.4948

Set the target record table header/Editable
no lon lat height residual weight

Ok Cancel



Open text file Save as Save process Follow example

62636844.042	62636851.905	62636853.400	-7.8630	-9.3578	-1.4948		
no lon lat height residual weight							
2	102.546777	24.458002	1659.0410	-0.8046	0.94		
3	102.632412	24.458211	2120.2558	-0.7142	1.23		
4	102.725921	24.460578	2111.3872	-0.7612	1.68		
5	102.420803	24.566357	1990.6386	-0.7157	1.95		
6	102.528697	24.562786	1936.4260	-0.7491	2.93		
9	102.832641	24.575505	1977.4949	-0.8223	1.04		
10	102.345532	24.668953	1919.7825	-0.7782	3.53		
11	102.423972	24.652933	1959.3369	-0.7548	2.02		
12	102.529771	24.667079	2157.7877	-0.7317	1.46		
13	102.631063	24.657055	1906.3415	-0.8185	3.53		
14	102.742718	24.652871	1935.7882	-0.7767	3.39		
15	102.843573	24.642787	1880.7707	-0.8319	0.81		
16	103.137778	24.658224	1838.4387	-0.7730	0.53		
17	102.426305	24.743284	1929.0475	-0.7771	1.48		
20	102.729945	24.734909	1856.2213	-0.8356	6.12		
21	102.840819	24.752018	2117.8582	-0.7459	1.56		
22	102.939253	24.728089	2050.9590	-0.7907	0.81		
23	103.029713	24.748496	2034.1986	-0.8217	0.88		
24	103.129600	24.753135	1575.0654	-0.8477	1.41		
25	103.227846	24.747081	1668.7801	-0.8116	3.06		

Open the source ASCII text file Number of rows of the file header 1 Exact and edit data Organize and display results file Save data in the textbox as

Display of the input-output file

>> [Function] Convert the general ASCII data record file from different sources and non-standard formats into the discrete geodetic record file in PAGravf format.
 ** Please click the button [Open the source ASCII text file]...
 >> C:/PAGravf4.5_win64en/examples/EdPntrecordstandard/rntksich.txt.
 ** look at the source file information in the text box above, enter the number of rows of the file header firstly, click the button [Exact and edit data]...
 >> Set the format parameters about the target file header, record table header, and record attributes.
 ** Click the control button [Organize and display results file] to count the maximum number of each column characters of the target record attributes, the upper editable textbox will display target file header, record table header and all the records.
 ** It takes some time to organize the target record attributes. Please wait...
 >> Complete the statistics of the maximum number of characters of the target record attributes, and display the target file header, record table header and all the records in the editable textbox.
 ** Check the target records file displayed in the editable textbox. Click the control button [Save data in the textbox as] to save the contents in the textbox as the target file...

Load format

process Follow example

```
62636853.400 -7.8630 -9.3578 -1.4948
1659.0410 -33.6150 -0.8046 0.94 -0.0014
2120.2558 -33.3212 -0.7142 1.23 0.0890
2111.3872 -33.2058 -0.7612 1.68 0.0420
1990.6386 -33.5334 -0.7157 1.95 0.0875
1936.4260 -33.3720 -0.7491 2.93 0.0541
1977.4949 -33.1581 -0.8223 1.04 -0.0191
1919.7825 -33.7565 -0.7782 3.53 0.0250
1959.3369 -33.4781 -0.7548 2.02 0.0484
2157.7877 -33.2933 -0.7317 1.46 0.0715
1906.3415 -33.3155 -0.8185 3.53 -0.0153
1935.7882 -33.1128 -0.7767 3.39 0.0265
1880.7707 -33.1133 -0.8319 0.81 -0.0287
1838.4387 -32.7463 -0.7730 0.53 0.0302
1929.0475 -33.4575 -0.7771 1.48 0.0261
1856.2213 -33.2087 -0.8356 6.12 -0.0324
2117.8582 -32.8948 -0.7459 1.56 0.0573
2050.9590 -32.8500 -0.7907 0.81 0.0125
2034.1986 -32.8194 -0.8217 0.88 -0.0185
1575.0654 -32.8486 -0.8477 1.41 -0.0445
1668.7801 -32.6509 -0.8116 3.06 -0.0084
1829.6718 -32.3302 -0.7499 3.77 0.0533
```

Number of rows of the file header 1 Exact and edit data Organize and display results file Save data in the textbox as

Save program process as

Convert the general ASCII data record file from different sources and non-standard formats into the discrete geodetic record file in PAGravf format.
 source ASCII text file...
 C:/EdPntrecordstandard/rntksich.txt.
 In the text box above, enter the number of rows of the file header firstly, click the button [Exact and edit data]...
 Set the target file header, record table header, and record attributes.
 Click the control button [Organize and display results file] to count the maximum number of each column characters of the target record attributes, the upper editable textbox will display target file header and all the records.
 It takes some time to organize the target record attributes. Please wait...
 Complete the statistics of the maximum number of characters of the target record attributes, and display the target file header, record table header and all the records in the editable textbox.
 Check the target records file displayed in the editable textbox. Click the control button [Save data in the textbox as] to save the contents in the textbox as the target file...

face for PAGravf to accept the external text data.



Changing of grid resolution by interpolation

Open file

Save as

Import parameters

Start computation

Save process

Follow example

Precise Approach of Earth Gravity Field and Geoid

PAGravf4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Changing of grid resolution by interpolation

Interpolating of geodetic site attribute from grid

Selecting of records based on an attribute condition

Separating of (vector) grid data to two different regions

Open a geodetic grid file

>> Program Process ** Operation Prompts

Save program process as

Process many files in a folder

Grid spatial resolution 5.000'

Interpolation mode

Weighted inverse distance

>> Select the function module from the four control buttons at the top of the interface...

>> [Function] Increase or decrease the grid spatial resolution according to the given grid resolution and specified interpolation method.

** The grid direct averaging method is that sums up all the effective source cell-grid element values within the target cell-grid element, and then divided the sum by the number of the effective source cell-grid elements. The grid equal-area averaging method is that sums up all the effective source cell-grid element values within the target cell-grid element, and then divided the sum by the total number of source cell-grid elements.

>> Open a geodetic grid file C:/PAGravf4.5_win64en/examples/Edatafsimpleprocess/dbmGM1800150sksi.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/Edatafsimpleprocess/dbmGM1800300sksi.dat.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-27 09:46:11

>> Complete the computation!

>> Computation end time: 2024-09-27 09:46:12

Save the results as

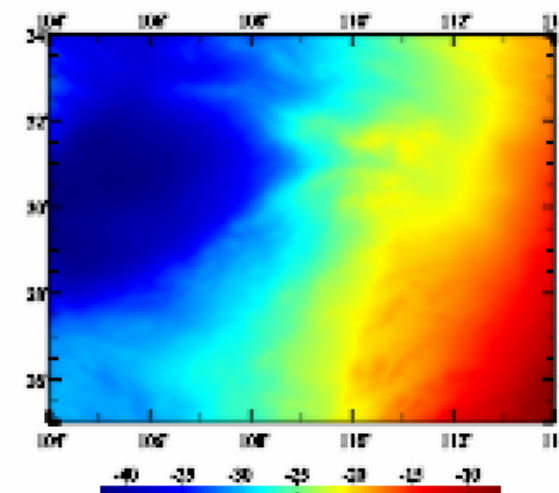
Import setting parameters

Start computation

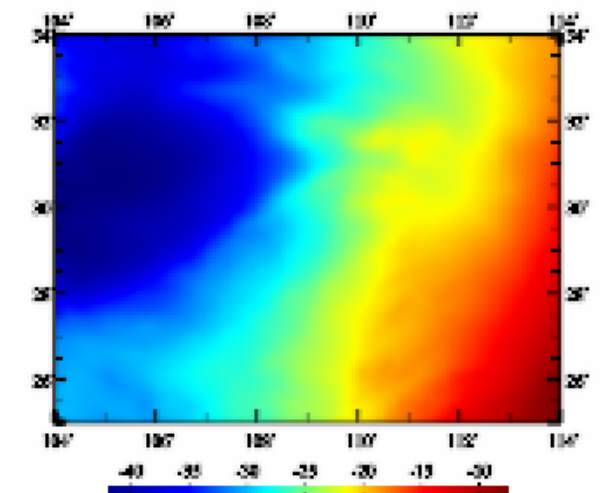
104.000000	114.000000	25.000000	34
-30.2919	-30.2668	-30.2778	-
-30.6576	-30.5428	-30.4278	-
-29.4737	-29.2776	-29.1069	-
-26.6049	-26.5548	-26.5321	-
-23.9284	-23.7268	-23.5718	-
-20.2001	-19.8410	-19.5237	-
-15.2558	-14.8489	-14.5217	-
-11.0481	-10.7002	-10.4082	-
-30.2686	-30.2461	-30.2499	-
-30.5727	-30.4886	-30.4152	-
-29.5261	-29.3636	-29.2124	-
-26.6002	-26.5250	-26.4927	-
-23.9027	-23.7075	-23.5598	-

Extract results

Plot↓



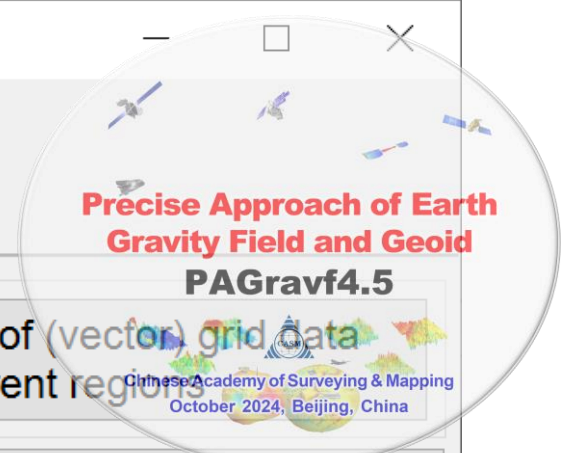
input grid



result grid

Interpolating of geodetic site attribute from grid

Open file Save as Import parameters Start computation Save process Follow example



Changing of grid resolution by interpolation | **Interpolating of geodetic site attribute from grid** | Selecting of records based on an attribute condition | Separating of (vector) grid data to two different regions

Open a discrete points file

Set format parameters of the file
Number of rows of the file header: 1

Open the grid file for interpolation

Interpolation mode
Weighted inverse distance

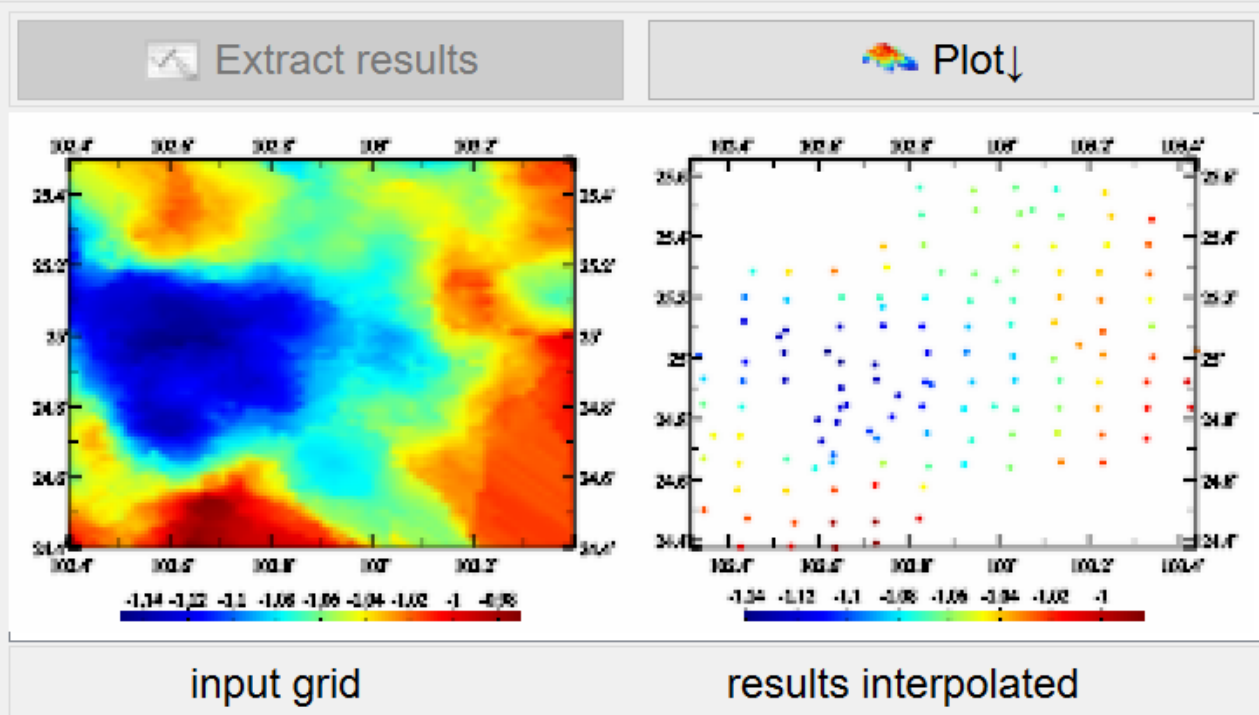
>> Program Process ** Operation Prompts

```
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-27 09:46:11
>> Complete the computation!
>> Computation end time: 2024-09-27 09:46:12
>> [Function] From a numerical grid, interpolate the attribute values of the geodetic sites using the specified interpolation method.
>> Open a discrete points file C:/PAGravf4.5_win64en/examples/Edatafsimpleprocess/pntdata.txt.
** Look at the input file information in the text box above, set the file format parameters...
>> Open the grid file for interpolationC:/PAGravf4.5_win64en/examples/Edatafsimpleprocess/pntgrid.dat.
>> Save the results as C:/PAGravf4.5_win64en/examples/Edatafsimpleprocess/rstpnt.txt.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2024-09-27 09:56:47
>> Complete the computation!
>> Computation end time: 2024-09-27 09:56:47
```

Save program process as

Save the results as | Import setting parameters | Start computation

number	lon(deg/decimal)	lat	ellipHeight(m)
1	102.442457	24.471769	1972.7703
2	102.546777	24.458002	1659.0410
3	102.632412	24.458211	2120.2558
4	102.725921	24.460578	2111.3872
5	102.420803	24.566357	1990.6386
6	102.528697	24.562786	1936.4260
7	102.634437	24.565660	2192.9271
8	102.725888	24.581970	2303.7797
9	102.832641	24.575505	1977.4949
10	102.345532	24.668953	1919.7825
11	102.423972	24.652933	1959.3369
12	102.529771	24.667079	2157.7877
13	102.631063	24.657055	1906.3415

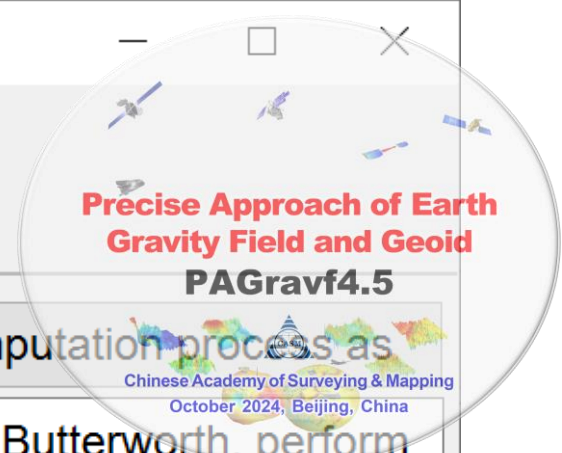


Low-pass filtering operation on geodetic grid file

Open grid file Import parameters Save as Start Computation

Save process

Follow example



Open the geodetic grid file

Select low-pass filter

moving average filter

Set filter parameter n 2

Save the results as

Import setting parameters

Start Computation

>> Computation Process ** Operation Prompts

>> [Function] Using the low-pass filters such as the moving average, Gaussian, exponential or Butterworth, perform low-pass filtering on the geodetic grid file. Before and after filtering, the grid specification (Latitude and longitude range and spatial resolution) remain unchanged.

** For the moving average filtering, the greater the filtering parameter n, the greater the filtering strength. For 'Exponential' or 'Butterworth' filters, the smaller the n, the greater the filtering strength.

>> Open the geodetic grid file C:/PAGravf4.5_win64en/examples/EdGrdlowpassfilter/dbmGM1800150sgr.dat.

>> Save the results as C:/PAGravf4.5_win64en/examples/EdGrdlowpassfilter/result.dat.

** The program output the low-pass filtered file with the same grid specification as the input file.

>> The parameter settings have been entered into the system!

** Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2024-09-27 10:32:30

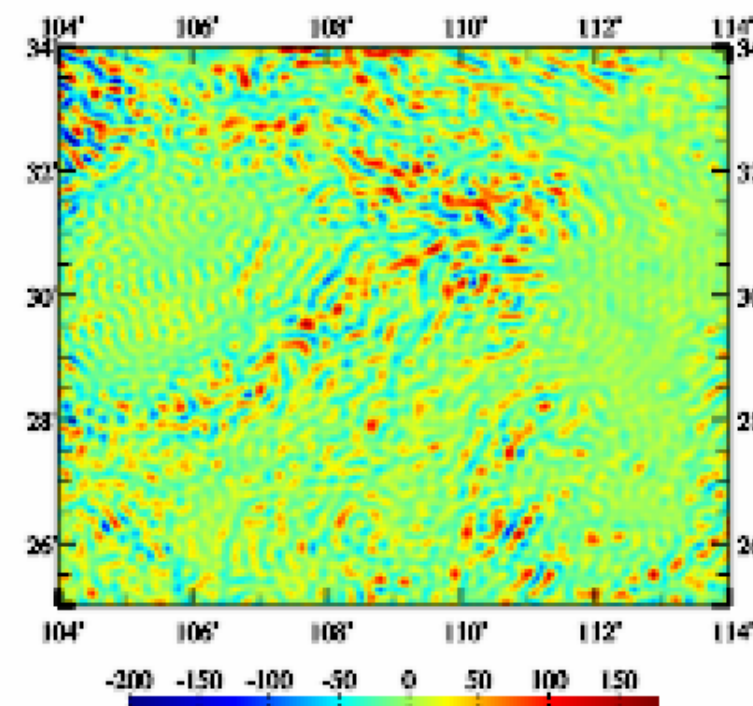
>> Complete the Low-pass filtering operation!

>> Computation end time: 2024-09-27 10:32:30

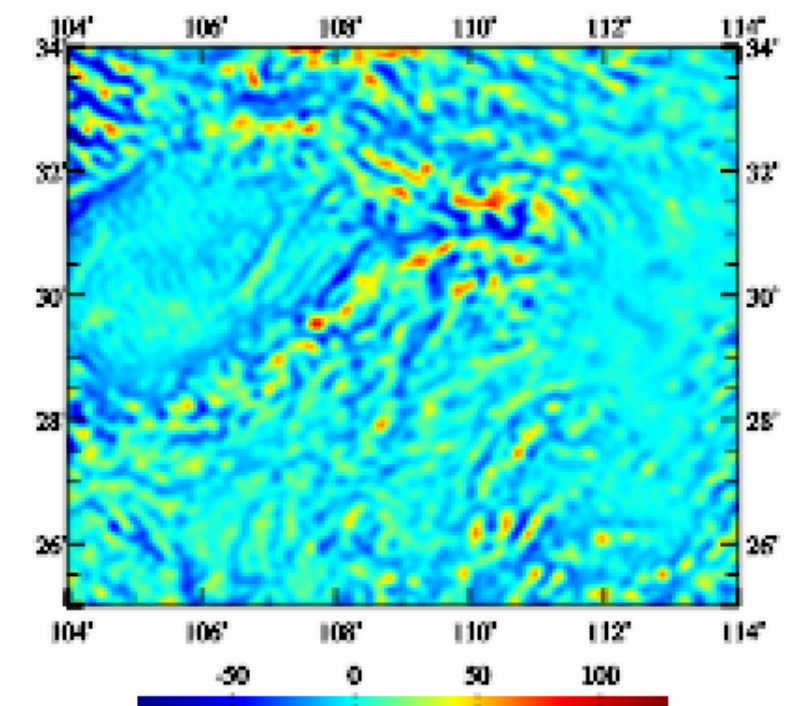
104.000000	114.000000	25.000000	34.000000	0.041667
-5.962	4.177	11.466	23.289	28.210
-10.021	-2.122	7.745	14.268	12.628
-6.945	-2.312	6.767	18.694	31.652
-36.281	-36.125	-29.339	-19.418	-11.661
-32.602	-28.244	-23.450	-17.043	-7.400
2.814	7.501	6.571	1.403	-4.846
11.234	8.115	3.029	-3.837	-11.794
2.271	-6.546	-13.002	-10.816	0.961
-18.356	-9.850	-3.663	-4.016	-9.983
13.916	11.283	9.246	10.708	15.153
-20.631	-18.825	-17.034	-15.637	-13.492
-24.640	-23.201	-25.161	-31.713	-38.808
-6.841	-6.836	-4.822	-2.367	-1.876
-3.447	-14.404	-21.274	-23.791	-21.795
-37.146	-36.745	-32.950	-24.857	-14.622
-35.635	-30.386	-17.813	-6.002	-0.671
-8.413	0.194	6.596	17.027	21.671

Extract filter result

Plot



input grid



low-pass filter grid

Low-pass filtering operation on geodetic grid file

Open grid file

Import parameters

Save as

Start Computation

Save process

Follow example

Precise Approach of Earth Gravity Field and Geoid
PAGravf4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Open the geodetic grid file

Select low-pass filter

Gaussian filter

Set filter parameter n 2

Save the results as

Import setting parameters

Start Computation

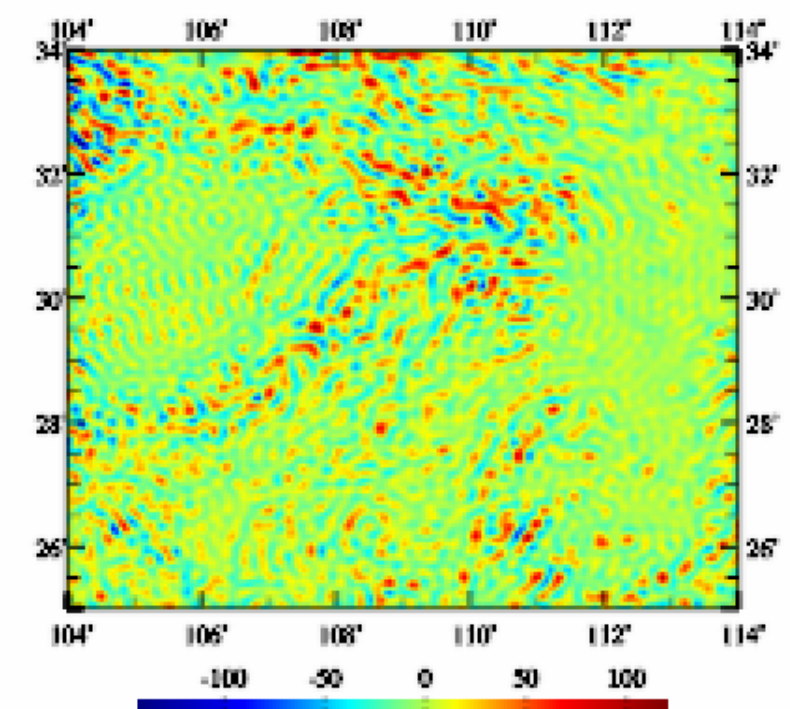
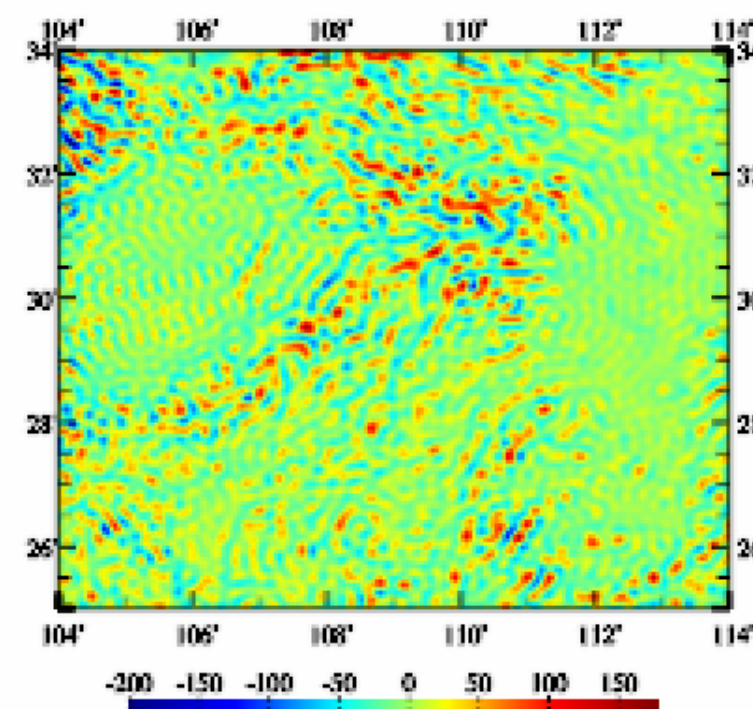
>> Computation Process ** Operation Prompts

'Exponential' or 'Butterworth' filters, the smaller the n, the greater the filtering strength.
 >> Open the geodetic grid file C:/PAGravf4.5_win64en/examples/EdGrdlowpassfilter/dbmGM1800150sgr.dat.
 >> Save the results as C:/PAGravf4.5_win64en/examples/EdGrdlowpassfilter/result.dat.
 ** The program output the low-pass filtered file with the same grid specification as the input file.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-27 10:32:30
 >> Complete the Low-pass filtering operation!
 >> Computation end time: 2024-09-27 10:32:30
 >> Save the results as C:/PAGravf4.5_win64en/examples/EdGrdlowpassfilter/result1.dat.
 ** The program output the low-pass filtered file with the same grid specification as the input file.
 >> The parameter settings have been entered into the system!
 ** Click the [Start Computation] control button, or the [Start Computation] tool button...
 >> Computation start time: 2024-09-27 10:33:26
 >> Complete the Low-pass filtering operation!
 >> Computation end time: 2024-09-27 10:33:27

104.000000	114.000000	25.000000	34.000000	0.041666
-19.431	-7.879	11.413	26.825	31.233
-19.523	-14.984	4.138	24.059	29.113
-18.862	-18.524	-15.997	-7.949	7.834
-29.674	-36.187	-30.500	-14.321	-0.916
-19.362	-8.006	-6.767	-8.914	-2.765
-6.860	-7.769	-6.066	-6.575	-9.922
17.310	5.179	-4.766	-8.772	-9.741
3.796	-11.765	-24.376	-16.442	8.155
-28.917	-10.133	2.926	-0.675	-15.467
3.900	-1.687	-1.105	8.596	22.421
-18.939	-15.864	-6.493	-1.751	-8.407
-10.302	15.787	17.485	0.926	-20.983
-10.792	-3.370	5.604	11.021	8.286
-14.854	-30.729	-39.021	-42.515	-40.857
-4.766	-17.662	-18.287	1.630	27.378
-29.743	-22.831	-7.968	2.368	4.241
-18.081	-5.241	14.003	27.689	31.614

Extract filter result

Plot



Gridding of discrete geodetic data by simple interpolation

Open file Save as Import parameter Start computation Save process Follow example

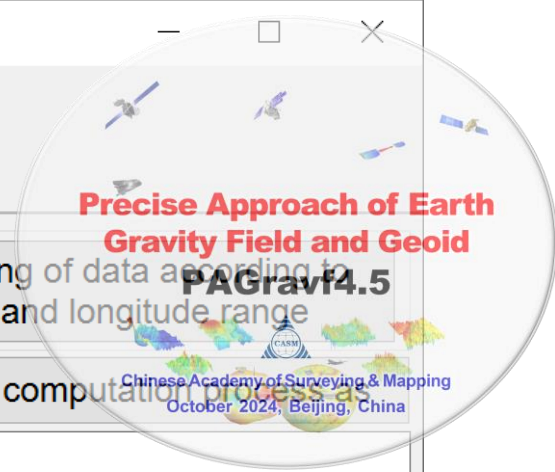
Gridding of discrete geodetic data by simple interpolation

Interpolation of vector grid from two attributes in geodetic records

Gridding of high-resolution record attributes by direct averaging

Constructing of general geodetic grid file

Extracting of data according to latitude and longitude range



Open a discrete point file

Process batch files with same specification Output spherical coordinate grid

Save computation process as

Number of rows of the file header: 1

Column ordinal number of the target attribute in the record: 4

Select interpolation mode: weighted inverse distance

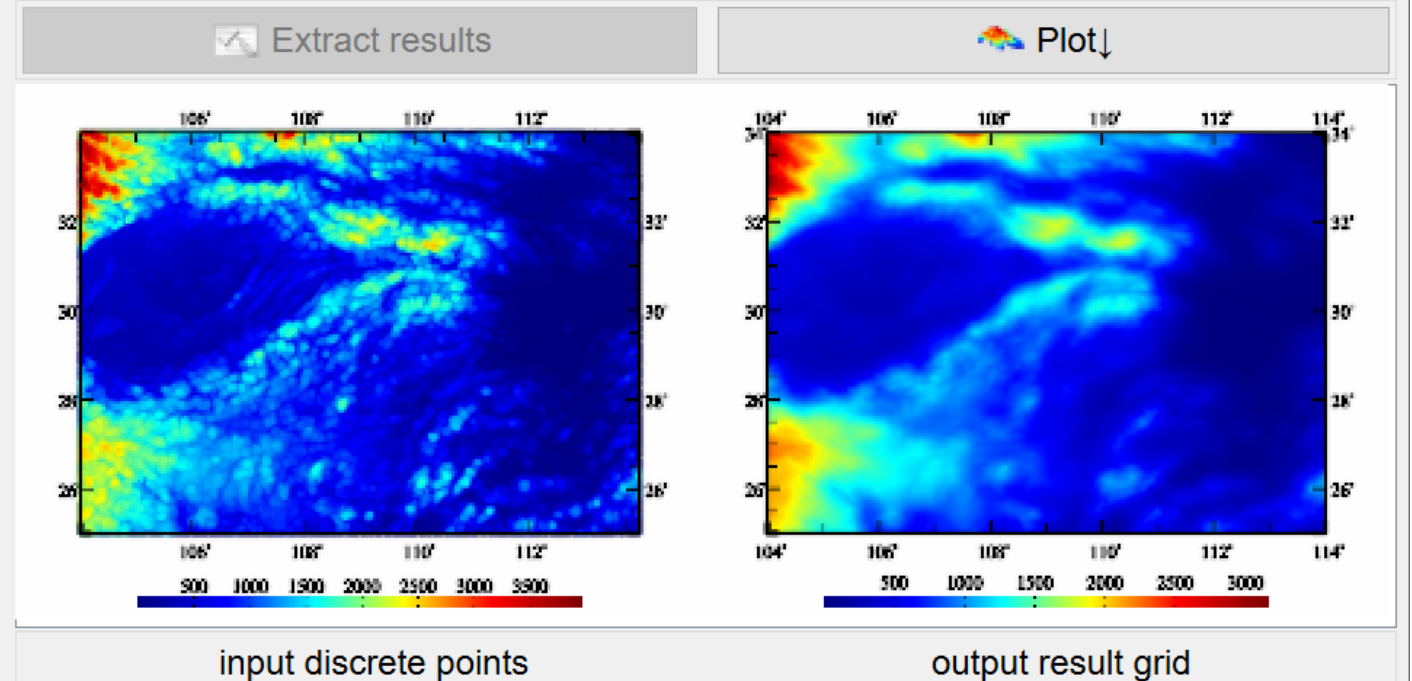
Interpolation search radius (multiple number of the cell grid): 5

```
>> Select the computation function from the 5 control buttons on the top of the interface...
>> [Function] From a geodetic discrete point file, generate the specified attribute grid file according to the specified interpolation method and grid specification. The program has the function of gridding batch discrete point files.
>> Open the discrete point file C:/PAGrav4.5_win64en/examples/Edareageodeticdata/dbmhgt150s.txt.
** Look at the input file information in the text box below, set the file format parameters.....
>> Save the results as C:/PAGrav4.5_win64en/examples/Edareageodeticdata/dbmhgt150s.dat.
>> Setting parameters have been imported in the program!
** Click the control button [Start computation], or the tool button [Start computation]....
>> Computation start time: 2024-09-27 10:57:36
>> Computation end time: 2024-09-27 10:57:44
>> Complete the computation!
```

Maximum latitude: 34.000°
 Minimum longitude: 104.000° Resolution: 3.000' Maximum longitude: 114.000°
 Minimum latitude: 25.000°

Save the results as
 Import setting parameters
 Start computation

104.000000	114.000000	25.000000	34.000000	0.05000000	0.05000000	
1912.5904	1911.5703	1894.6598	1892.0005	1860.2780	1805.2358	1735.2501
1501.5751	1452.5959	1369.1316	1302.7811	1258.5839	1290.7015	1299.0390
1297.9370	1248.0554	1157.4627	1079.7218	990.4826	892.5431	813.1832
719.6808	722.9691	692.5029	653.0434	636.2823	639.1619	628.3186
649.0571	677.0091	700.1582	669.0468	671.2319	678.5258	687.5093
756.8666	695.5997	646.0431	612.9434	560.7456	477.7001	467.2389
572.2131	657.7112	674.5429	654.7447	632.3204	602.1491	553.7679
217.7440	253.5656	303.8334	335.2665	341.6214	368.5970	401.2640
237.8323	221.9884	206.2026	185.5597	176.4804	177.4285	207.1053
535.1840	503.6774	470.6640	458.6786	503.5616	445.9992	389.0096
373.2007	427.3413	507.7882	559.9410	598.3770	622.1065	697.8113
540.5047	560.0292	548.2523	541.3006	536.5536	466.8930	430.2204
591.4949	575.7512	559.5084	549.6903	521.3611	501.4113	442.4179
246.4003	274.4692	304.5733	333.6479	361.8329		
1927.1494	1922.9193	1912.6866	1912.1639	1873.0282	1827.8662	1762.1738
1482.2412	1432.5739	1366.1587	1311.1388	1296.6929	1311.1117	1311.2577



Gridding of discrete geodetic data by simple interpolation

Open file Save as Import parameters Start Computation Save process Follow example

Precise Approach of Earth Gravity Field and Geoid

PAGravf4.5

Chinese Academy of Surveying & Mapping
October 2024, Beijing, China

Combining of two grid files into a vector grid file

Decomposing of vector grid file into two grid files

Transforming of vector form for vector grid file

Converting of vector grid into discrete point file

Save computation process

Open the grid file 1 with the same specification

Open the grid file 2 with the same specification

>> Computation Process ** Operation Prompts

- >> Select the function module from the four control buttons at the top of the interface...
- >> [Function] Combine two grids with the same specification as the two components of the vector into a vector grid.
- >> Open the grid file 1 with the same specification C:/PAGravf4.5_win64en/examples/EdVectorgridtransf/dbmchpcs.dat.
- >> Open the grid file 2 with the same specification C:/PAGravf4.5_win64en/examples/EdVectorgridtransf/dbmchpcw.dat.
- >> Save the results as C:/PAGravf4.5_win64en/examples/EdVectorgridtransf/dbmchcpc.dat.
- >> The parameter settings have been entered into the system!
- ** Click the [Start Computation] control button, or the [Start Computation] tool button...
- >> Computation start time: 2024-09-27 11:13:41
- >> Complete the computation!
- >> Computation end time: 2024-09-27 11:13:41

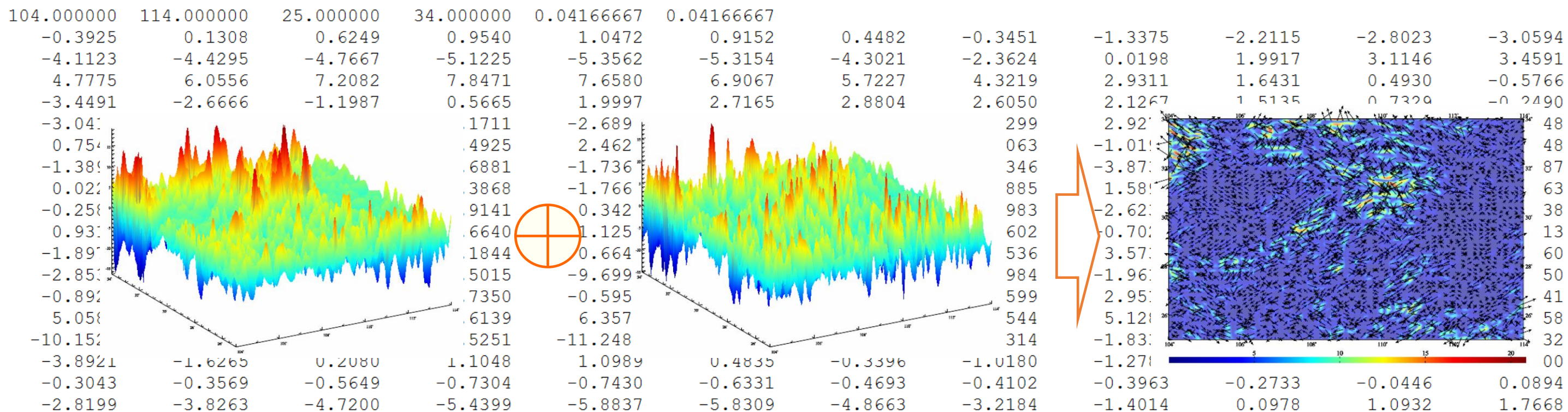
Save the vector grid as

Import setting parameters

Start Computation

Display of the input-output file ↓

Save data in the text box as



Statistical analysis on various geodetic data file

Select the file type to be statistic

The discrete point file

Open the discrete point file

Number of rows of the file header 0

Column ordinal number of the attribute to be statistic 5

Import setting parameters

Start statistic

Save statistic process as

** Please select the file type for statistics firstly!
 >> Statistics on the specified attributes...
 >> Open the discrete point file C:/PAGravf4.5_win64en/examples/Tlstatisticanalysis/GNSSIksirent.txt.
 ** Look at the input file information in the textbox above, set the file parameters.....
 >> Setting parameters have been imported into the program!
 ** Click the control button [Start statistic], or the tool button [Start statistic]...
 >> Computation start time: 2024-09-27 11:54:33

>> Statistic results:
 **Minimum longitude: 102.3455°
 Maximum longitude: 103.4253°
 Minimum latitude: 24.3751°
 Maximum latitude: 25.4877°
 **Mean: -0.1007
 Standard deviation: 0.0308
 Minimum: -0.1550
 Maximum: -0.0459

>> Complete the statistical calculation!
 >> Computation end time: 2024-09-27 11:54:33

Display of the input-output file↓

Save data in the textbox as

2	102.546777	24.458002	1659.0410	-0.1046
4	102.725921	24.460578	2111.3872	-0.0612
6	102.528697	24.562786	1936.4260	-0.0491
9	102.832641	24.575505	1977.4949	-0.1223
10	102.345532	24.668953	1919.7825	-0.0782
11	102.423972	24.652933	1959.3369	-0.0548
13	102.631063	24.657055	1906.3415	-0.1185
14	102.742718	24.652871	1935.7882	-0.0767
15	102.843573	24.642787	1880.7707	-0.1319
16	103.137778	24.658224	1838.4387	-0.0730
17	102.426305	24.743284	1929.0475	-0.0771
20	102.729945	24.734909	1856.2213	-0.1356
21	102.840819	24.752018	2117.8582	-0.0459
22	102.939253	24.728089	2050.9590	-0.0907
23	103.029713	24.748496	2034.1986	-0.1217
24	103.129600	24.753135	1575.0654	-0.1477
25	103.227846	24.747081	1668.7801	-0.1116
26	103.327056	24.734505	1829.6718	-0.0499
28	102.649137	24.836450	1915.0798	-0.0515
30	102.830331	24.840826	1892.0219	-0.1239
31	102.922274	24.832754	2217.9935	-0.0469
32	103.037233	24.830408	2035.5017	-0.0674

Open file Import parameters Start statistic Save process Follow example

Select the file type to be statistic

The geodetic grid file

Open the geodetic grid file

Import setting parameters

Start statistic

Maximum: -0.0459
 >> Complete the statistical calculation!
 >> Computation end time: 2024-09-27 11:54:33
 >> Statistics on the cell grid values...
 >> Open the geodetic grid file C:/PAGravf4.5_win64en/examples/Tlstatisticanalysis/dwmchrgr.dat.
 >> Setting parameters have been imported into the program!
 ** Click the control button [Start statistic], or the tool button [Start statistic]...
 >> Computation start time: 2024-09-27 11:55:56
 >> Statistic results:
 **Minimum longitude: 104.0000°
 Maximum longitude: 114.0000°
 Minimum latitude: 25.0000°
 Maximum latitude: 34.0000°
 **Mean: -0.0578
 Standard deviation: 22.9654
 Minimum: -167.3475
 Maximum: 175.2691
 >> Complete the statistical calculation!
 >> Computation end time: 2024-09-27 11:55:56

Display of the input-output file↓

Save data in the textbox as

104.000000	114.000000	25.000000	34.000000	0.04166667	0.04166667				
-25.7608	-13.3875	7.2186	24.7149	31.4088	25.8554	11.1546			
1.2492	8.2511	25.2000	40.5106	41.0960	24.1742	0.2044			
-29.8425	-27.6304	-21.0353	-8.0648	11.9223	35.0907	53.6553			

Open file Import parameters Start statistic Save process Follow example

Select the file type to be statistic

The vector grid file

Open the vector grid file

Import setting parameters

Start statistic

Maximum: 175.2691
 >> Complete the statistical calculation!
 >> Computation end time: 2024-09-27 11:55:56
 >> Statistics on the vector grid values...
 >> Open the vector grid file C:/PAGravf4.5_win64en/examples/Tlstatisticanalysis/vectorgrd.dat.
 >> Setting parameters have been imported into the program!
 ** Click the control button [Start statistic], or the tool button [Start statistic]...
 >> Computation start time: 2024-09-27 11:58:27
 >> Statistic results:
 **Minimum longitude: 104.0000°
 Maximum longitude: 114.0000°
 Minimum latitude: 25.0000°
 Maximum latitude: 34.0000°
 **Mean: -0.0043
 Standard deviation: 2.8762
 Minimum: -16.5760
 Maximum: 19.3528
 >> Complete the statistical calculation!
 >> Computation end time: 2024-09-27 11:58:27

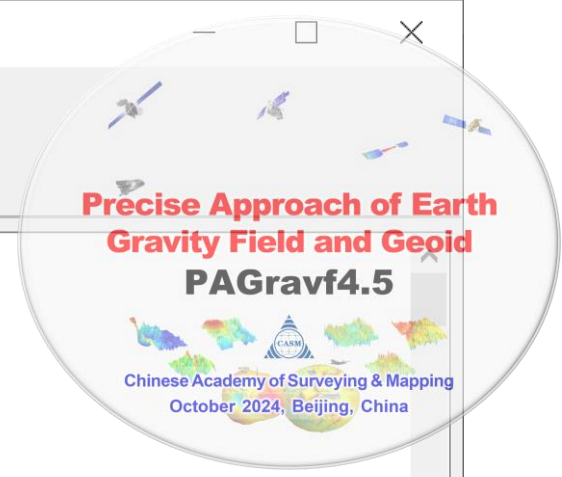
Display of the input-output file↓

Save data in the textbox as

104.000000	114.000000	25.000000	34.000000	0.04166667	0.04166667				
-0.3925	0.1308	0.6249	0.9540	1.0472	0.9152	0.4482	-0.3451	-1.3528	
-4.1123	-4.4295	-4.7667	-5.1225	-5.3562	-5.3154	-4.3021	-2.3624	0.0000	
4.7775	6.0556	7.2082	7.8471	7.6580	6.9067	5.7227	4.3219	2.9127	
-3.4491	-2.6666	-1.1987	0.5665	1.9997	2.7165	2.8804	2.6050	2.9127	
-3.0411	-3.2056	-3.2628	-3.1711	-2.6898	-1.6204	-0.0657	1.6299	2.9127	
0.7549	2.7751	3.6802	3.4925	2.4620	1.1620	0.0232	-0.7063	-1.0000	
-1.3899	-0.9508	-0.5012	-0.6881	-1.7360	-3.2512	-4.5168	-4.6346	-3.0000	
0.0223	-0.7894	-1.8763	-2.3868	-1.7663	-0.4668	0.8935	1.6885	1.0000	
-0.2582	0.3857	0.8903	0.9141	0.3425	-0.6010	-1.5352	-2.1983	-2.0000	
0.9317	0.8853	0.1592	-0.6640	-1.1252	-1.1305	-0.9017	-0.6602	-0.0000	
-1.8977	-1.1169	-0.6554	-0.1844	0.6645	1.9103	3.1100	3.6536	3.0000	
-2.8537	-6.2001	-8.2377	-9.5015	-9.6995	-8.9175	-7.2034	-4.6984	-1.0000	
-0.8920	-1.5237	-1.9587	-1.7350	-0.5952	1.0092	2.3268	2.8599	2.0000	
5.0580	5.3817	6.1200	6.6139	6.3571	5.5005	4.8020	4.7544	5.0000	
-10.1525	-9.9466	-9.9842	-10.5251	-11.2484	-11.3053	-9.1193	-5.5314	-1.0000	
-3.8921	-1.6265	0.2080	1.1048	1.0989	0.4835	-0.3396	-1.0180	-1.0000	
-0.3043	-0.3569	-0.5649	-0.7304	-0.7430	-0.6331	-0.4693	-0.4102	-0.0000	
-2.8199	-3.8263	-4.7200	-5.4399	-5.8837	-5.8309	-4.8663	-3.2184	-1.0000	
5.0169	5.7481	6.0781	5.8009	4.8926	3.6417	2.3429	1.3166	0.0000	
-1.2537	-0.4886	0.4475	1.3945	2.2480	2.9354	3.5076	3.8209	3.0000	

Visualization of multi-attribute curves from 2D geodetic data

Open file Import parameters Chart plot Save plot Follow example



Open 2D multi-attribute record file

Column ordinal number of x-axis (sort increment)

Location parameter of group 1 curve plotted

Location parameter of group 2 curve plotted

Location parameter of group 3 curve plotted

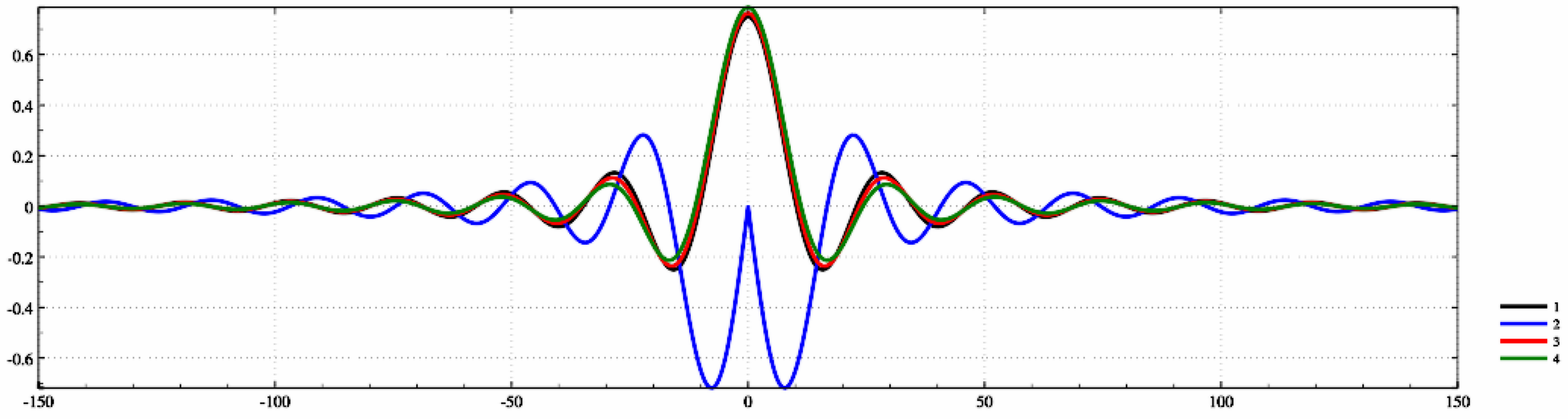
Row ordinal number of the starting-ending record

The program can plot less than 15 curves each time.

1	2	120	1800	3.00		
-150.000	-0.00691	-0.00541	-0.00850	-0.01087		
-149.814	-0.00657	-0.00513	-0.00810	-0.01150		
-149.629	-0.00621	-0.00483	-0.00768	-0.01209		
-149.443	-0.00583	-0.00453	-0.00723	-0.01265		
-149.257	-0.00544	-0.00420	-0.00677	-0.01318		
-149.072	-0.00503	-0.00387	-0.00628	-0.01368		
-148.886	-0.00460	-0.00352	-0.00577	-0.01413		
-148.700	-0.00416	-0.00316	-0.00525	-0.01456		
-148.515	-0.00371	-0.00280	-0.00471	-0.01494		
-148.329	-0.00324	-0.00242	-0.00416	-0.01528		
-148.144	-0.00276	-0.00204	-0.00359	-0.01559		
-147.958	-0.00228	-0.00164	-0.00301	-0.01585		
-147.772	-0.00178	-0.00125	-0.00242	-0.01607		
-147.587	-0.00128	-0.00084	-0.00182	-0.01624		
-147.401	-0.00078	-0.00044	-0.00122	-0.01638		
-147.215	-0.00027	-0.00003	-0.00060	-0.01646		
-147.030	0.00025	0.00038	0.00001	-0.01651		
-146.844	0.00076	0.00080	0.00063	-0.01650		
-146.658	0.00128	0.00121	0.00125	-0.01645		
-146.473	0.00179	0.00161	0.00187	-0.01636		
-146.287	0.00230	0.00202	0.00248	-0.01622		
-146.101	0.00280	0.00242	0.00309	-0.01604		

Label font size Line thickness

Import set parameters Chart plot Save current plot as



Hold down the left mouse button to rotate the plot, hold down the right button or scroll the middle mouse button to zoom the plot and hold down the middle button to pan the plot.
 If needing a larger scale plot, enlarge the graphics window on the right firstly, and then click the control button [Chart plot].

Visualization for specified attribute in discrete point record file

Open file Import parameters Scatter plot Save plot Follow example

Open the discrete geodetic point file

number of rows of file header: 1
 Column ordinal number of x: 2
 Column ordinal number of y: 3
 Column ordinal number of z: 5
 Minimum z: -9990.0
 Maximum z: 9990.0

Display style: Plane color scatter plot

Label font size: 6

Custom scale range (for batch plots)

Import parameters

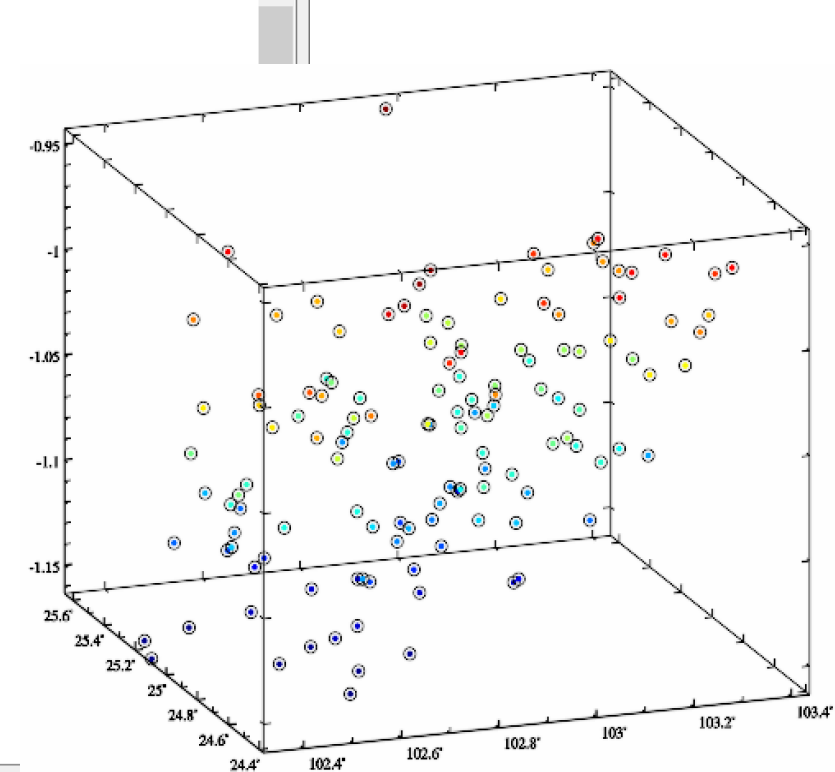
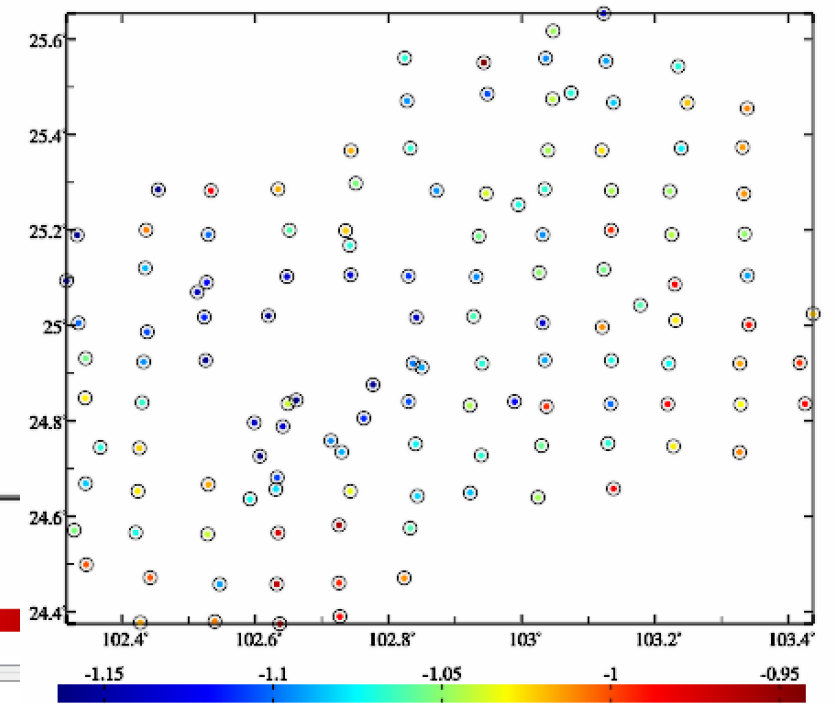
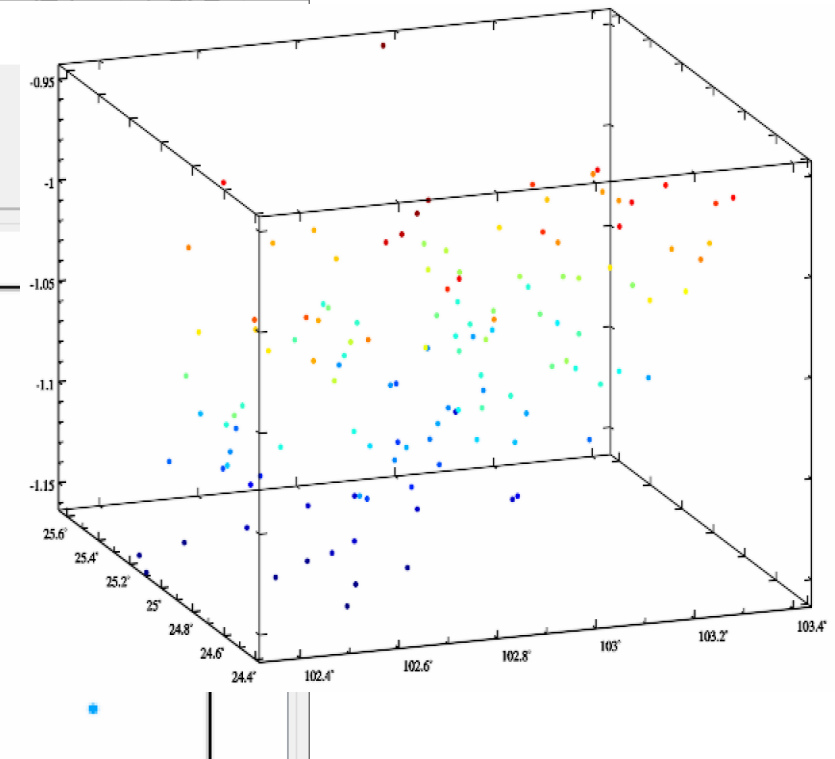
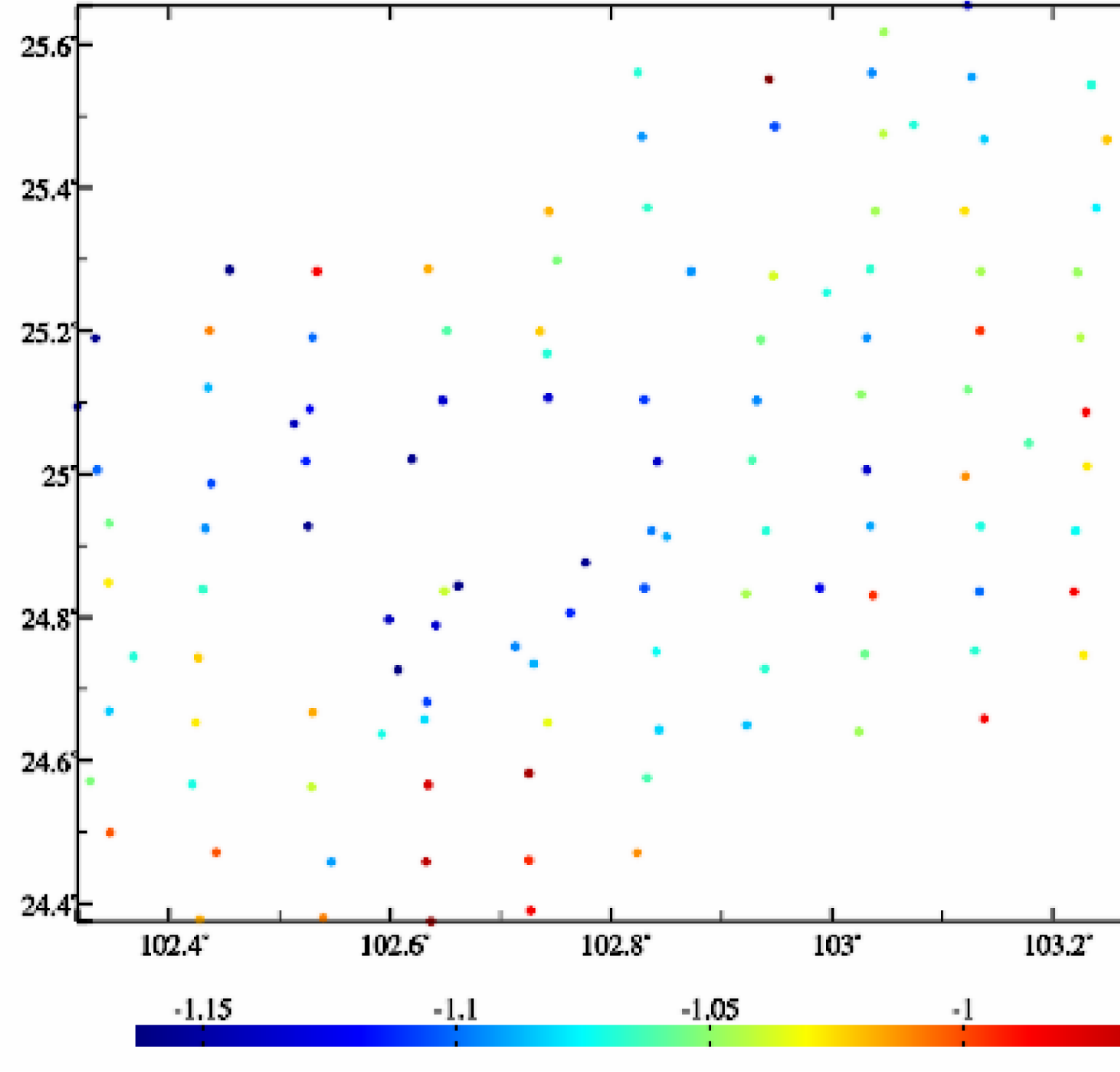
Scatter plot →

Hold down the left mouse button to rotate the plot, hold down the right button or scroll the middle mouse button to zoom the plot and hold down the middle button to pan the plot.

If needing a larger scale plot, enlarge the graphics window on the right firstly, and then click the control button [Chart plot].

After the input data file, z attribute or other parameters changed, you need to click the control button [Import setting parameters] again to update the plot.

Save current plot as



number	long(deg/decimal)	lat	ellipHeight (m)	rentKsi (m)	TerEffect (mGal)
1	102.442457	24.471769	1972.7703	-1.0013	-3.3508
2	102.546777	24.458002	1659.0410	-1.0916	-6.6124
3	102.632412	24.458211	2120.2558	-0.9639	-5.0422
4	102.725921	24.460578	2111.3872	-0.9936	-3.6867
5	102.420803	24.566357	1990.6386	-1.0706	-3.1489
6	102.528697	24.562786	1936.4260	-1.0402	-2.0473
7	102.634437	24.565660	2192.9271	-0.9743	-4.0534
8	102.725888	24.581970	2303.7797	-0.9566	-7.1388
9	102.832641	24.575505	1977.4949	-1.0619	-5.9858
10	102.345532	24.668953	1919.7825	-1.0840	-1.6645
11	102.423972	24.652933	1959.3369	-1.0281	-3.0476
12	102.529771	24.667079	2157.7877	-1.0165	-4.2396
13	102.631063	24.657055	1906.3415	-1.0806	-1.6637
14	102.742718	24.652871	1935.7882	-1.0343	-1.7419
15	102.843573	24.642787	1880.7707	-1.0819	-7.7294
16	103.137778	24.658224	1838.4387	-0.9843	-11.7862
17	102.426305	24.743284	1929.0475	-1.0229	-4.1779
20	102.729945	24.734909	1856.2213	-1.0884	-0.8096
21	102.840819	24.752018	2117.8582	-1.0735	-3.9704
22	102.939253	24.728089	2050.9590	-1.0675	-7.6863

Visualization for the geodetic grid file

Open grid Import parameters Draw plot Save plot Follow example

Open the geodetic grid file

Minimum -9000.0 Maximum 9000.0

Plot parameters

Label font size 6

Display style 2D color map

Custom scale range (for batch plots)

Import parameters

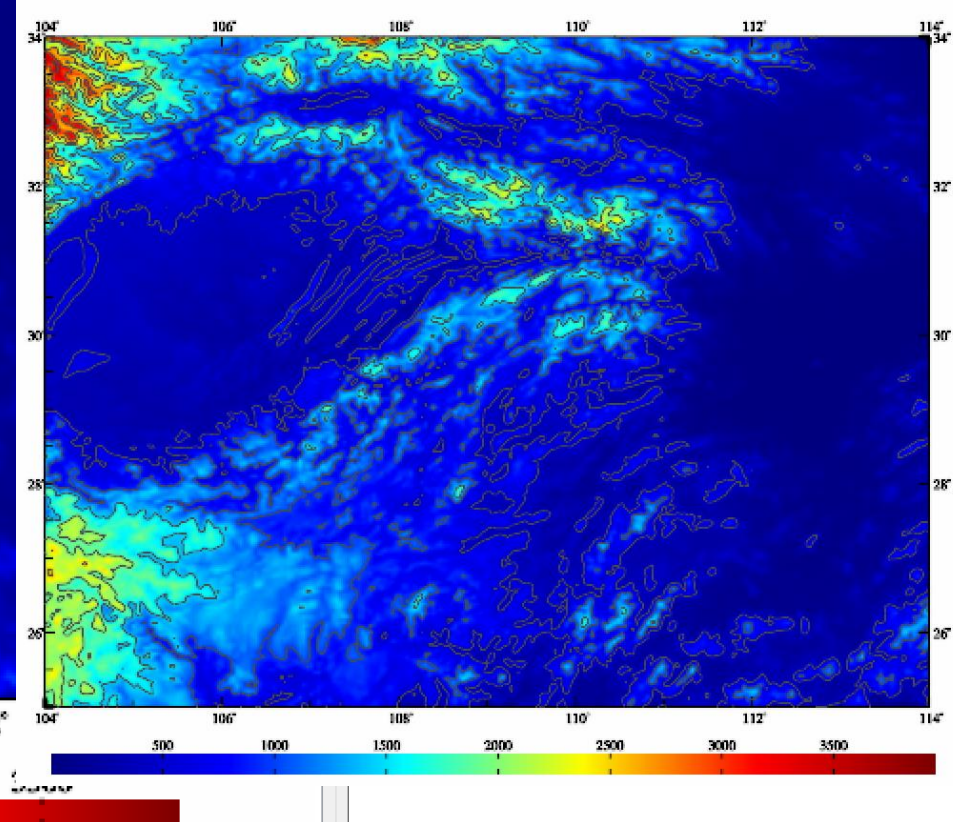
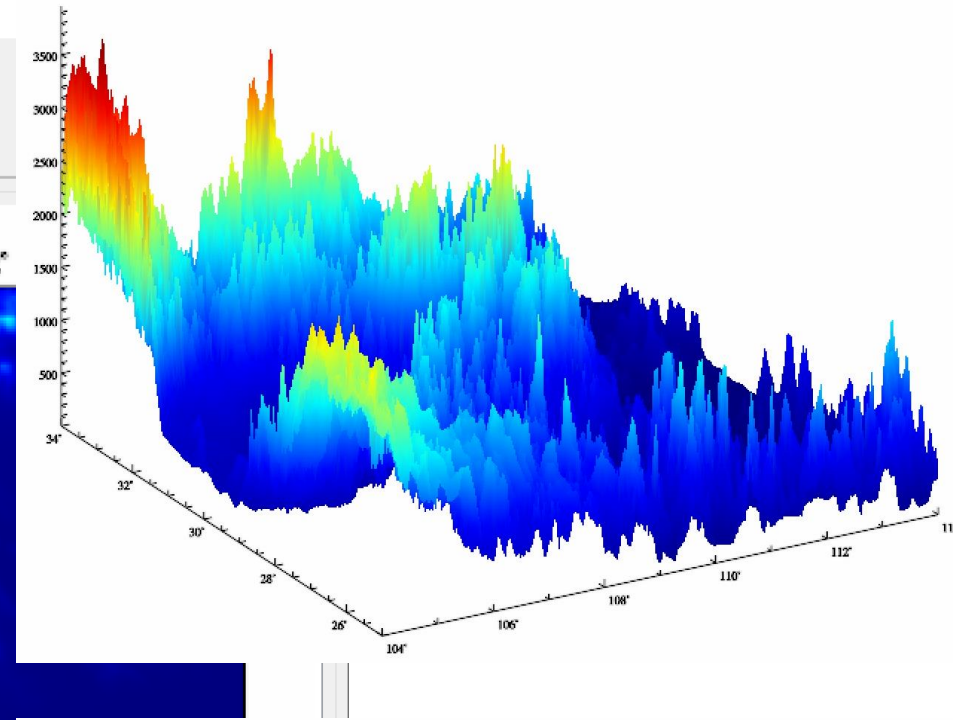
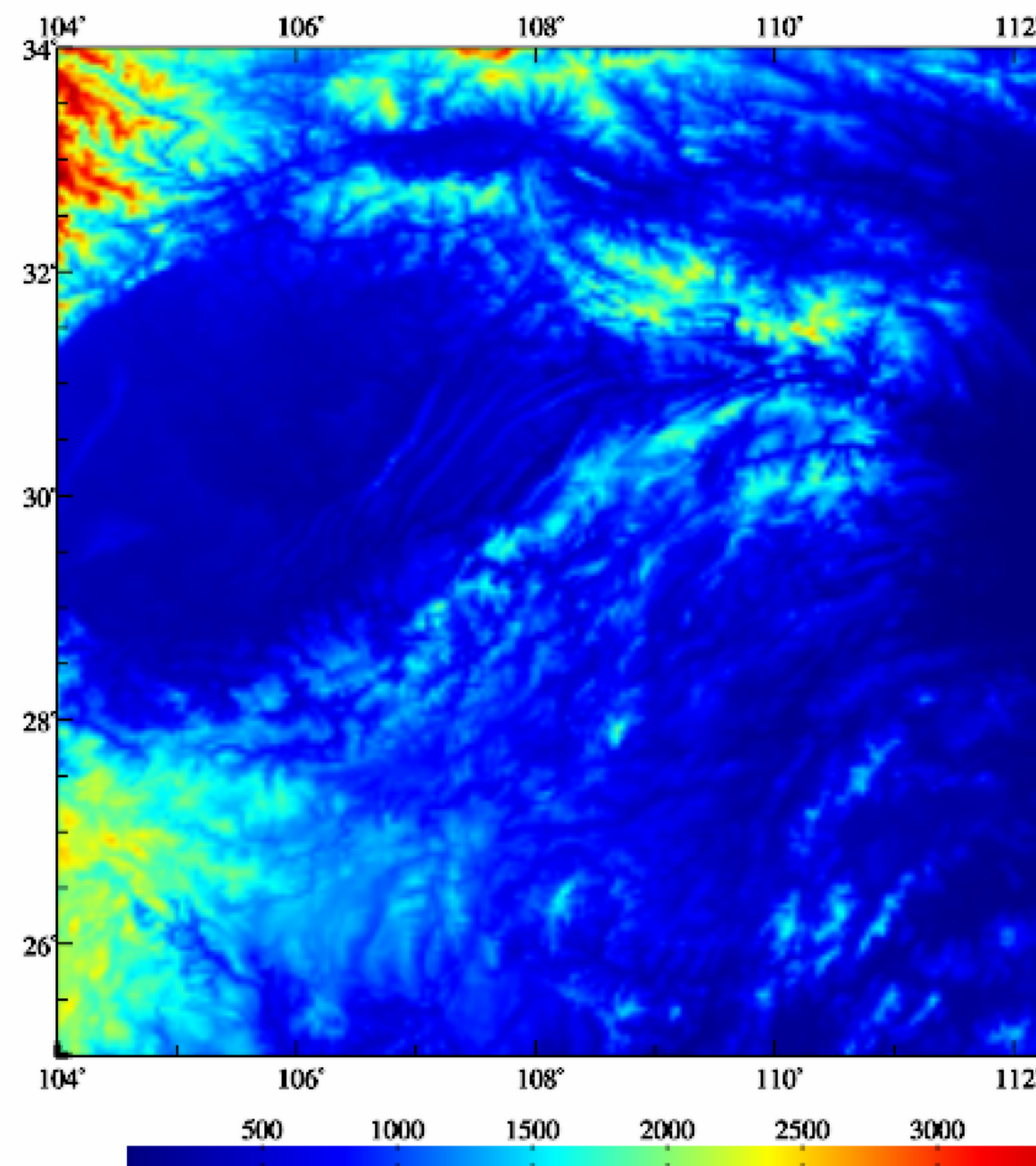
Draw plot →

Hold down the left mouse button to rotate the plot, hold down the right button or scroll the middle mouse button to zoom the plot and hold down the middle button to pan the plot.

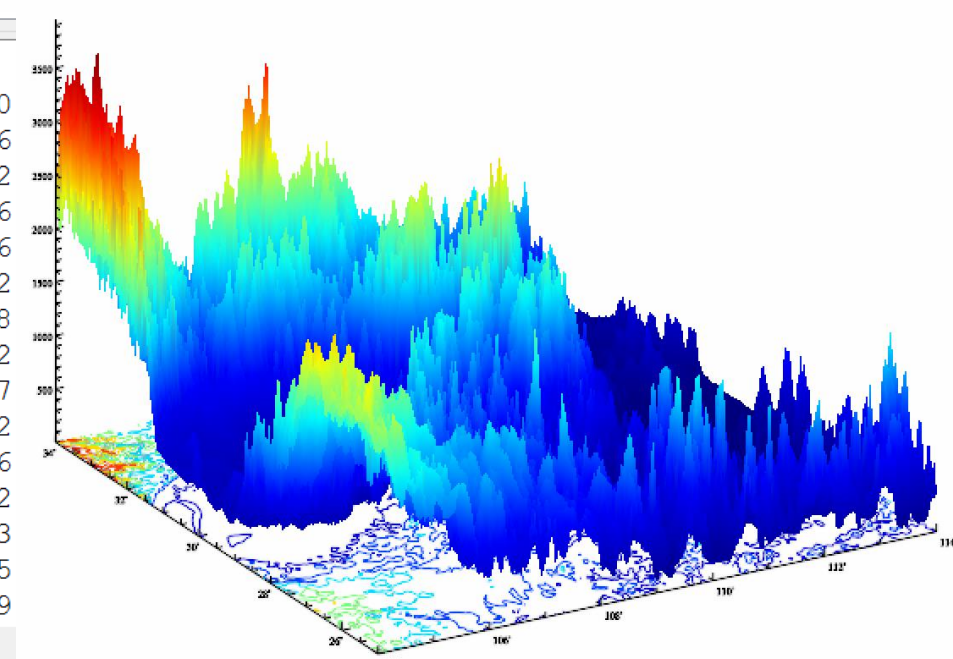
If needing a larger scale plot, enlarge the graphics window on the right firstly, and then click the control button [Draw plot].

After the input data file or other parameters changed, you need to click the control button [Import setting parameters] again to update the plot.

Save current plot as

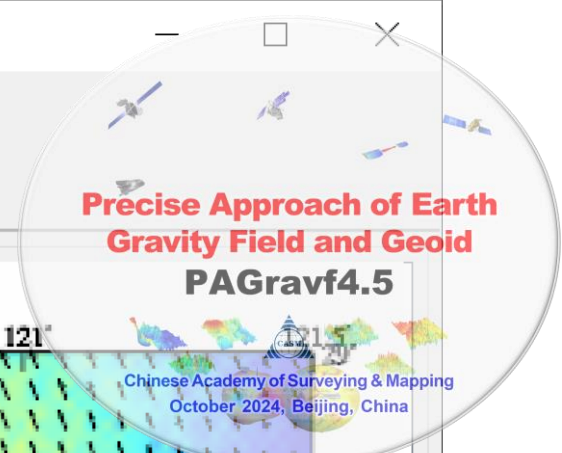


104.000000	114.000000	25.000000	34.000000	0.04166667	0.04166667						
1880.6229	1872.6631	1910.7226	1931.7678	1992.7628	1897.7201	1807.6282	1607.5273	1451.4399	1394.3910		
1579.5092	1478.5386	1457.5814	1610.5779	1703.5245	1392.4420	1257.3073	1156.1960	1088.1513	1250.1386		
1127.0908	1141.1294	1156.2046	1181.3156	1335.4458	1400.5863	1424.7030	1433.7637	1352.7645	1266.7092		
530.3341	562.3269	484.3763	478.4654	553.5572	717.6303	623.7012	541.7780	488.8902	636.0126		
642.5738	575.7033	629.8140	654.9278	694.0588	807.1893	877.3003	868.3630	752.3735	584.3726		
726.9660	439.0429	598.0917	604.1553	596.2404	510.3625	572.5056	692.6572	840.7887	791.9102		
820.3976	667.4142	588.4198	585.4228	661.4284	557.4446	337.4741	378.4927	359.5243	305.5678		
494.4589	433.5887	353.7412	430.9411	723.1664	821.3833	718.5536	599.6331	615.6516	595.6682		
128.9313	219.0568	175.1873	152.2870	137.3672	113.4730	108.6262	179.8153	317.0100	466.1877		
456.2484	331.3966	360.5464	451.7045	575.8571	698.9677	492.0606	313.0891	189.0889	170.1022		
151.7808	150.9295	208.1037	343.2835	296.4796	343.6928	326.9646	534.2658	1004.5335	951.7826		
220.4672	560.7057	752.8913	548.0598	375.1793	295.2814	273.3952	273.5185	318.6440	319.7772		
267.7158	300.9213	596.1217	576.3492	569.5540	559.7308	469.9046	541.0749	593.2796	657.5093		
466.1732	254.1907	224.2331	236.3034	250.4140	331.5690	326.7496	452.8991	547.0093	341.1055		
509.0990	504.2612	607.4467	873.6645	972.9187	777.1467	812.2700	762.3513	763.4239	620.5569		



Visualization for the geodetic vector grid file

Open vector Import parameters Draw plot Save plot Follow example



Open the vector grid file

Label font size

Vector parameters

x direction arrow number

vector arrow size

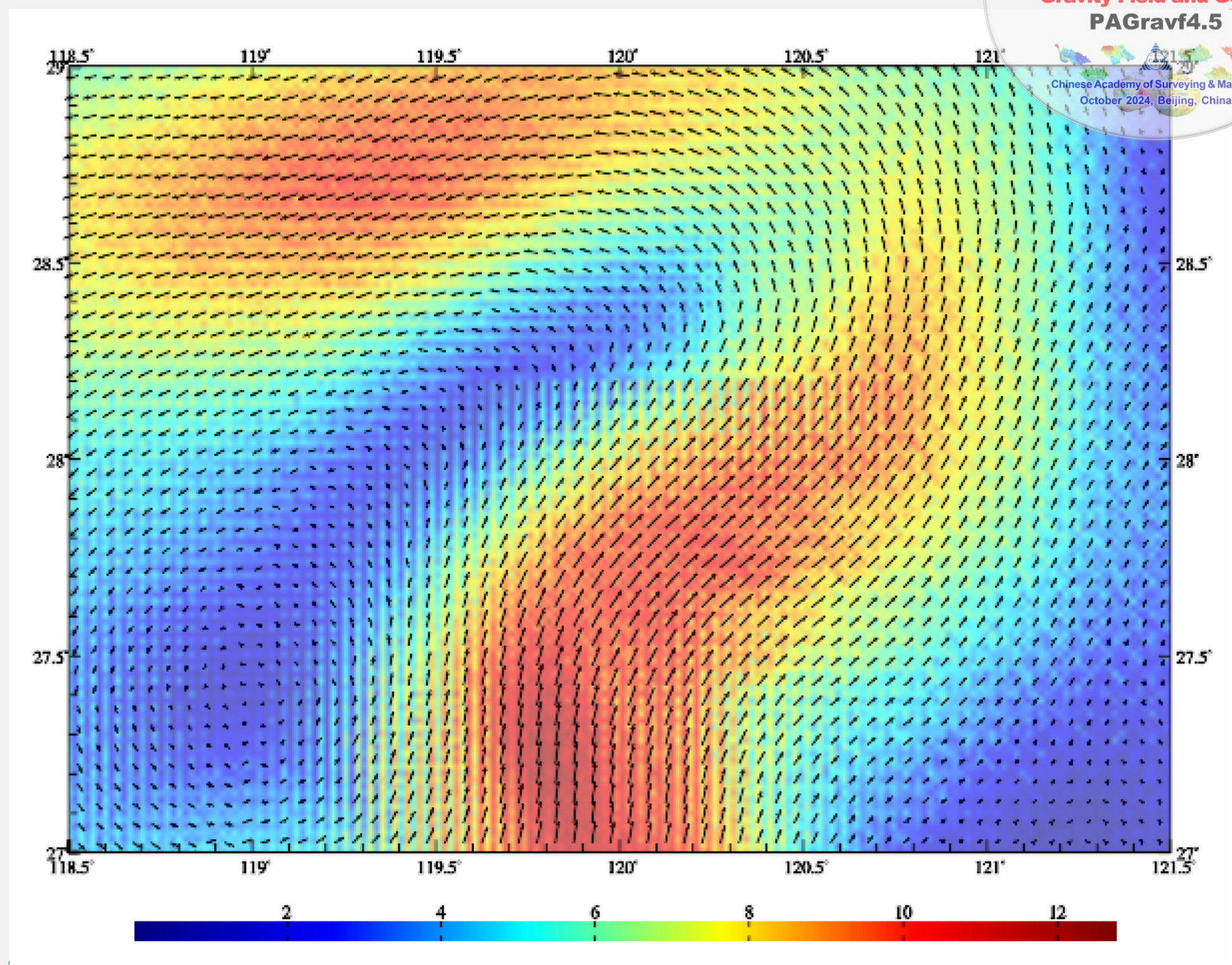
length of modulus of vector

Vector form

Import parameters Draw plot →

- Hold down the left mouse button to rotate the plot, hold down the right button or scroll the middle mouse button to zoom the plot and hold down the middle button to pan the plot.
- If needing a larger scale plot, enlarge the graphics window on the right firstly, and then click the control button [Draw plot].
- After the input data file or other parameters changed, you need to click the control button [Import setting parameters] again to update the plot.

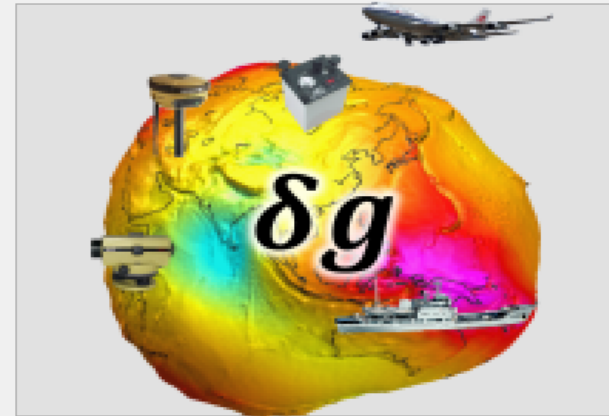
Save the current plot as



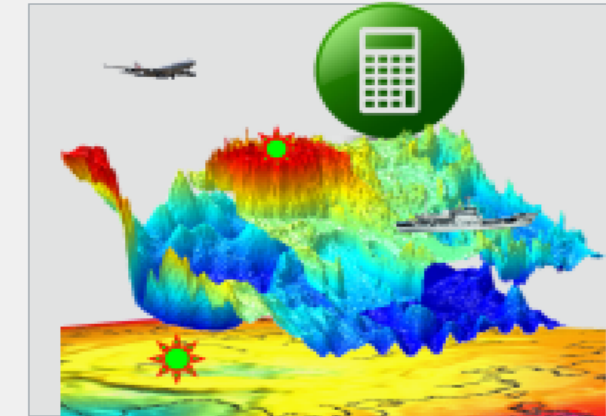
118.500000	121.500000	27.000000	29.000000	1.66666667E-02	1.66666667E-02	2015070106							
4.2017E+00	1.8364E+00	3.5829E+00	1.1078E+00	3.3135E+00	1.0280E+00	3.7127E+00	6.4872E-01	2.8045E+00	6.1878E-01	3.4332E+00	2.9941E-01		
-1.6967E-01	2.8743E+00	-6.7866E-01	2.2256E+00	-1.2675E+00	2.1258E+00	-6.9862E-01	1.8563E+00	-1.9861E+00	1.9162E+00	-1.4072E+00	1.7166E+00		
1.4771E+00	-2.1258E+00	9.9803E-01	-3.0041E+00	5.5890E-01	-3.0340E+00	1.0879E+00	-3.4732E+00	9.9803E-03	-3.5630E+00	5.4892E-01	-3.9622E+00		
-4.7606E+00	-5.7886E-01	-5.4493E+00	-1.5669E+00	-6.2776E+00	-1.9761E+00	-6.0181E+00	-2.7646E+00	-7.5351E+00	-3.2037E+00	-7.2457E+00	-3.9622E+00		
-5.2097E+00	-8.4234E+00	-5.8485E+00	-9.0821E+00	-6.5770E+00	-9.2518E+00	-6.2676E+00	-9.9404E+00	-7.7447E+00	-9.8606E+00	-7.3755E+00	-1.0170E+01		
-1.0978E+01	-9.4813E+00	-1.1208E+01	-1.0489E+01	-1.1907E+01	-1.0879E+01	-1.0928E+01	-1.1427E+01	-1.2006E+01	-1.1368E+01	-1.0589E+01	-1.1228E+01		
-1.1068E+01	-9.9304E+00	-1.1108E+01	-1.0090E+01	-1.1577E+01	-9.7009E+00	-1.0260E+01	-9.8007E+00	-1.1138E+01	-9.0122E+00	-1.0040E+01	-8.5132E+00		
-7.7148E+00	-9.2418E+00	-7.3056E+00	-9.1320E+00	-7.3056E+00	-8.2837E+00	-5.6888E+00	-8.2038E+00	-6.2676E+00	-7.2757E+00	-4.7906E+00	-6.3475E+00		



Summary, parameter settings and visualization for PAGravf4.5



Data analysis and preprocessing calculation of Earth gravity field



Computation of various terrain effects on various field elements outside geoid

☆ The basic principles, main methods and all the formulas in physical geodesy and Earth gravity field have been realized completely in PAGravf4.5 to improve high education environment.

☆ Many long-term puzzles such as various terrain effects on various observations, all-element analytical modelling on gravity field, fine gravity prospecting modelling from heterogeneous observations, external accuracy index measurement and computational performance control have been effectively solved to strengthen the application capacity of Earth gravity field.

www.zcyphygeodesy.com/en/

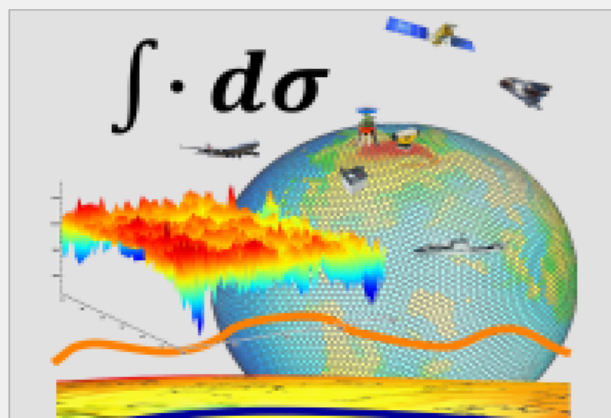


☆ PAGravf4.5 is suitable for senior under-graduates, graduate students, scientific researchers, and engineer technicians in geodesy and geophysics, geology and geoscience, geomatics and geographic information, seismic and geodynamics.

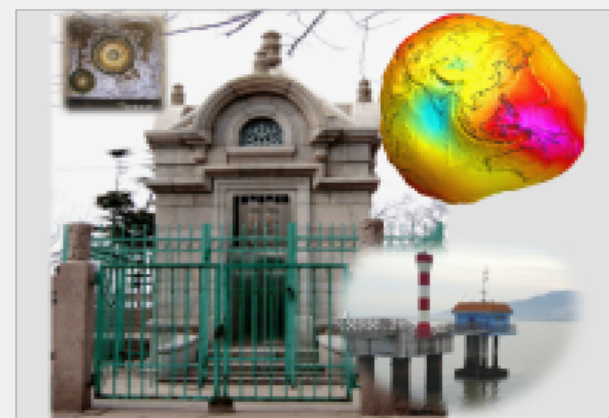
☆ There are the example files saved in the folder C:\PAGravf4.5_win64en\examples for each program, which includes the operation process file process.txt, some input-output data files and screenshots. It will take about 5 working days to complete all the example exercises. Thereafter, you can use PAGravf4.5 alone.

PAGravf4.5 scientific computation programs organization structure

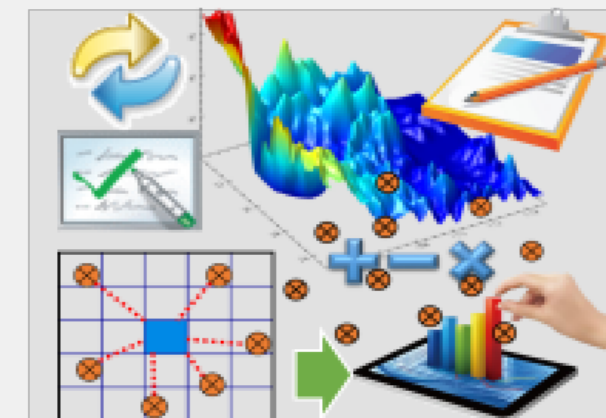
Geodetic data format and geodetic quantity convention in PAGravf4.5



Precise approach and all-element modeling on Earth gravity field



Optimization, unification, and application for regional height datum



Editing and calculation tools for geodetic data files

Classroom Teaching, Self-Exercise, Science Research and Engineer Computing

- Cross aliasing of heterogeneous observations in land-sea-space
- Loop closed analytical operations on outer gravity field elements
- Index measurement of observation errors and computation control

- Various terrain effects on all-element gravity field in whole space
- All-element modeling on Earth gravity field in whole outer space
- Gravity prospecting modelling from heterogeneous observations