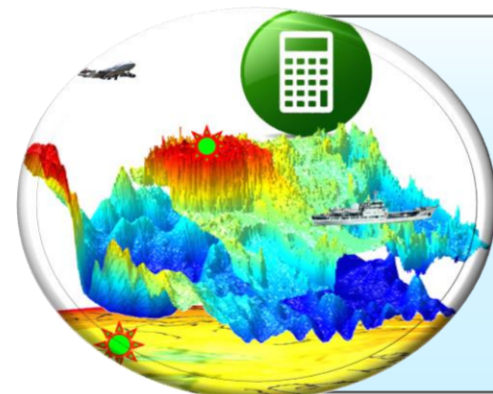




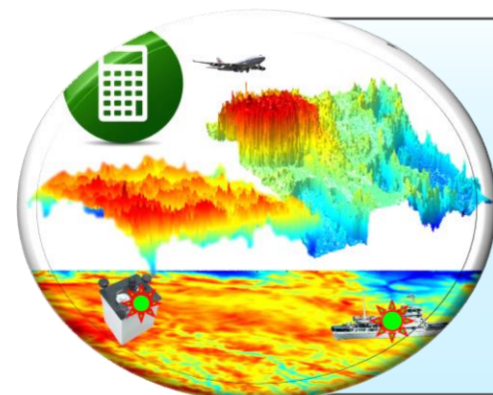
**Precise Approach of Earth  
Gravity Field and Geoid  
PAGravf4.5**

# Computation demo for terrain effect and gravity prospecting model

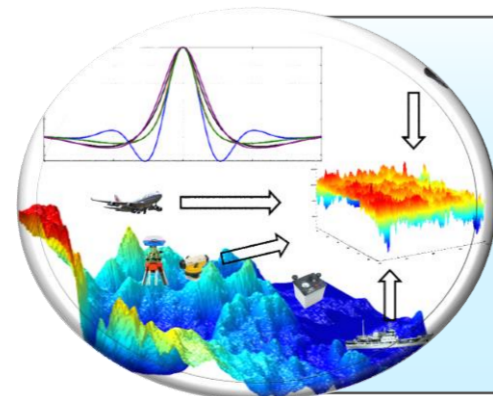
Chinese Academy of Surveying & Mapping  
Ma



**Computation demo of land-sea  
Bouguer / equilibrium anomaly  
from geopotential model**



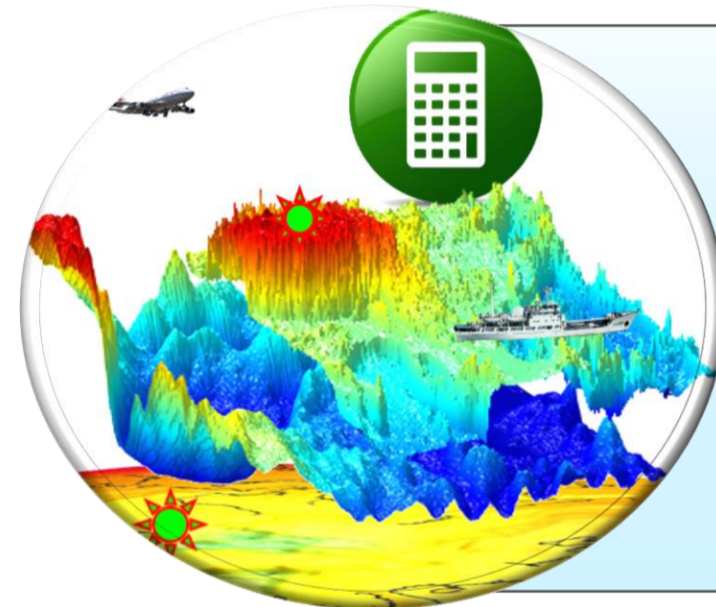
**Computation process demo of  
complete Bouguer anomaly on  
terrain equiheight surface**



**Scheme of gravity prospecting  
modeling by analytic fusion of  
heterogeneous observations**



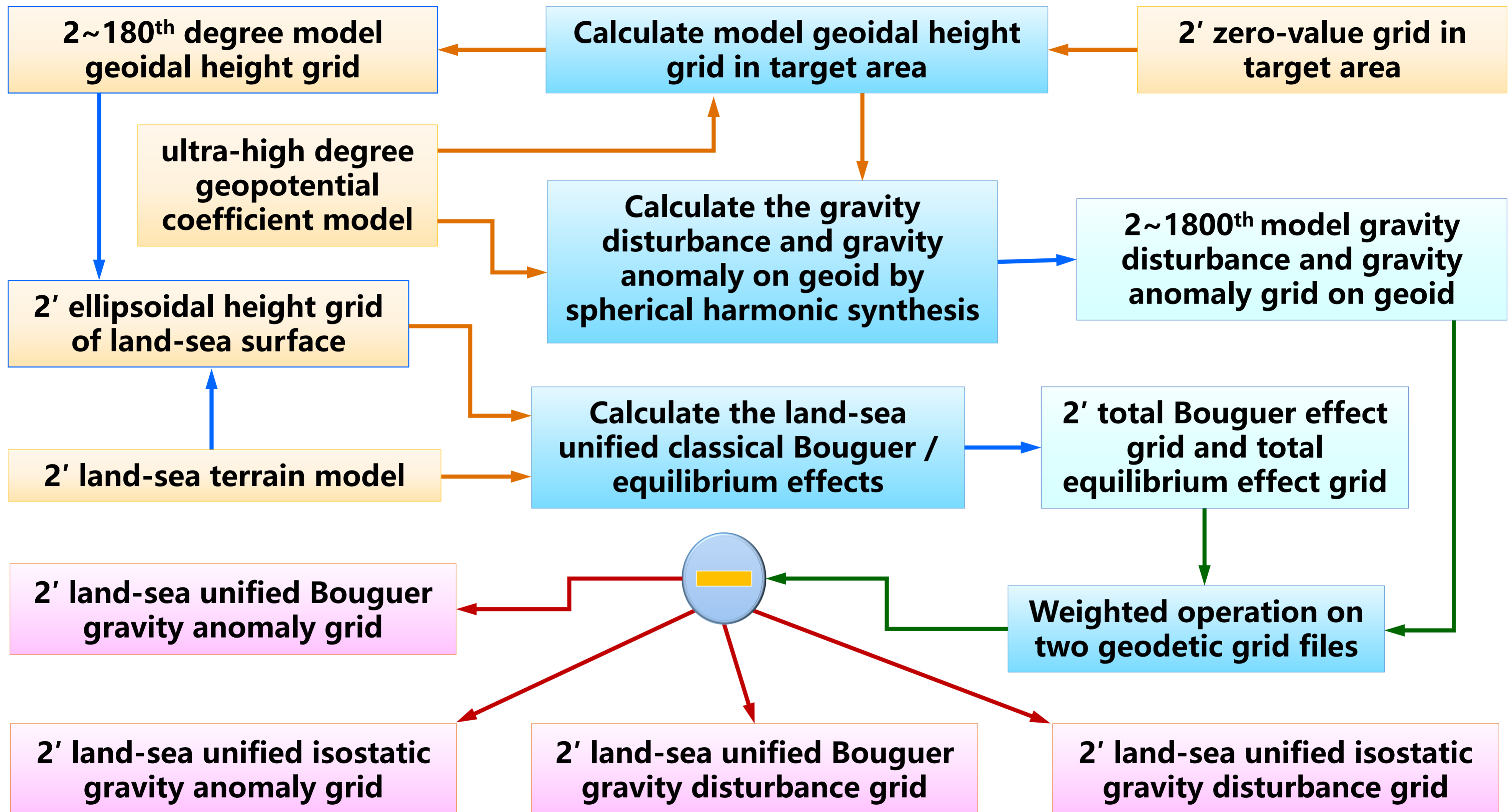
**Only four steps universal in global land-sea area. Everyone will !**



**Computation demo of land-sea Bouguer / equilibrium anomaly from geopotential model**

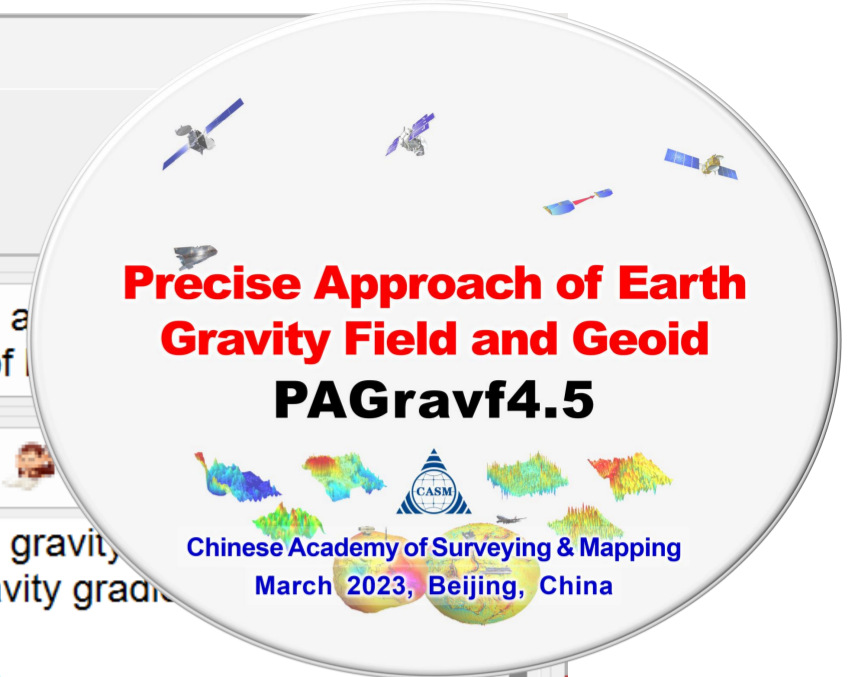
**The computation processes for Bouguer (isostatic) gravity anomaly (disturbance) are all exactly the same !**

[zcyphygeodesy.com/en/](http://zcyphygeodesy.com/en/)



Computation process demo of land-sea Bouguer/equilibrium anomaly from geopotential model

# (1) Calculate the 2~180th degree model geoidal height grid as the gravity reduction surface grid in target area.



Calculation of gravity field elements from global geopotential model

Calculation of model value for residual terrain (complete Bouguer) effects

Global geopotential coefficient model Calculator

Calculation a character of

Open global geopotential coefficient model file

Select calculation file format

Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select elements to be calculated

height anomaly (m)

gravity anomaly (mGal)

gravity disturbance (mGal)

vertical deflection (" , SW)

disturbing gravity gradient (E, radial)

tangential gravity gradient (E, NW)

Laplace operator (E)

Minimum degree 2

Maximum degree 180

Save computation process as

>> [Function] From global geopotential coefficient model, calculate the model value of the (residual) height anomaly (m), gravity anomaly (mGal), vertical deflection vector (" , south, west), disturbing gravity gradient (E, radial), tangential gravity gradient (E, NW), or Laplace operator (E).

\*\* Click the [Open global geopotential coefficient model file] control button or the [Open geopotential model] tool button...

>> Open global geopotential coefficient model file C:/PAGrav4.5\_win64en/data/EGM2008.gfc.

\*\* The window below only shows the geopotential coefficients data with no more than 2000 rows in it.

>> Open ellipsoidal height grid file of calculation surface C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougEquilibrium/zero2m.dat.

>> Save the results as C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougEquilibrium/GMgeoidh2m\_180.txt.

\*\* The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of anomalous field elements.

\*\* The program also outputs (residual) height anomaly (\*.ksi), gravity anomaly (\*.gra), gravity disturbance (\*.rga), vertical deflection vector (\*.dft), disturbing gravity gradient (\*.grr), tangential gravity gradient vector (\*.hgd) or Laplace operator (\*.lps) model value grid file into the current directory. Where \* is the output file name entered in the interface, and the program outputs the corresponding (residual) model value grid file according to the selected gravity field element type.

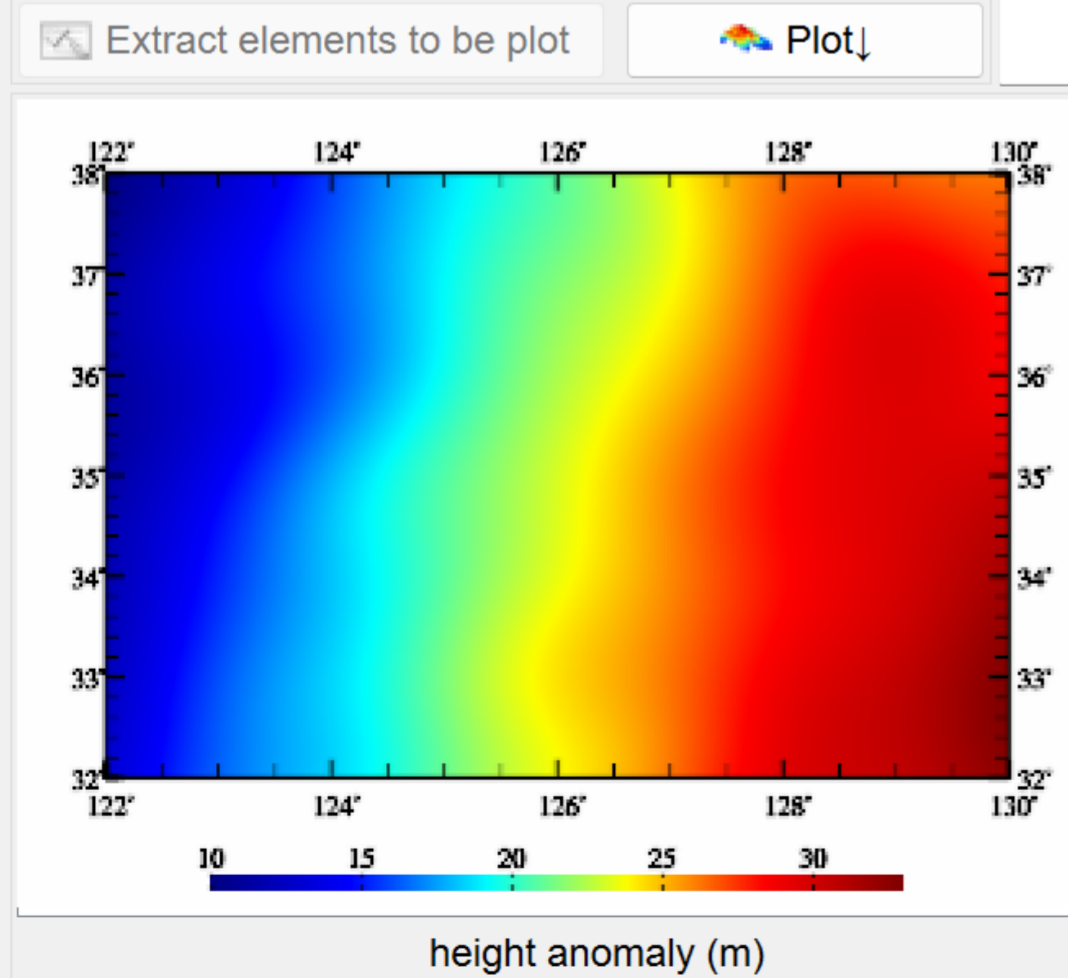
>> The parameter settings have been entered into the system!

Save the results as

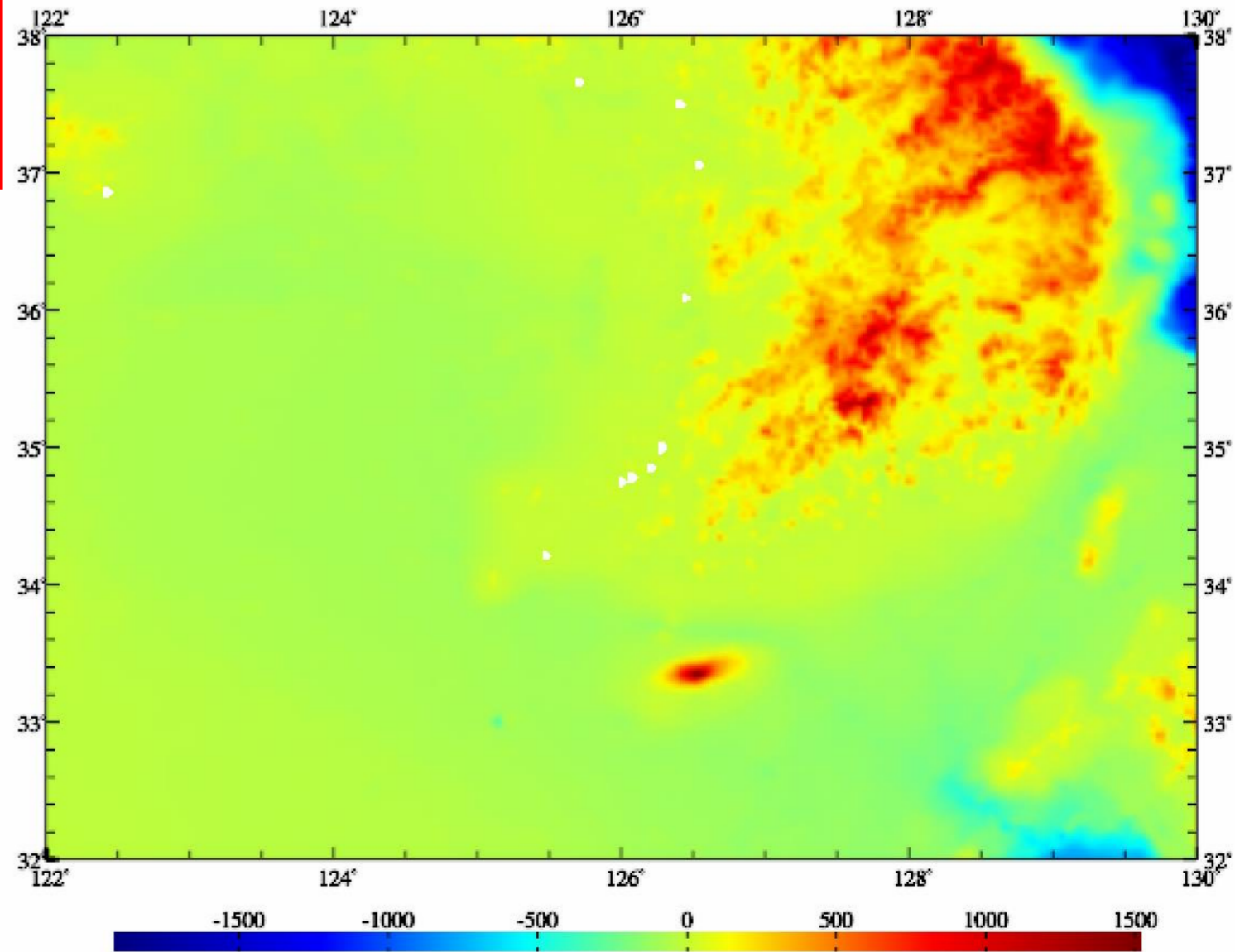
Import setting parameters

Start Computation

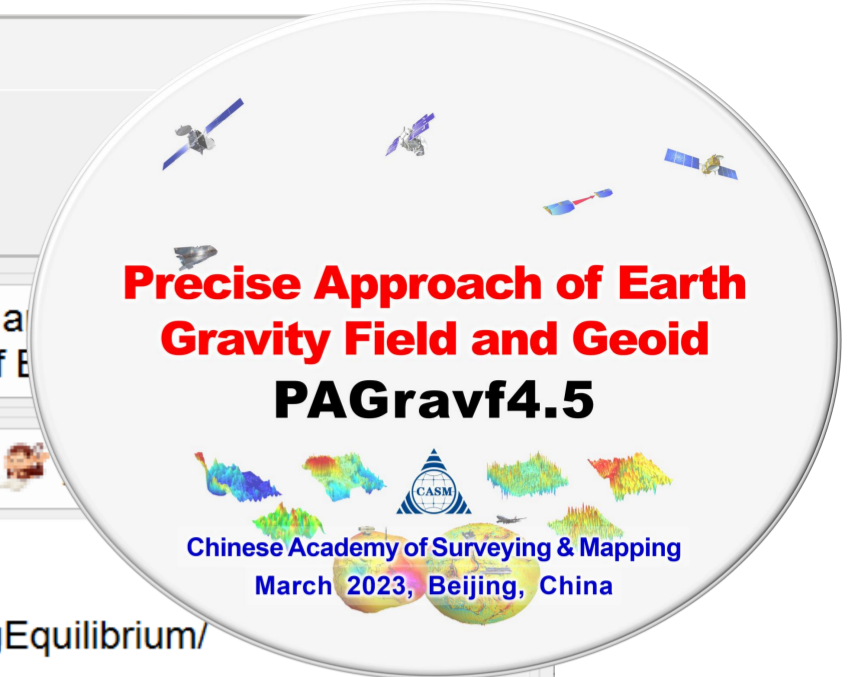
1	122.01667	32.01667	0.000	13.0311
2	122.05000	32.01667	0.000	13.1534
3	122.08333	32.01667	0.000	13.2760
4	122.11667	32.01667	0.000	13.3989
5	122.15000	32.01667	0.000	13.5220
6	122.18333	32.01667	0.000	13.6452
7	122.21667	32.01667	0.000	13.7683
8	122.25000	32.01667	0.000	13.8914
9	122.28333	32.01667	0.000	14.0142
10	122.31667	32.01667	0.000	14.1366



The 2~180th degree model geoidal height grid as the gravity reduction surface grid in target area



## (2) Calculate the gravity anomaly and gravity disturbance on geoid from the geopotential coefficient model.



Select calculation file format  
 Ellipsoidal height grid file

Select elements to be calculated

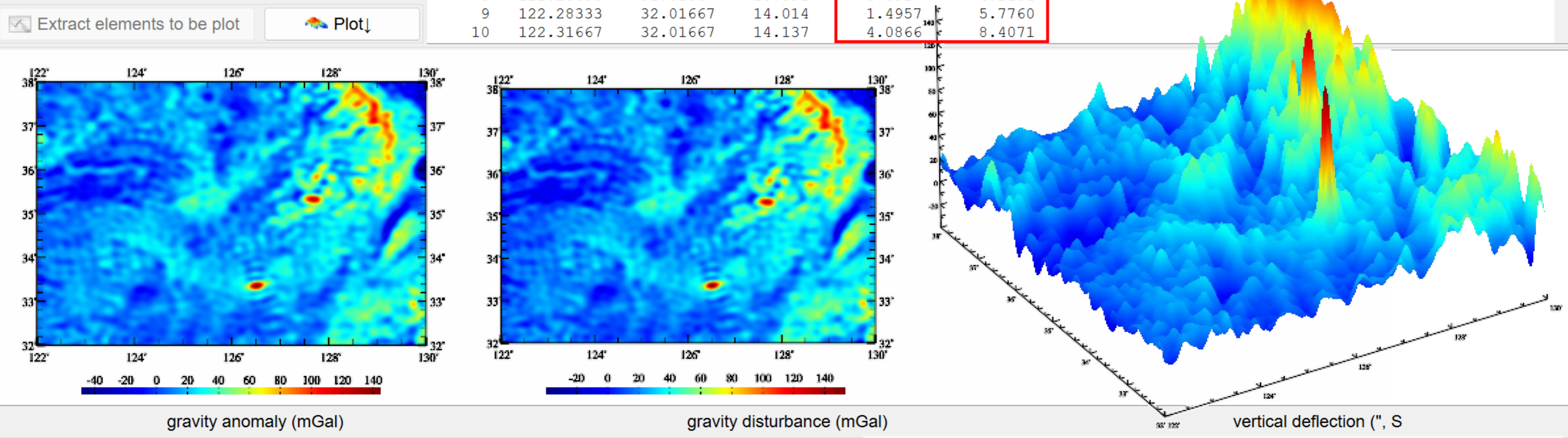
height anomaly (m)  
 gravity anomaly (mGal)  
 gravity disturbance (mGal)  
 vertical deflection (" , SW)  
 disturbing gravity gradient (E, radial)  
 tangential gravity gradient (E, NW)  
 Laplace operator (E)

Minimum degree 2  
 Maximum degree 1800

```

>> Open global geopotential coefficient model file C:/PAGrav4.5_win64en/data/EGM2008.gfc.
** The window below only shows the geopotential coefficients data with no more than 2000 rows in it.
>> Open ellipsoidal height grid file of calculation surface C:/PAGrav4.5_win64en/examples/Terraininflexercise/GMBougEquilibrium/GMgeoidh2m_180.ksi.
>> Save the results as C:/PAGrav4.5_win64en/examples/Terraininflexercise/GMBougEquilibrium/EGM2008_2m_1800.txt.
** The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of anomalous field elements.
** The program also outputs (residual) height anomaly (*.ksi), gravity anomaly (*.gra), gravity disturbance (*.rga), vertical deflection (*.dft), disturbing gravity gradient (*.grr), tangential gravity gradient vector (*.hgd) or Laplace operator (*.lps) model value grid file into the current directory. Where * is the output file name entered in the interface, and the program outputs the corresponding (residual) model value grid file according to the selected gravity field element type.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
** The calculation process need wait, during which you can open the output file to look at the calculation progress...
>> Computation start time: 2023-03-19 00:07:22
    
```

1	122.01667	32.01667	13.031	4.2037	8.2077
2	122.05000	32.01667	13.153	2.6153	6.6517
3	122.08333	32.01667	13.276	1.3041	5.3727
4	122.11667	32.01667	13.399	0.3653	4.4667
5	122.15000	32.01667	13.522	-0.2572	3.8777
6	122.18333	32.01667	13.645	-0.6185	3.5509
7	122.21667	32.01667	13.768	-0.6312	3.5738
8	122.25000	32.01667	13.891	-0.0317	4.2101
9	122.28333	32.01667	14.014	1.4957	5.7760
10	122.31667	32.01667	14.137	4.0866	8.4071



When the minimum and maximum degree n to be set is equal, the program calculates the contribution of the **The 2~1800th model gravity disturbance on geoid** be employed to analyze and evaluate the spectral and space properties of the geopotential coefficient model.

### (3) Calculate the total Bouguer effects and total equilibrium effects on gravity.



Integral of land-sea unified classical gravity Bouguer / equilibrium effect

Calculator of land-sea unified classical gravity Bouguer / equilibrium effect

Algorithms land-sea unified Bouguer and equilibrium

Open the land-sea terrain model file

Open the ellipsoidal height grid file of land-sea surface

Select calculation points file format  
ellipsoidal height grid file

Open the ellipsoidal height grid file on land-sea calculation surface

Integral radius for local terrain effect: 90 km

Integral radius for seawater Bouguer / equilibrium effect: 300 km

Equilibrium compensation depth: 30 km

>> Computation Process \*\* Operation Prompts

>> Open the land-sea terrain model file C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougequilibrium/extlandseadm2m.dat.

>> Open the ellipsoidal height grid file of land-sea surface C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougequilibrium/extlandseahgt2m.dat.

>> Open the ellipsoidal height grid file on land-sea calculation surface C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougequilibrium/extlandseahgt2m.dat.

>> Save the results as C:/PAGrav4.5\_win64en/examples/Terraininflexercise/GMBougequilibrium/BougEquinfi2m.txt0

\*\* Record format: Point no, longitude, latitude, ellipsoidal height, terrain height/sea depth, local terrain effect, plane layer effect, seawater Bouguer effect, land equilibrium effect, ocean equilibrium effect, total Bouguer effect and total equilibrium effect.

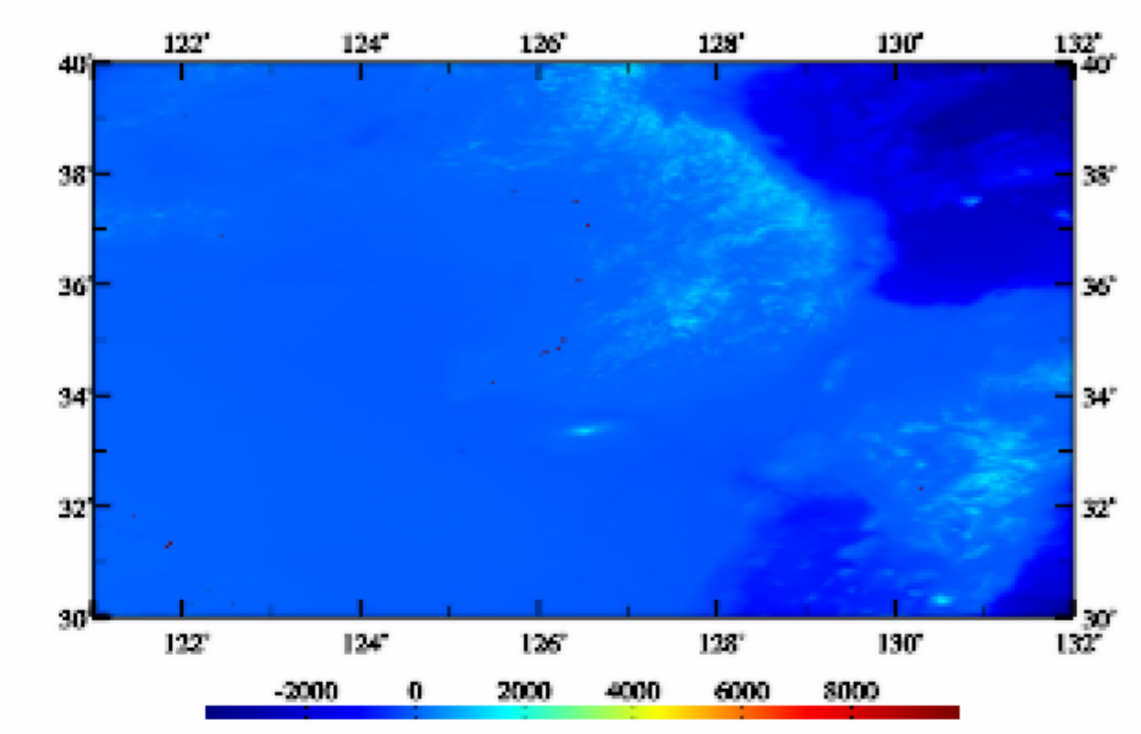
\*\* At the same time, the program also outputs the land-sea total Bouguer effect (\*.bgr) and land-sea total equilibrium effect (\*.ist) grid file into the current directory, where \* is the output file name entered from the interface.

Save the results as    Import setting parameters    Start Computation

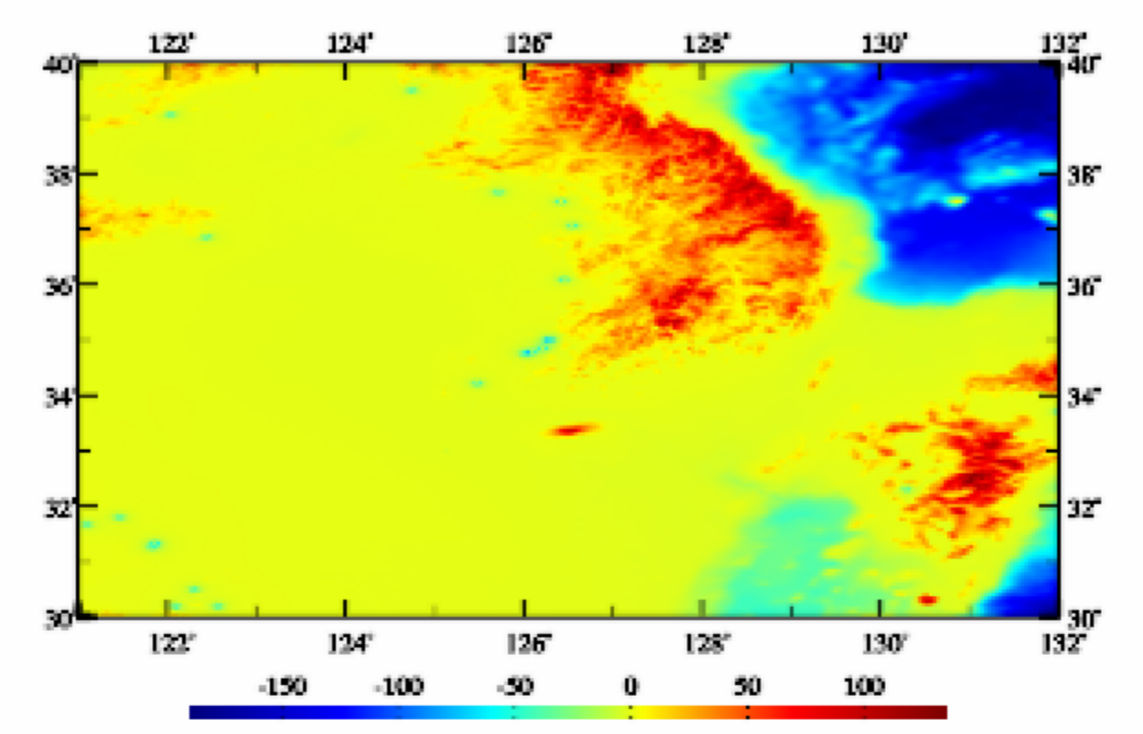
no	lon(deg/decimal)	lat	height/depth	local terrian	plane layer	sea water Bouguer effect	...
1	121.01667	30.01667	43.360	-0.0930	4.8550	-0.0052	-0.5258    0.0729
2	121.05000	30.01667	20.550	-0.0329	2.3010	-0.0053	-0.5820    0.0774
3	121.08333	30.01667	45.640	-0.1658	5.1102	-0.0056	-0.6299    0.0821
4	121.11667	30.01667	7.880	-0.0164	0.8823	-0.0057	-0.6957    0.0870
5	121.15000	30.01667	6.400	-0.0072	0.7166	-0.0058	-0.7545    0.0922
6	121.18333	30.01667	5.000	-0.0311	0.5598	-0.0060	-0.8137    0.0977

Extract effects

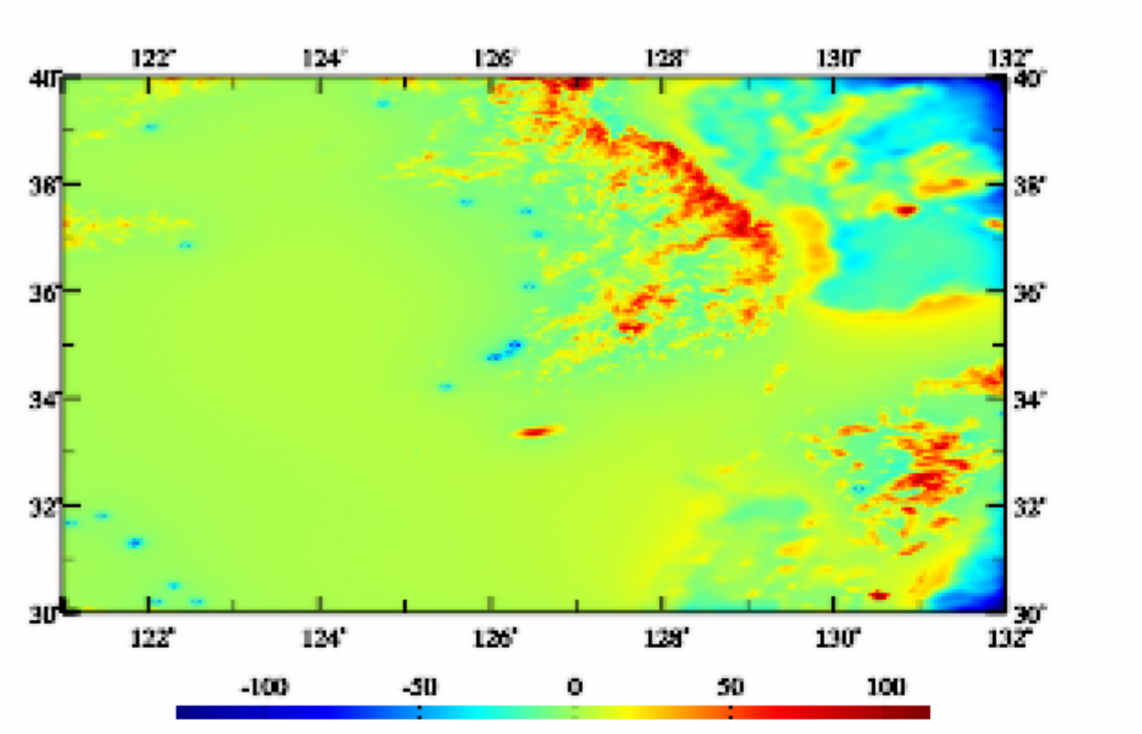
Plot↓



land-sea terrain model (m)



total Bouguer effect (mGal)



total equilibrium effect (mGal)

- Classic Bouguer gravity anomaly on geoid = gravity anomaly at the measurement point – total Bouguer effect – analytical continuation of gravity anomaly from the measurement point to the geoid. Classic Bouguer gravity disturbance on geoid = gravity disturbance at the measurement point – total Bouguer effect – analytical continuation of gravity disturbance from the measurement point to the geoid.
- Classic equilibrium gravity anomaly on geoid = gravity anomaly at the measurement point – total equilibrium effect – analytical continuation of gravity anomaly from the measurement point to the geoid. Classic equilibrium gravity disturbance on geoid = gravity disturbance at the measurement point – total equilibrium effect – analytical continuation of gravity disturbance from the measurement point to the geoid.

# (4) Generate the 2'x2' land-sea unified classical Bouguer / isostatic anomaly grid model.

Weighted operation on two specified attributes in record file | **Weighted operation on two geodetic grid files** | Weighted operation on two vector grid files | Weighted harmonic...

Open geodetic grid file 1 | Open geodetic grid file 2

Select operation mode: **Plus +**

Set weight: The first weight 1.00 | The second weight 1.00

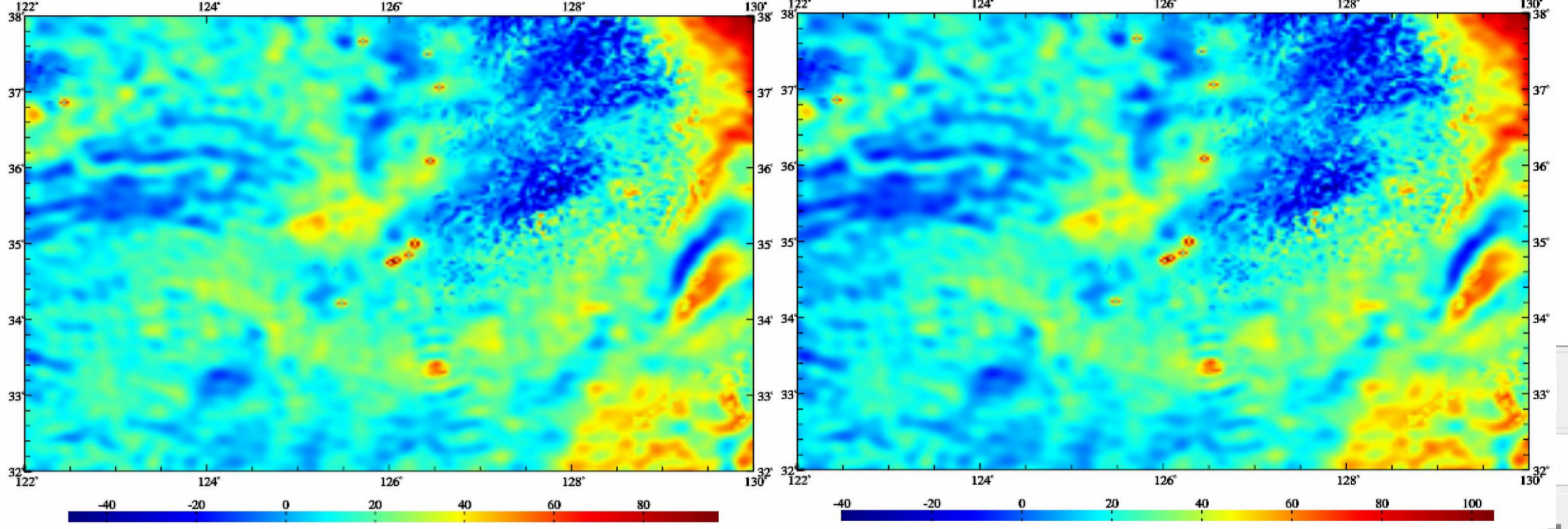
Vector grid operation

>> Program Process \*\* Operation Prompts

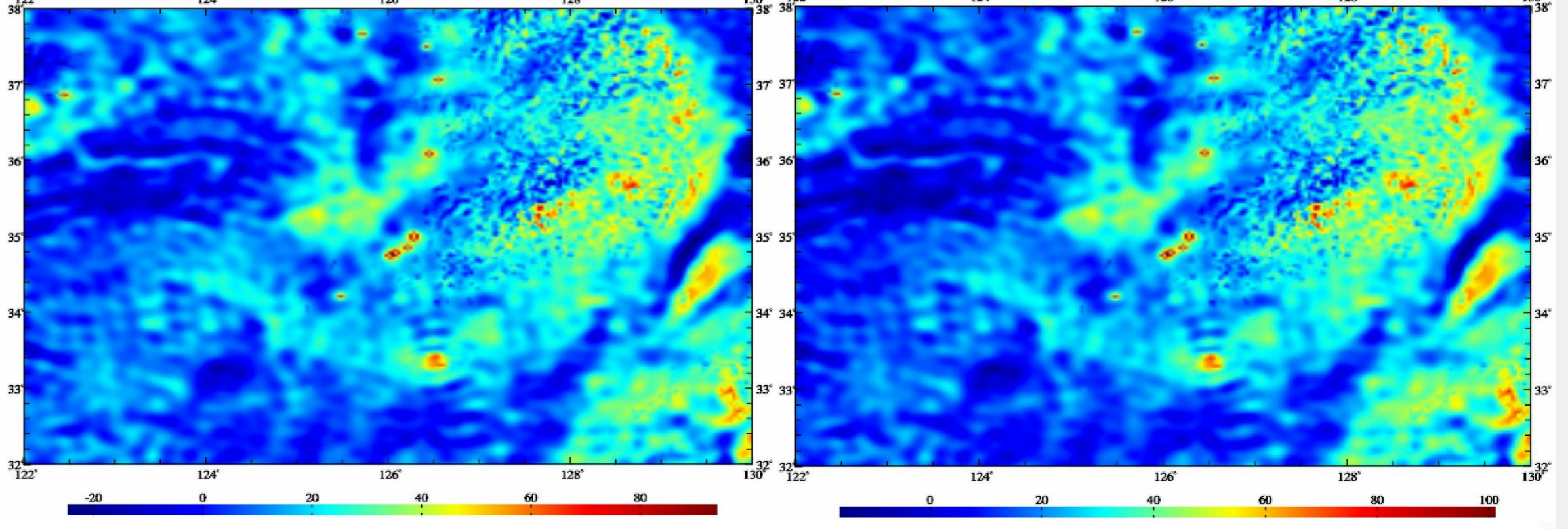
- >> Select the function module from the four control buttons at the top of the interface...
- >> [Function] Perform weighted plus, minus, or multiply operation on grid elements in two (vector) grid files with the same...
- >> Open geodetic grid file 1 C:/PAGravf4.5\_win64en/examples/Terraininflexercise/GMBougEquilibrium/EGM2008\_2m\_1800.gra.
- >> Open geodetic grid file 2 C:/PAGravf4.5\_win64en/examples/Terraininflexercise/GMBougEquilibrium/BougEquinfl2m0.bgr.
- >> Save the results as C:/PAGravf4.5\_win64en/examples/Terraininflexercise/GMBougEquilibrium/Istbggravanom2m.dat.
- >> The parameter settings have been entered into the system!
- \*\* Click the [Start Computation] control button, or the [Start Computation] tool button...
- >> Computation start time: 2023-03-19 10:06:41
- >> Complete the...
- >> Computation...
- >> Open geode...
- >> Open geode...
- >> Save the res...
- >> The paramet...
- \*\* Click the [St...
- >> Computation...
- >> Complete the...
- >> Computation...

Display of the input-output file ↓

122.000000	130.000000	32.000000	38.000000	0.03
8.3775	6.8966	5.6899	4.8540	
19.2133	17.4019	15.8291	14.7983	
24.3218	26.4713	28.0518	28.6086	
12.9158	10.3765	10.0539	11.7974	
15.3356	13.0657	11.4755	11.0485	
22.3411	22.1708	21.4036	20.3436	
12.8327	12.3341	11.1957	10.0041	
22.0979	22.6739	23.1295	23.1236	
23.9972	26.5997	28.6183	30.3440	
27.7904	27.6035	26.8185	26.0919	
36.7723	32.2543	27.9404	25.2177	
23.0243	24.8093	26.4821	28.4630	
60.4889	61.1129	60.1925	58.4199	
52.1456	47.6924	45.4768	45.1435	
9.4949	11.3991	12.7729	13.7259	
0.4051	-4.5601	-10.9319	-16.3954	
14.7698	13.3947	11.4517	9.3666	
22.1548	20.7063	19.4075	18.5611	
22.9153	25.1115	26.7739	27.3524	
16.1274	12.9445	12.2021	13.7358	
16.1741	13.6392	11.3091	9.8888	



The 2' land-sea unified classical Bouguer gravity anomaly and disturbance



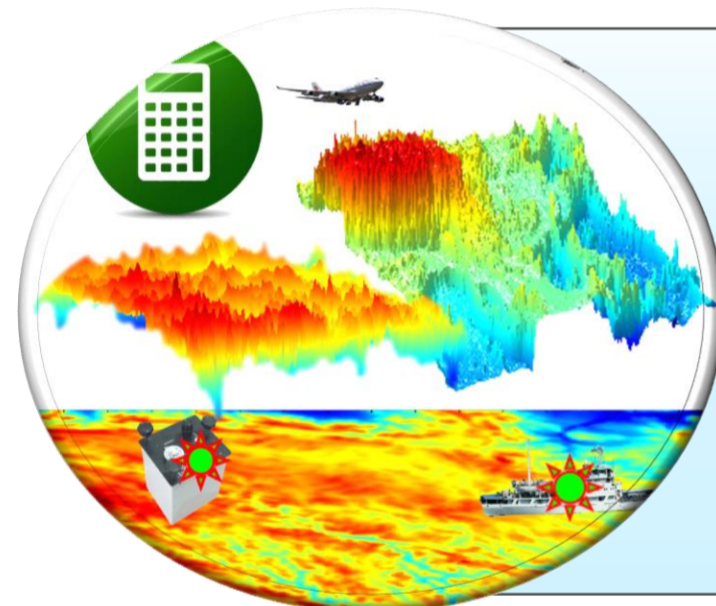
The 2' land-sea unified classical isostatic gravity anomaly and disturbance

**Precise Approach of Earth Gravity Field and Geoid**  
**PAGrav4.5**

Chinese Academy of Surveying & Mapping  
March 2023, Beijing, China



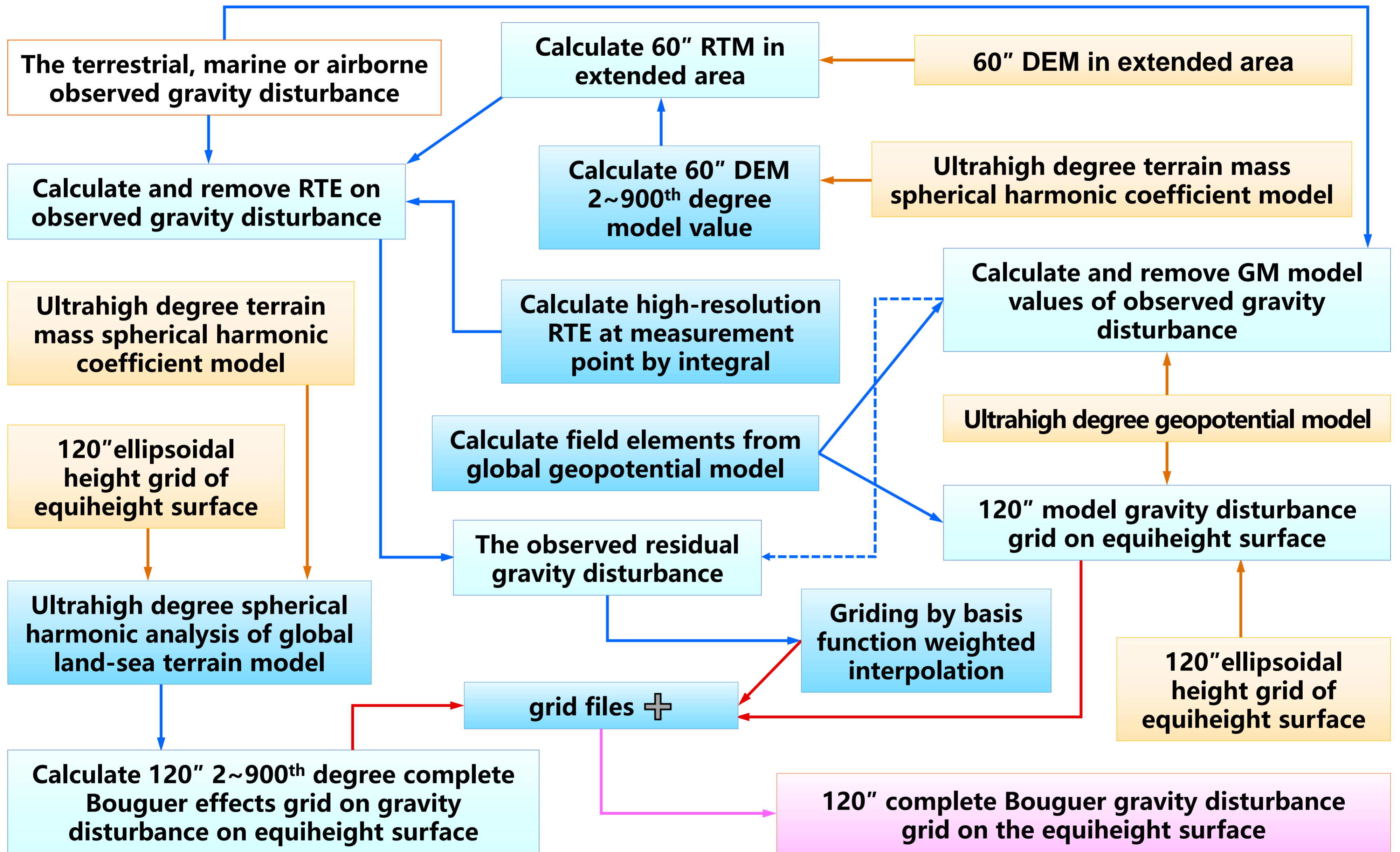
# Seven steps of computation, global land-sea universal!



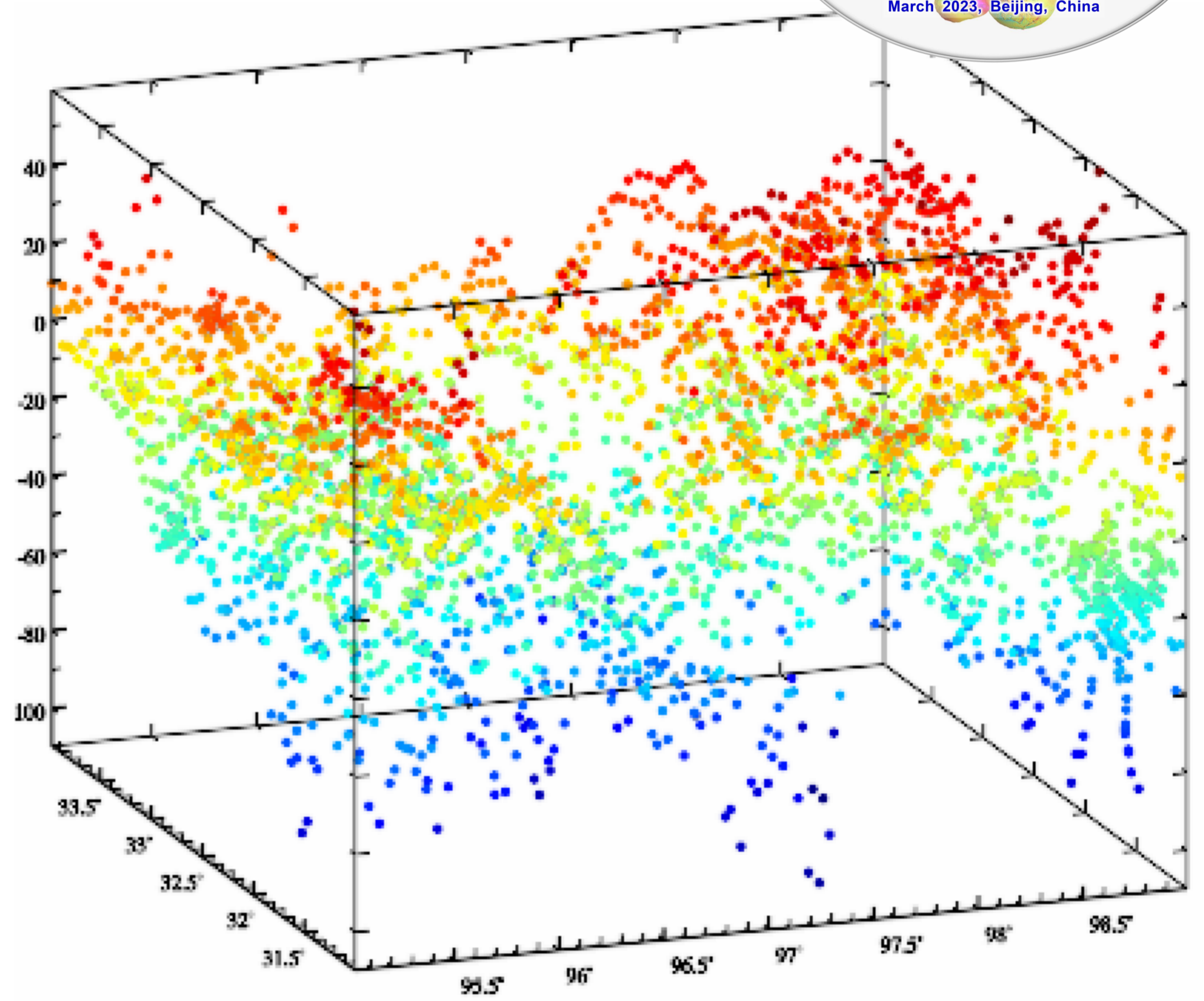
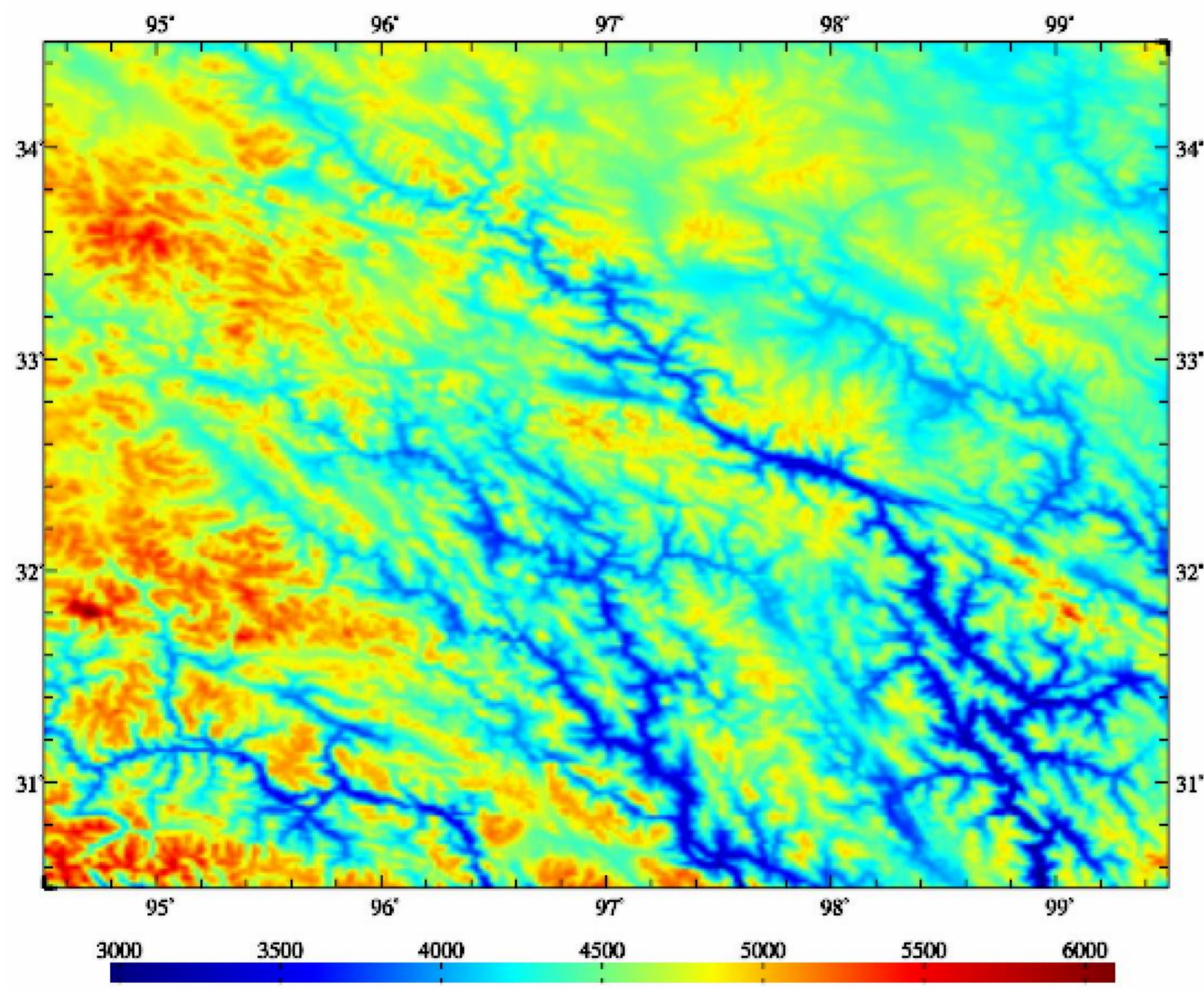
**Computation process demo of  
complete Bouguer anomaly on  
terrain equiheight surface**

- 🌍 The remove - restore scheme combining with global terrain mass spherical harmonic coefficient model and residual terrain effect.
- 🌍 The computation processes for complete Bouguer gravity anomaly (disturbance, and gradient) and vertical deflection are all exactly the same !





**Computation process demo of complete Bouguer anomaly on terrain equiheight surface**



Ground digital elevation model (m) and gravity measurement point distribution

# Construct the ground ellipsoidal height grid and ellipsoidal height grid of the terrain equiheight surface.

- Weighted operation on two specified attributes in record file
- Weighted operation on two geodetic grid files**
- Weighted operation on two vector grid files
- Weighted harmoni...

Open geodetic grid file 1

Open geodetic grid file 2

Select operation mode

Plus +

Set weight

The first weight 1.00

The second weight 1.00

Vector grid operation

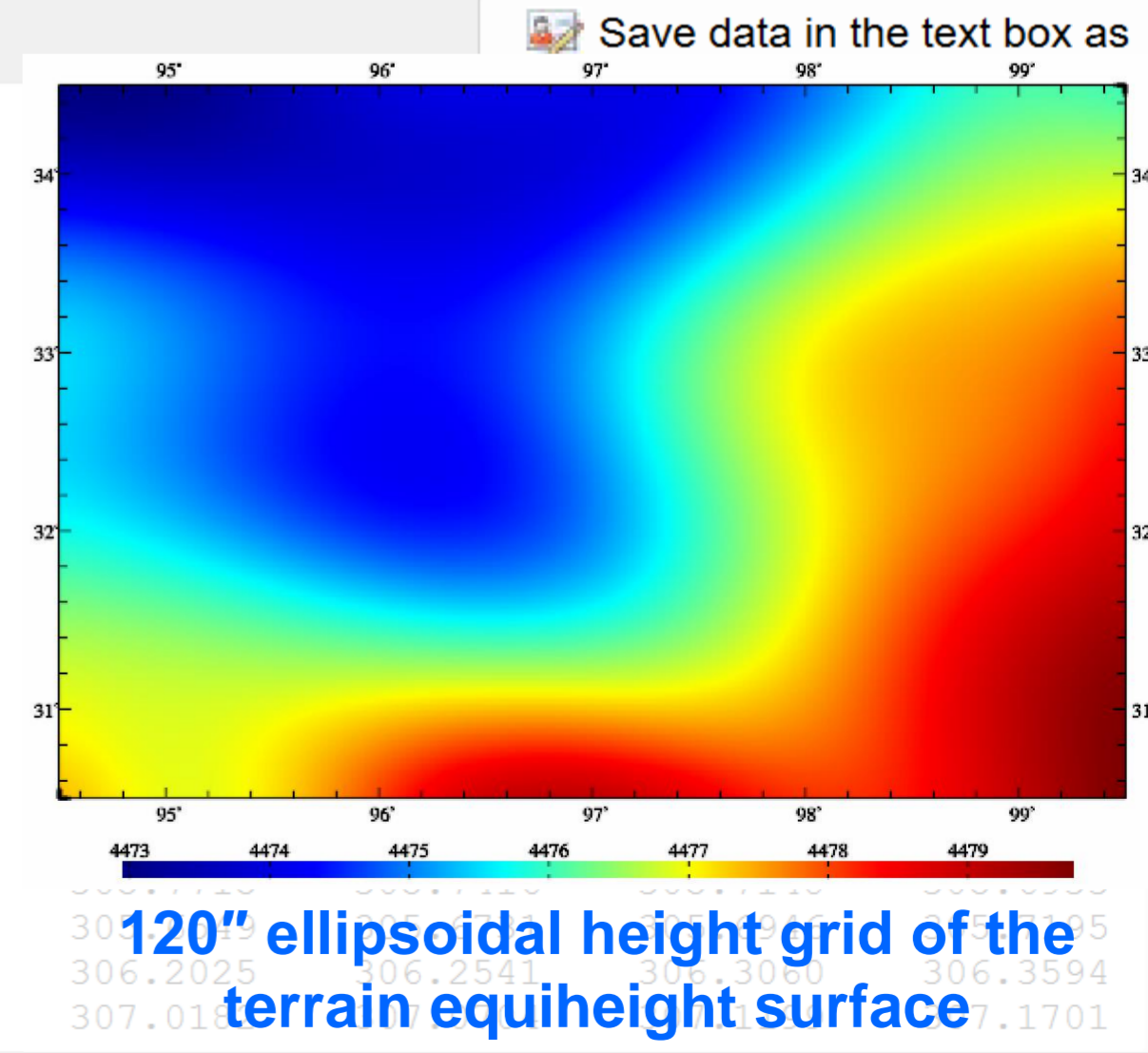
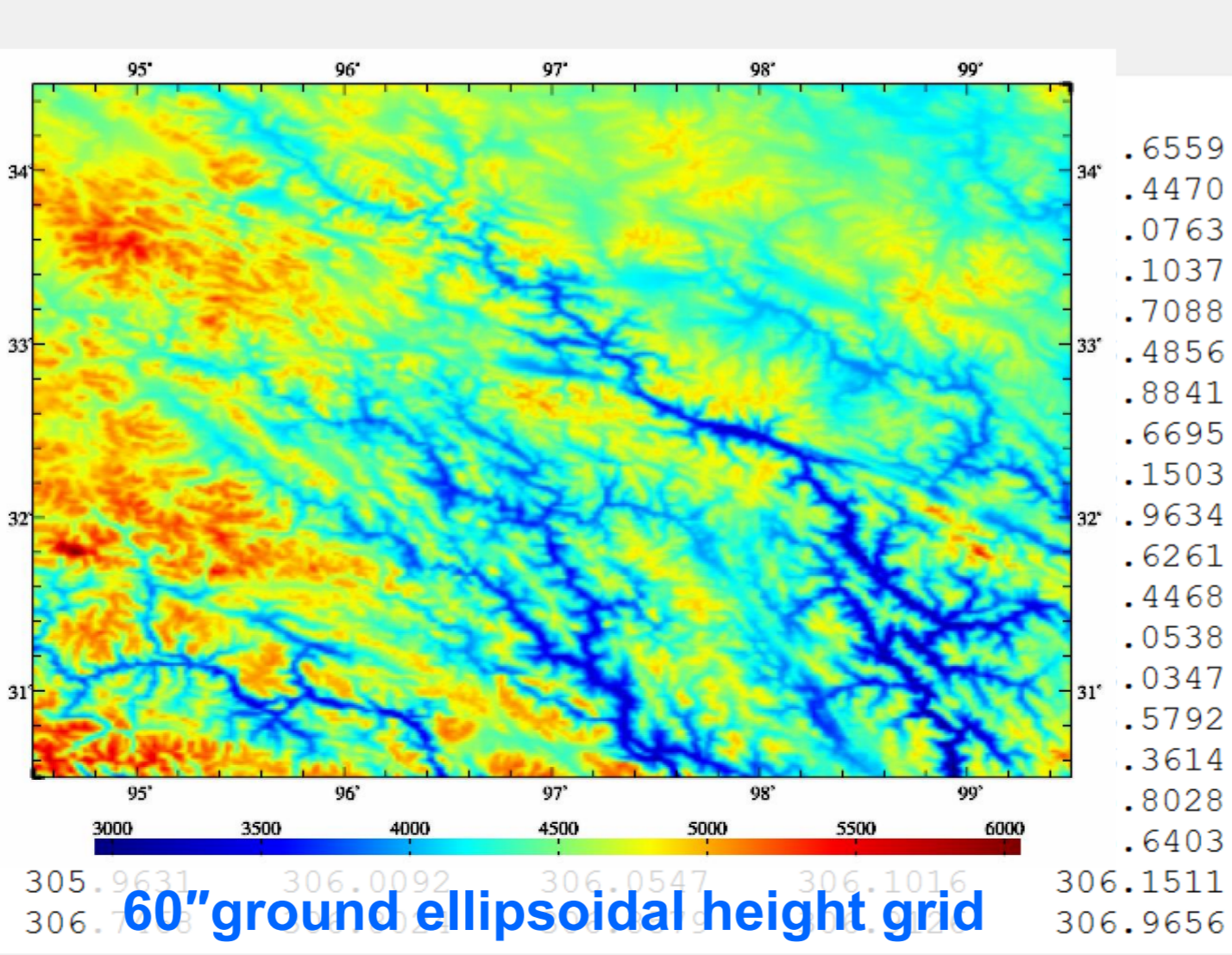
```
>> Program Process ** Operation Prompts
>> [Function] Perform weighted plus, minus, or multiply operation on grid elements in two (vector) grid files with specifications.
>> Open geodetic grid file 1 C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/extdtm60s.dat.
>> Open geodetic grid file 2 C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/EGM180ksi60s.dat.
>> Save the results as C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/surfhgt60s.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2023-03-18 12:37:44
>> Complete the computation!
>> Computation end time: 2023-03-18 12:37:44
>> Open geodetic grid file 1 C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/const339.5.dat.
>> Open geodetic grid file 2 C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/EGM180ksi120s.dat.
>> Save the results as C:/PAGravf4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/equihgt120s.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2023-03-18 12:44:42
>> Complete the computation!
>> Computation end time: 2023-03-18 12:44:42
```

The ground ellipsoidal height grid is employed to give the space location of the terrain surface for the integral operation.

Display of the input-output file↓

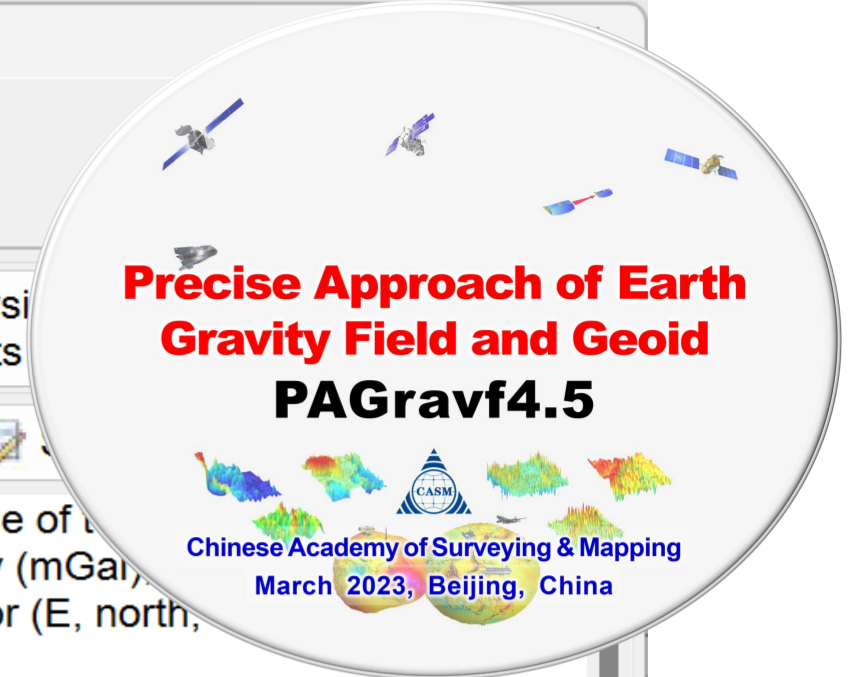
94.500000	99.500000	30.500000
304.9759	304.9250	304.8757
304.4461	304.4353	304.4261
304.6877	304.7340	304.7837
305.6230	305.6941	305.7651
306.5466	306.5795	306.6058
306.6824	306.6657	306.6451
306.1619	306.1215	306.0821
305.6821	305.6697	305.6585
305.8508	305.8859	305.9240
306.5752	306.6304	306.6856
304.9252	304.8780	304.8321
304.4372	304.4266	304.4191
304.6815	304.7264	304.7740
305.5747	305.6442	305.7135
306.4293	306.4679	306.4925
306.5528	306.5377	306.5189
306.0610	306.0205	305.9836
305.6288	305.6193	305.6156
305.8399	305.8782	305.9189
306.5802	306.6355	306.6912

- Save the results as
- Import setting parameters
- Start computation



Precise Approach of Earth Gravity Field and Geoid  
**PAGravf4.5**  
 Chinese Academy of Surveying & Mapping  
 March 2023, Beijing, China

# (1) Calculate and remove the model terrain height value, and then construct 60" residual terrain model (RTM) grids.



Open global land-sea terrain mass spherical harmonic coefficient model file

Select calculation file format  
Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

- Select elements to be calculated
- terrain height/sea depth (m)
  - height anomaly (m)
  - gravity anomaly/disturbance (mGal)
  - vertical deflection (" SW)
  - disturbing gradient (E, radial)
  - tangential gradient (E, NW)
  - disturbing potential/geopotential (m<sup>2</sup>/s<sup>2</sup>)

Minimum degree 1  
Maximum degree 900

>> Computation Process \*\* Operation Prompts

>> [Function] From global land-sea terrain mass spherical harmonic coefficient model (kg/m<sup>2</sup>), calculate the model value of  $\sigma$  as well as the land-sea unified complete Bouguer or residual terrain effects on the height anomaly (m), gravity anomaly (mGal), vertical deflection vector (" south, west), disturbing gravity gradient (E, radial), tangential gravity gradient vector (E, north, geopotential (m<sup>2</sup>/s<sup>2</sup>) on the geoid or in its outer space.

\*\* Click the [Open global land-sea terrain mass spherical harmonic coefficient model file] control button, or the [Open terrain model] tool button...

>> Open global land-sea terrain mass spherical harmonic coefficient model file C:/PAGrav4.5\_win64en/data/ETOPOcs1800.dat.

\*\* The window below only shows the geopotential coefficients data with no more than 2000 rows in it.

>> Open ellipsoidal height grid file of calculation surface C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/surfhgt60s.dat.

>> Save the results as C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/mldtm60s.txt.

\*\* The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of complete Bouguer or residual terrain effects.

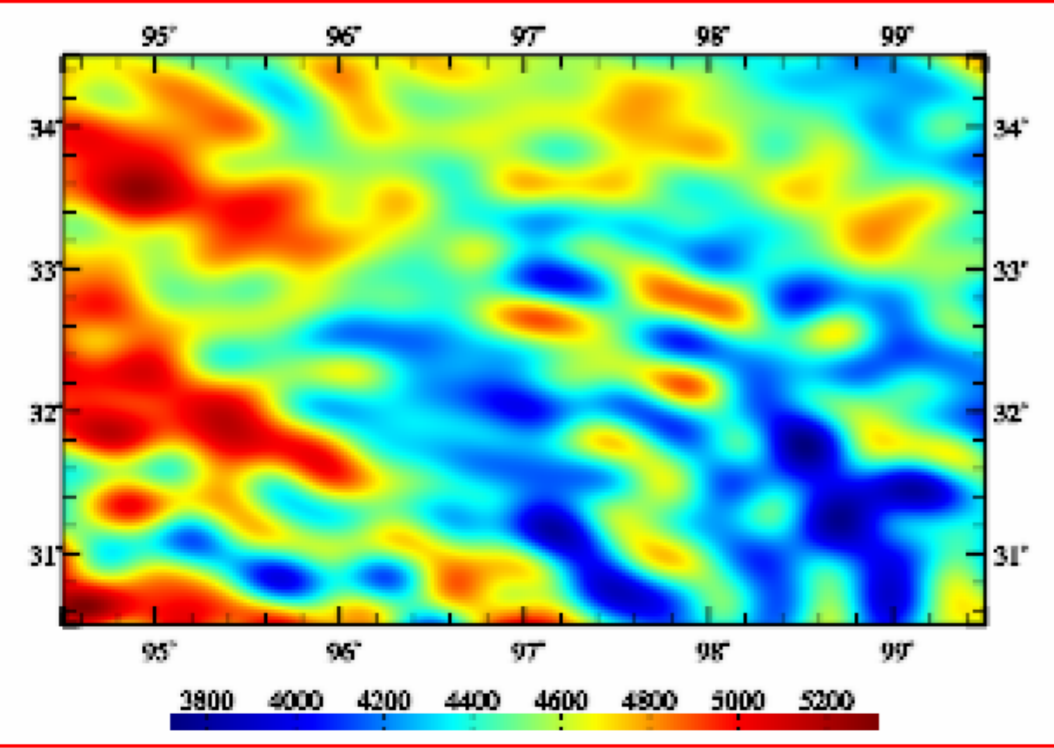
\*\* The program also outputs the model values grid file for the terrain height/sea depth (\*.dtm) complete Bouguer or residual terrain effects on height anomaly (\*.ksi), gravity anomaly (\*.gra), gravity disturbance (\*.rga), vertical deflection vector (\*.dft), disturbing gravity gradient (\*.grr), tangential gravity gradient vector (\*.hgd) or disturbing geopotential (\*.get) into the current directory, where \* is the output file name entered from the interface.

>> The parameter settings have been entered into the system!

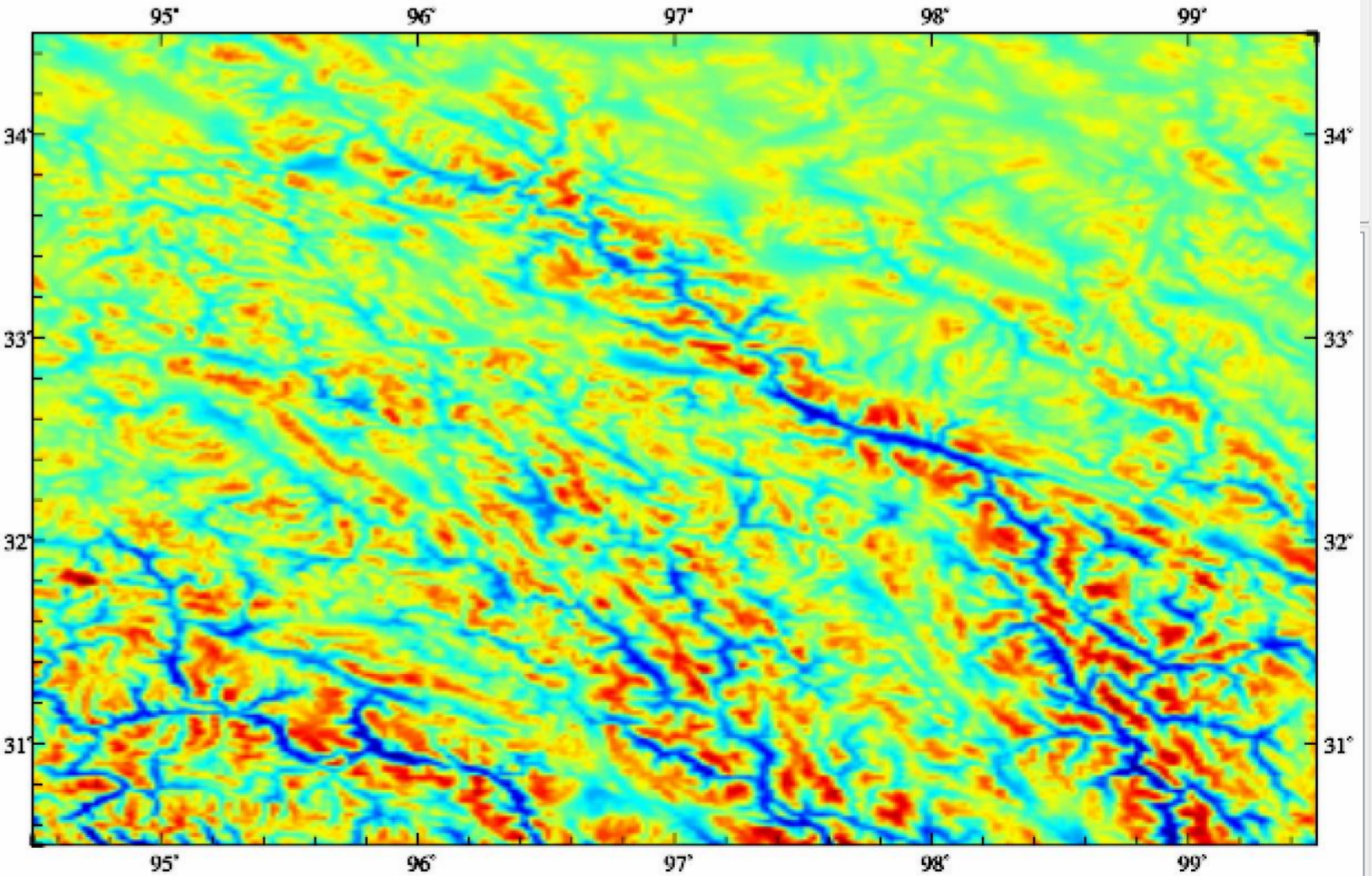
\*\* Click the [Start Computation] control button, or the [Start Computation] tool button.

Save the results as    Import setting parameters

1	94.50833	30.50833	4370.696	4853.86
2	94.52500	30.50833	4510.612	4874.82
3	94.54167	30.50833	4743.215	4891.56
4	94.55833	30.50833	4685.708	4903.66
5	94.57500	30.50833	4496.684	4910.88
6	94.59167	30.50833	4619.551	4913.11
7	94.60833	30.50833	5004.403	4910.42
8	94.62500	30.50833	5464.643	4903.03
9	94.64167	30.50833	5530.371	4891.54
10	94.65833	30.50833	5336.237	4876.10



terrain height/sea depth (m)



gravity effect (mGal)

The program is suitable for the unified computation of the complete Bouguer and residual terrain effects on various **60" residual terrain model (RTM) resdtm60s.dat** may be on the geoid and its outer Earth space.

## (2) Calculate and remove the ultrahigh-degree model gravity disturbance at the observed points.



- Calculation of gravity field elements from global geopotential model
- Calculation of model value for residual terrain (complete Bouguer) effects
- Global geopotential coefficient model Calculator
- Calculation and analysis of spectral character of Earth gravity field

Open global geopotential coefficient model file

Select calculation file format  
Discrete calculation point file

Open space calculation point location file

Set input point file format

Number of rows of file header: 1

Column ordinal number of ellipsoidal height in the record: 4

Select elements to be calculated

- height anomaly (m)
- gravity anomaly (mGal)
- gravity disturbance (mGal)
- vertical deflection (", SW)
- disturbing gravity gradient (E, radial)
- tangential gravity gradient (E, NW)
- Laplace operator (E)

Minimum degree: 2

Maximum degree: 720

Save computation process as

\*\* Click the [Open global geopotential coefficient model file] control button, or the [Open geopotential model] tool button.

>> Open global geopotential coefficient model file C:/PAGrav4.5\_win64en/data/EGM2008.gfc.

\*\* The window below only shows the geopotential coefficients data with no more than 2000 rows in it.

>> Open space calculation point location file C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/obsgrav.txt.

\*\* Look at the file information in the window below and set the discrete point file format...

>> Save the results as C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/Obsgravmdl.txt.

\*\* Behind the record of the calculation point file, appends one or more columns of model values of anomalous field elements, and keeps 4 significant figures.

>> The parameter settings have been entered into the system!

\*\* Click the [Start Computation] control button, or the [Start Computation] tool button...

\*\* The calculation process need wait, during which you can open the output file to look at the calculation progress...

>> Computation start time: 2023-03-18 13:24:55

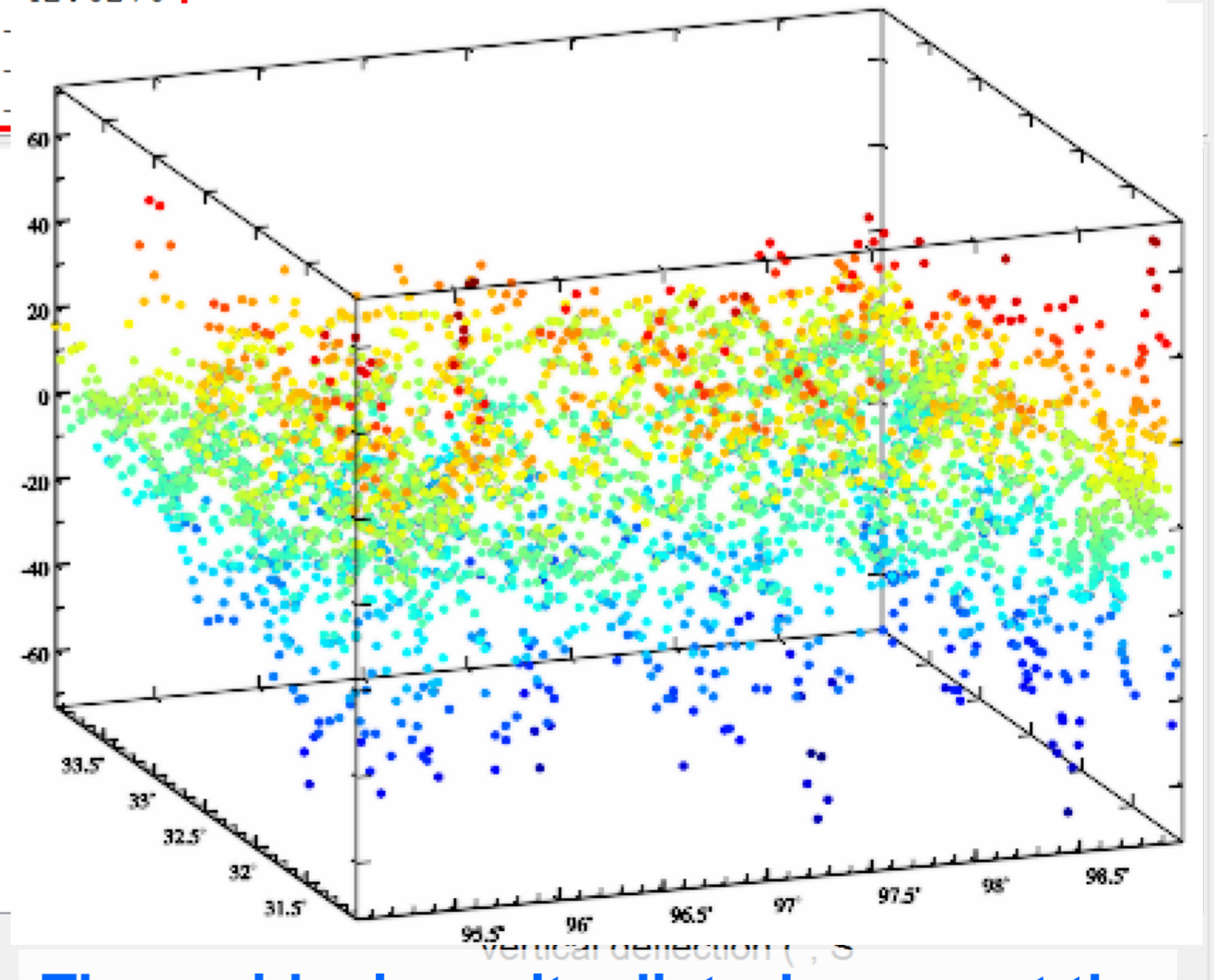
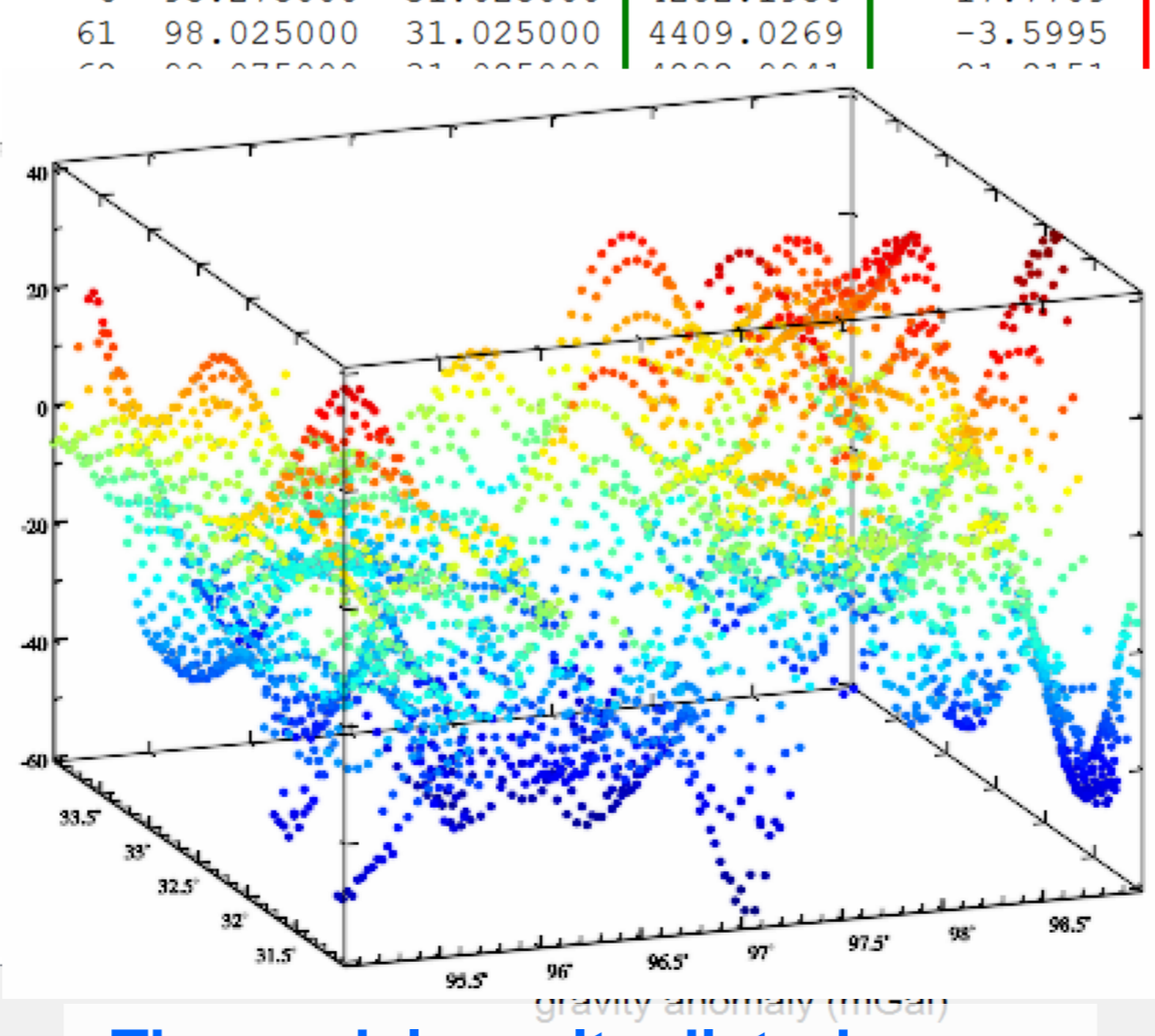
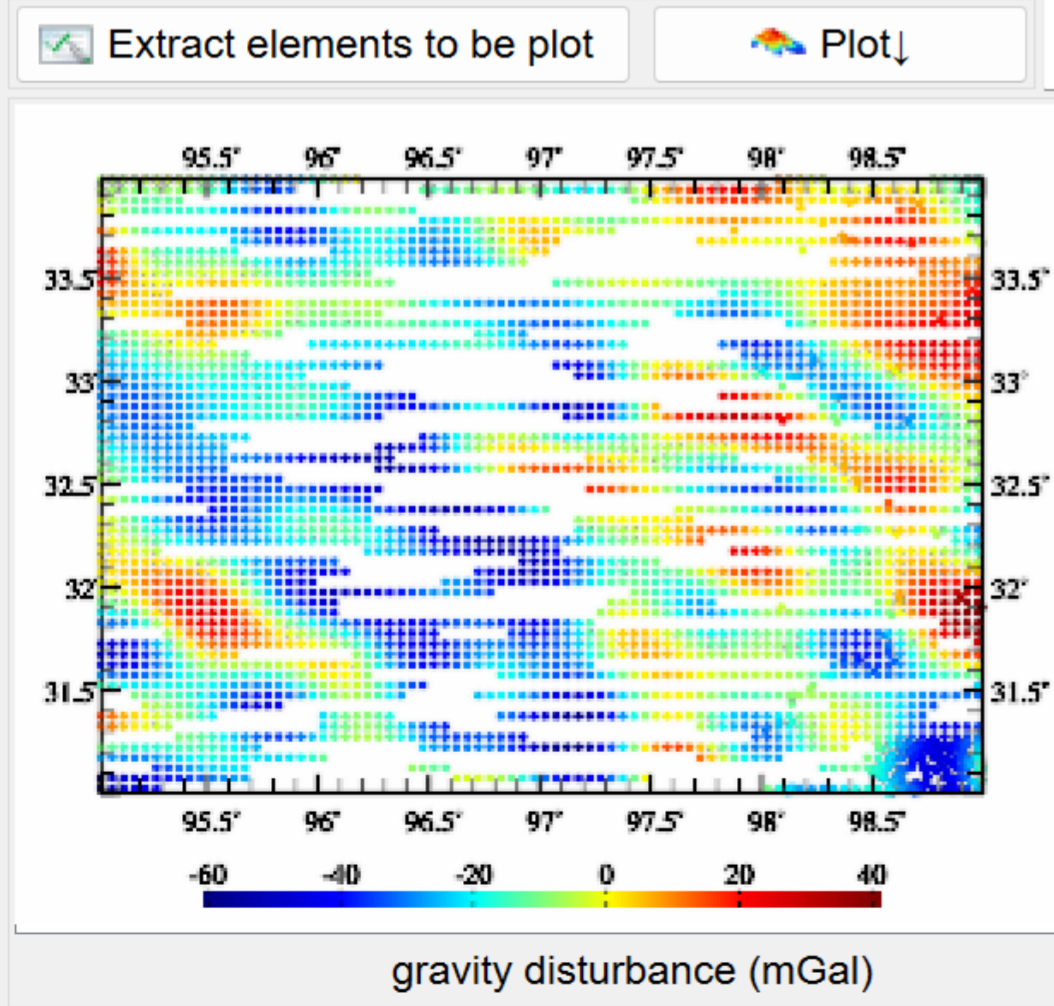
>> Complete the calculation of the model value of (residual) gravity field element!

>> Computation end time: 2023-03-18 13:27:24

Save the results as    Import setting parameters    Start Computation

no	lon(degree decimal)	lat	ellipsoid height(m)	rga(mGal)
1	95.025000	31.025000	4593.2264	-27.6576
2	95.075000	31.025000	4224.9678	-22.1858
3	95.125000	31.025000	4587.8601	-17.4344
4	95.175000	31.025000	4537.8310	-19.4157
5	95.225000	31.025000	4385.2290	-21.9257
6	95.275000	31.025000	4282.1950	-17.7709
61	98.025000	31.025000	4409.0269	-3.5995

-49.5225  
-49.1208  
-46.0653  
-44.5180  
-43.5038  
-42.6270



When the minimum and maximum degree n to be set is equal, the program calculates the contribution of the degree n geopotential coefficients to the anomalous gravity field element, which can be employed to analyze and evaluate the spectral and space properties of the geopotential model.

The model gravity disturbances at the observed points (mGal)

The residual gravity disturbances at the observed points (mGal)

### (3) Calculate and remove the residual terrain effects on the gravity disturbance at the observed points.



Numerical integral of land-sea residual terrain effects on various gravity field elements

FFT algorithm of land-sea residual terrain effects on various gravity field elements

Calculator of land-sea residual terrain effect or...

Open high-resolution land-sea terrain model file

Open the land-sea low-pass terrain model file

Open the ellipsoidal height grid file of the land-sea surface

Select calculation point file format  
discrete calculation points file

Open the calculation point position file

Set input point file format

Number of rows of file header 1

Column ordinal number of ellipsoidal height in the record 4

Select gravity field elements

height anomaly (m)

gravity anomaly (mGal)

gravity disturbance (mGal)

vertical deflection (", SW)

disturbing gravity gradient (E, radial)

Integral radius 90 km

Extract effects Plot

>> Computation Process \*\* Operation Prompts

\*\* The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also used to separate land and sea areas. Since the finite radius integral cannot deal with terrain zero-degree term, the program removes the average of the residual terrain model (RTM) grid.

>> Open the high-resolution land-sea terrain model file C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/extdtm060s.dtm.

>> Open the land-sea low-pass terrain model file C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/mldtm60s.dtm.

>> Open the ellipsoidal height grid file of the land-sea surface C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/surfhgt60s.dat.

>> Open the calculation point location file C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/Obsgravmdresd.txt.

\*\* Look at the file information in the window below, set the input file format parameters...

>> Save the results as C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/Obsgravresdtm.txt.

\*\* Record format: Behind the source calculation points file record, appends several columns of residual terrain effects on specified types of field elements, keeps 4 significant figures.

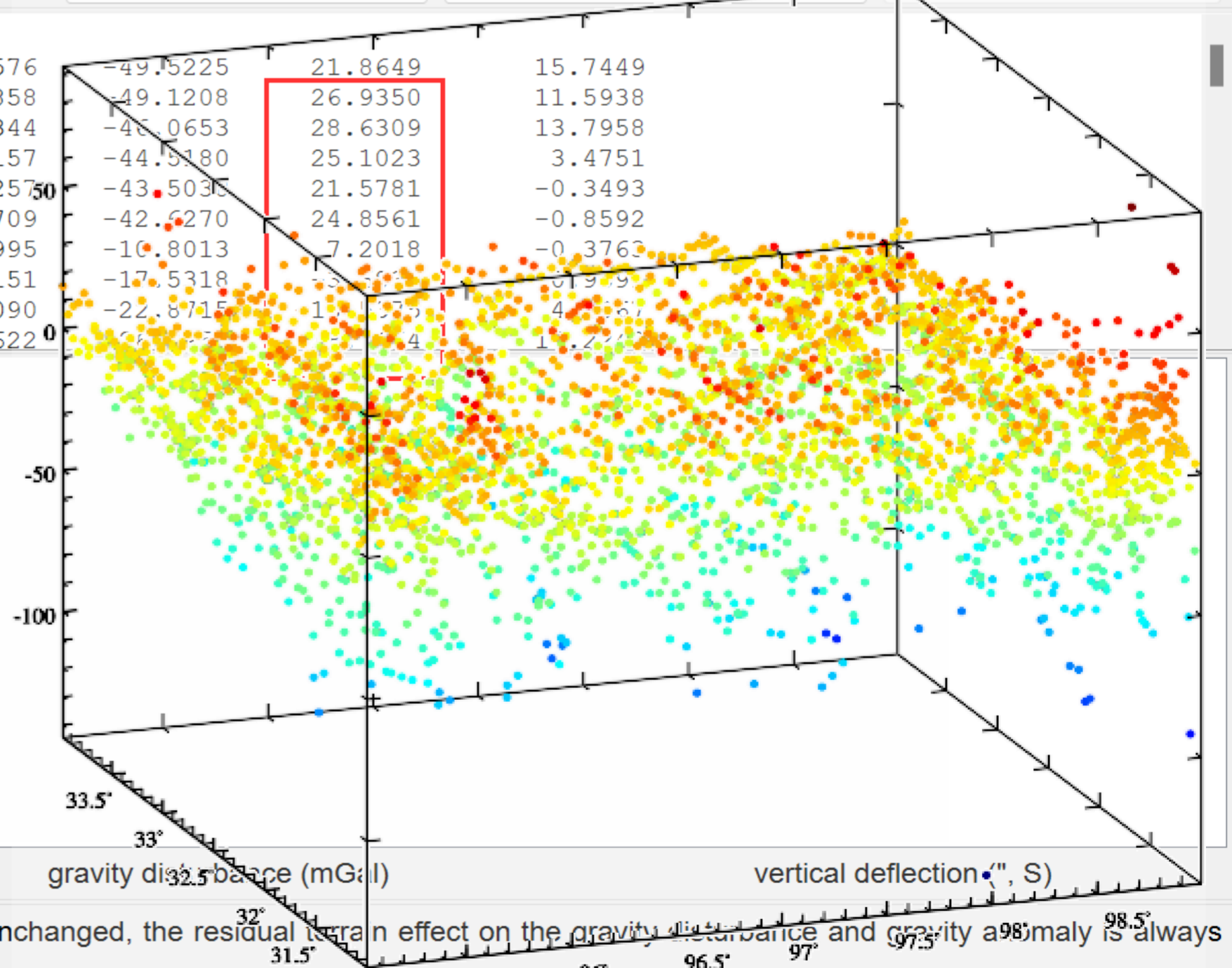
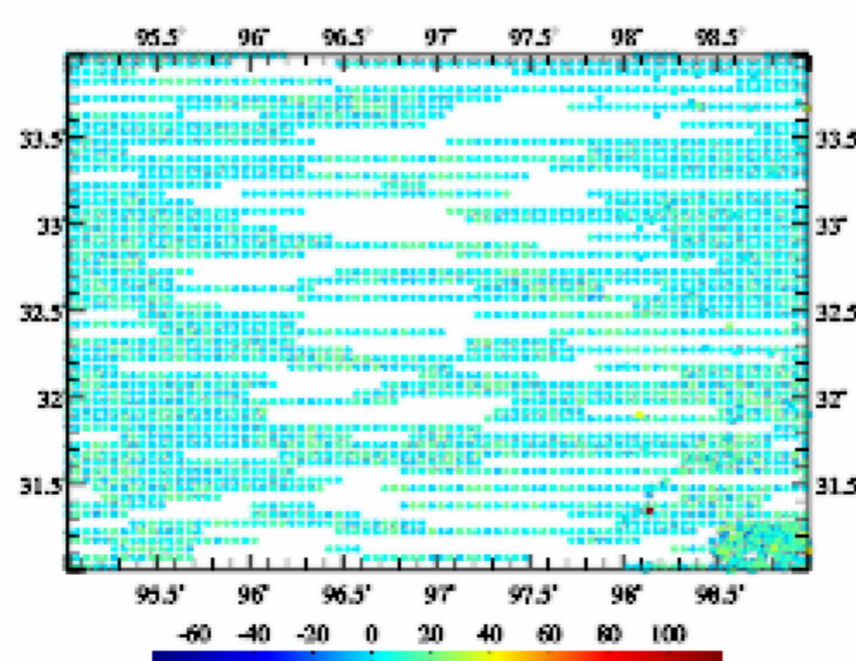
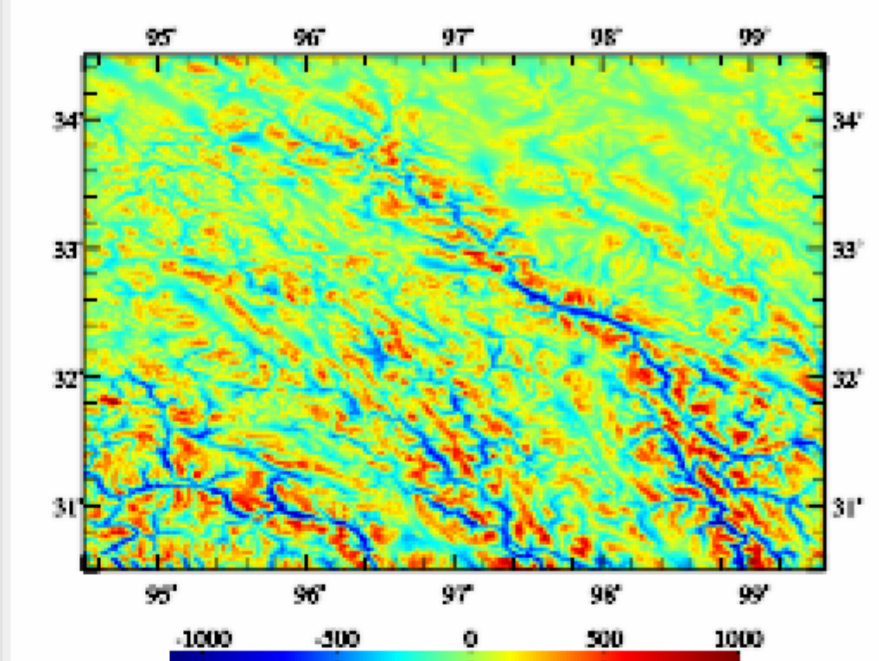
>> The parameter settings have been entered into the system!

\*\* Click the [Start Computation] control button, or the [Start Computation] tool button...

>> Computation start time: 2023-03-18 16:18:50

no	lon(degree decimal)	lat	elliphgt(m)	rga(mGal)
1	95.025000	31.025000	4593.2264	-27.6576
2	95.075000	31.025000	4224.9678	-22.1858
3	95.125000	31.025000	4587.8601	-17.4344
4	95.175000	31.025000	4537.8310	-19.4157
5	95.225000	31.025000	4385.2290	-21.9257
6	95.275000	31.025000	4282.1950	-17.7709
61	98.025000	31.025000	4409.0269	-3.5995
62	98.075000	31.025000	4282.9941	-21.2151
63	98.125000	31.025000	4129.0804	-36.4090
64	98.175000	31.025000	3972.1226	-45.0622

Save the results as Import setting parameters Start Computation



residual terrain model (m) gravity disturbance (mGal) gravity disturbance (mGal) vertical deflection (", S)

The calculation point may be on the geoid and its outer near-Earth space. Since the normal gravity field keeps unchanged, the residual terrain effect on the gravity disturbance and gravity anomaly is always equal to the residual terrain effect on gravity.

The program subtracts the land-sea high-resolution terrain model and land-sea low-pass terrain model with the same grid specifications to generate the land-sea residual terrain model (RTM) grid, while the land-sea high-resolution terrain model is also employed to separate land and sea areas.

**The remaining residual gravity disturbance (mGal)**

# (4) Gridding on the remaining residual gravity disturbance into 120"×120" grids on the terrain equiheight surface.

Save process Follow example

Gross error detection on observations based on low-pass reference surface

Estimation of observation weight with specified reference attribute

Gridding of heterogeneous data by basis function weighted interpolation

Save computation process as

The discrete geodetic observation file

Number of rows of file header 1

Column ordinal number of the attribute to be grid 9

Select the basis function

Gauss function  Equal weight

```
>> Select the computation function from the three control buttons at the top of the interface...
>> [Function] According to the given grid specifications (grid range and spatial resolution), and specified basis function, grid the specified attribute in the input discrete geodetic point file by the weighted basis function interpolation method.
>> Open the discrete geodetic file C:/PAGrav4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/Obsgravresidual.txt.
** Look at the file information in the window below and set the discrete point file format...
>> Save the results as C:/PAGrav4.5_win64en/examples/Terraininflexercise/TerComplbgprocess/distgravresidual.dat.
>> The parameter settings have been entered into the system!
** Click the [Start Computation] control button, or the [Start Computation] tool button...
>> Computation start time: 2023-03-18 16:43:27
>> Complete computation!
>> Computation end time: 2023-03-18 16:43:32
```

Save the results as

Import setting parameters

Start Computation

Set parameters

Number of neighboring points 50  
Kurtosis of basis function [1,20] 2

Grid specification

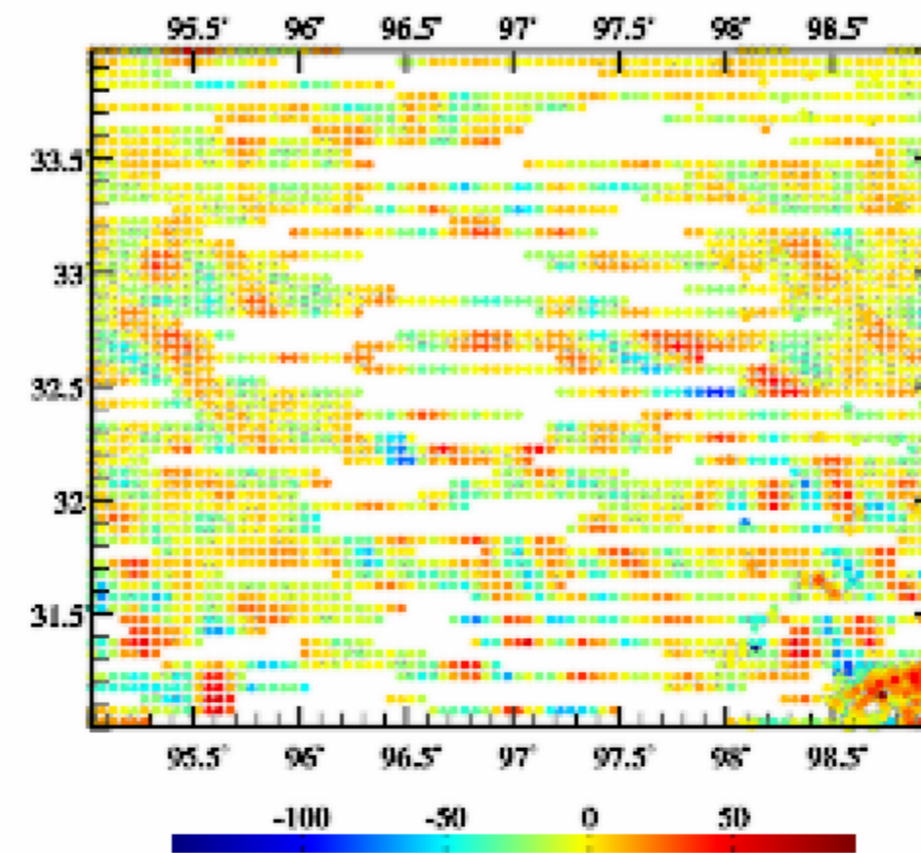
minLon resolution maxLon minLat maxLat  
95.000° 2.000' 99.000° 34.000°

120" remaining residual gravity disturbance grid (mGal) on the terrain equiheight surface

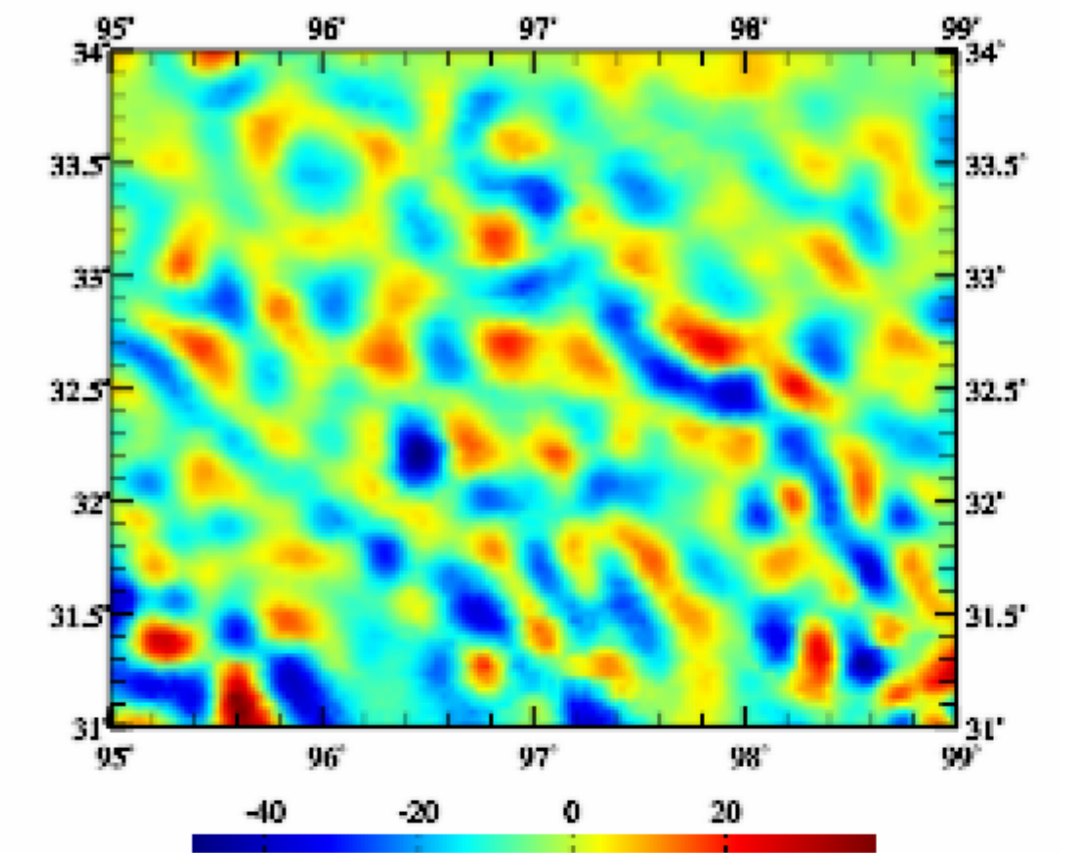
95.000000	99.000000	31.000000	34.000000	0.03333333	0.03333333
5.4912	8.7346	10.0258	9.1047	9.9525	
7.6809	14.2793	21.6982	28.5658	33.5367	
-31.0776	-29.7887	-24.5498	-22.4716	-17.8027	
-11.7546	-15.4609	-17.2719	-18.3561	-20.0680	
-2.3418	-5.2626	-8.2132	-16.2106	-22.0369	
-12.0456	-7.3175	-6.0417	-3.5252	-2.4801	
-9.2724	-11.8917	-11.3700	-11.1539	-16.4457	
-10.2183	-7.1565	-7.2403	-8.4751	-13.4060	
1.0154	5.4660	6.6695	8.5389	9.7455	
4.0836	16.2977	27.4113	35.9807	36.5720	
-31.4164	-28.5338	-22.7653	-20.4875	-17.8144	
-12.4799	-13.7954	-17.4646	-19.9317	-19.4601	
-3.7885	-1.9273	-5.5496	-10.5246	-20.7430	
-10.8099	-7.2387	-3.9721	-3.4047	-0.9118	
-10.2555	-10.7004	-11.4279	-14.0407	-14.5682	
-5.0738	-3.5202	-0.0956	-0.7535	-3.8726	
18.5835	15.3227	30.5333	38.5316	39.0230	
19.1166	15.7261	19.2651	-19.7318	-15.0054	
-14.7191	-15.4833	-17.5097	-20.1974	-19.2414	

Omit the analytical continuation process for the remaining residual gravity disturbance here.

Extract plot data



Source observations input



Gridding results

# (5) Calculate the 120" EGM2008 2~720<sup>th</sup> degree model value grid of the gravity disturbance on the terrain equiheight surface.



Calculation of gravity field elements from global geopotential model

Calculation of model value for residual terrain (complete Bouguer) effects

Global geopotential coefficient model Calculator

Calculation and character of E

Open global geopotential coefficient model file

Select calculation file format

Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select elements to be calculated

- height anomaly (m)
- gravity anomaly (mGal)
- gravity disturbance (mGal)
- vertical deflection (", SW)
- disturbing gravity gradient (E, radial)
- tangential gravity gradient (E, NW)
- Laplace operator (E)

Minimum degree 2

Maximum degree 720

Save computation process as

>> Open ellipsoidal height grid file of calculation surface C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbg/equiht120s1.dat.

>> Save the results as C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/distgravmdl.txt.

\*\* The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of anomalous field elements.

\*\* The program also outputs (residual) height anomaly (\*.ksi), gravity anomaly (\*.gra) gravity disturbance (\*.rga) vertical deflection vector (\*.dft), disturbing gravity gradient (\*.grr), tangential gravity gradient vector (\*.hgd) or Laplace operator (\*.lps) model value grid file into the current directory. Where \* is the output file name entered in the interface, and the program outputs the corresponding (residual) model value grid file according to the selected gravity field element type.

>> The parameter settings have been entered into the system!

\*\* Click the [Start Computation] control button, or the [Start Computation] tool button...

\*\* The calculation process need wait, during which you can open the output file to look at the calculation progress...

>> Computation start time: 2023-03-18 13:48:20

>> Complete the calculation of the model value of (residual) gravity field element!

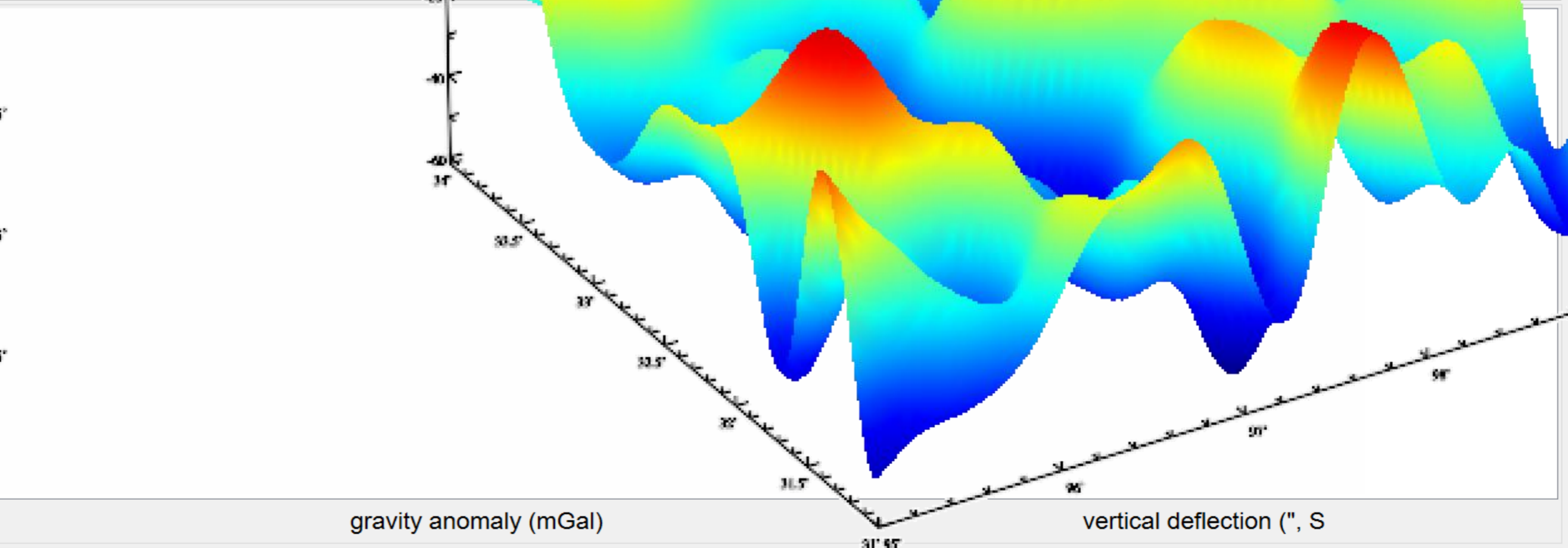
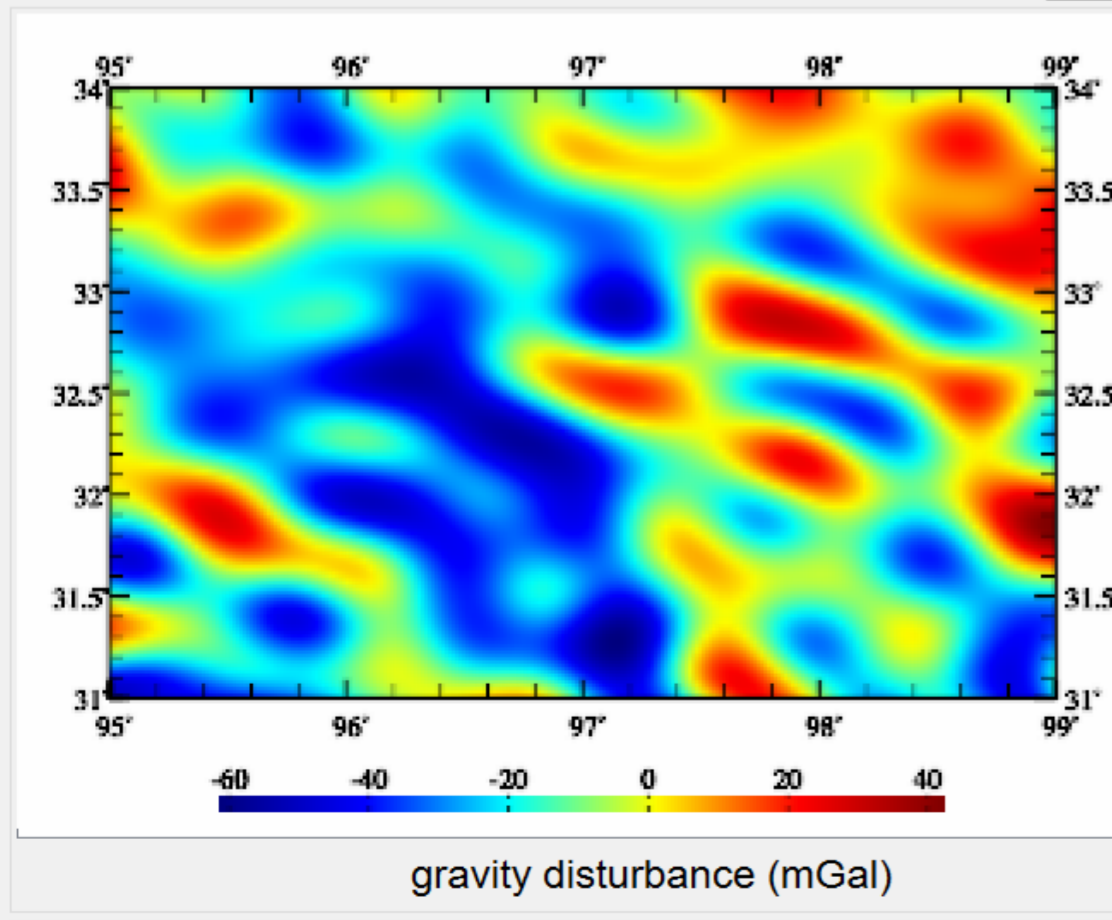
>> Computation end time: 2023-03-18 13:52:30

Save the results as

Import setting parameters

Start Computation

C:/PAGrav4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/



When the minimum and maximum degree n to be set is equal, the program calculates the contribution of the degree n geopotential coefficients to the anomalous gravity field element, which can be employed to analyze and evaluate the spectral and space properties of the geopotential coefficient model.



## (6) Calculate the 120" model complete Bouguer effect grid on the gravity disturbance on the terrain equiheight surface.

Calculation of model value for complete Bouguer or residual terrain effects

Calculator of global land-sea terrain effects model

Calculation and analysis of s of global terrain effects mod

Open global land-sea terrain mass spherical harmonic coefficient model file

Select calculation file format

Ellipsoidal height grid file

Open ellipsoidal height grid file of calculation surface

Select elements to be calculated

- terrain height/sea depth (m)
- height anomaly (m)
- gravity anomaly/disturbance (mGal)
- vertical deflection (" , SW)
- disturbing gradient (E, radial)
- tangential gradient (E, NW)
- disturbing potential/geopotential (m<sup>2</sup>/s<sup>2</sup>)

Minimum degree 2

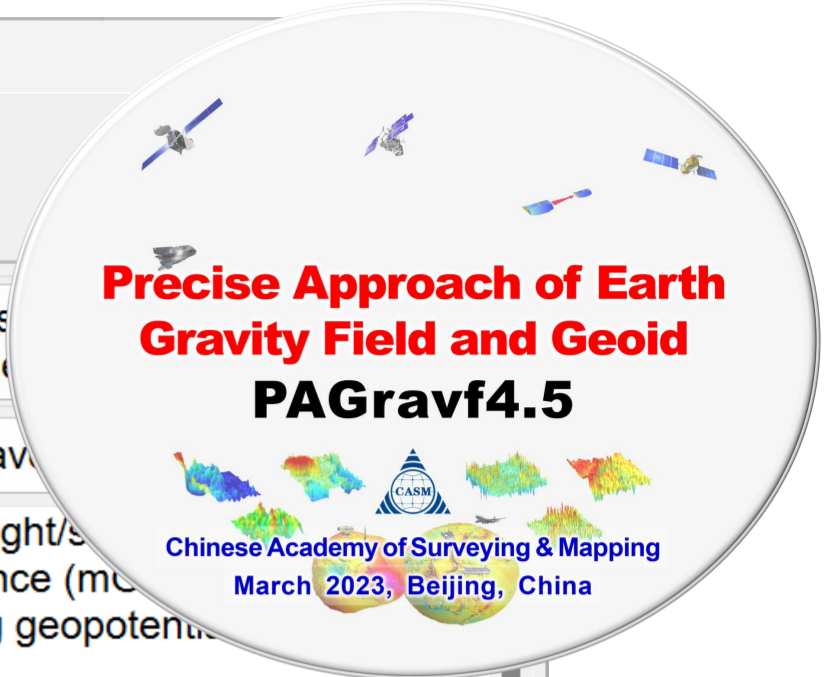
Maximum degree 900

Save the results as C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/equihgt120s1.dat.

Save the results as C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/distgravmdlcmpbg.txt.

gravity disturbance (\*.rga) vertical deflection vector (\*.dft), disturbing gravity gradient (\*.grr), tangential gravity gradient vector (\*.hgd) or disturbing geopotential (\*.get) into the current directory, where \* is the output file name entered from the interface.

Start Computation



>> Computation Process \*\* Operation Prompts

>> [Function] From global land-sea terrain mass spherical harmonic coefficient model (kg/m<sup>2</sup>), calculate the model value of terrain height/s the land-sea unified complete Bouguer or residual terrain effects on the height anomaly (m), gravity anomaly (mGal), gravity disturbance (m), deflection vector (" , south, west), disturbing gravity gradient (E, radial), tangential gravity gradient vector (E, north, west), or disturbing geopotential the geoid or in its outer space.

\*\* Click the [Open global land-sea terrain mass spherical harmonic coefficient model file] control button, or the [Open terrain model] tool button...

>> Open global land-sea terrain mass spherical harmonic coefficient model file C:/PAGravf4.5\_win64en/data/ETOPOcs1800.dat.

\*\* The window below only shows the geopotential coefficients data with no more than 2000 rows in it.

>> Open ellipsoidal height grid file of calculation surface C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/equihgt120s1.dat.

>> Save the results as C:/PAGravf4.5\_win64en/examples/Terraininflexercise/TerComplbgprocess/distgravmdlcmpbg.txt.

\*\* The record format: point no/name, longitude, latitude, ellipsoidal height, several columns of the model values of complete Bouguer or residual terrain effects.

\*\* The program also outputs the model values grid file for complete Bouguer or residual terrain effects on height anomaly (\*.ksi), gravity anomaly (\*.gra), gravity disturbance (\*.rga) vertical deflection vector (\*.dft), disturbing gravity gradient (\*.grr), tangential gravity gradient vector (\*.hgd) or disturbing geopotential (\*.get) into the current directory, where \* is the output file name entered from the interface.

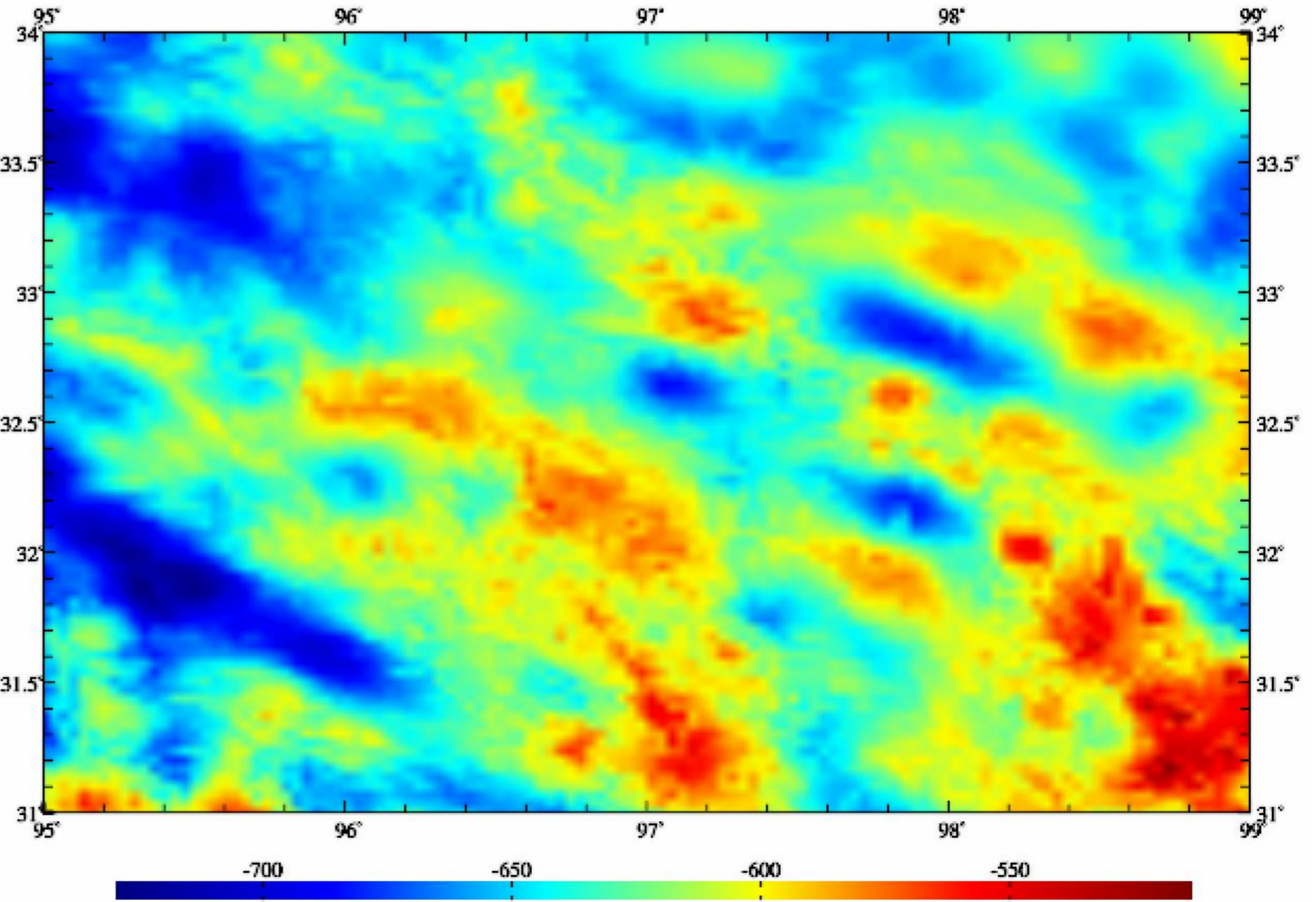
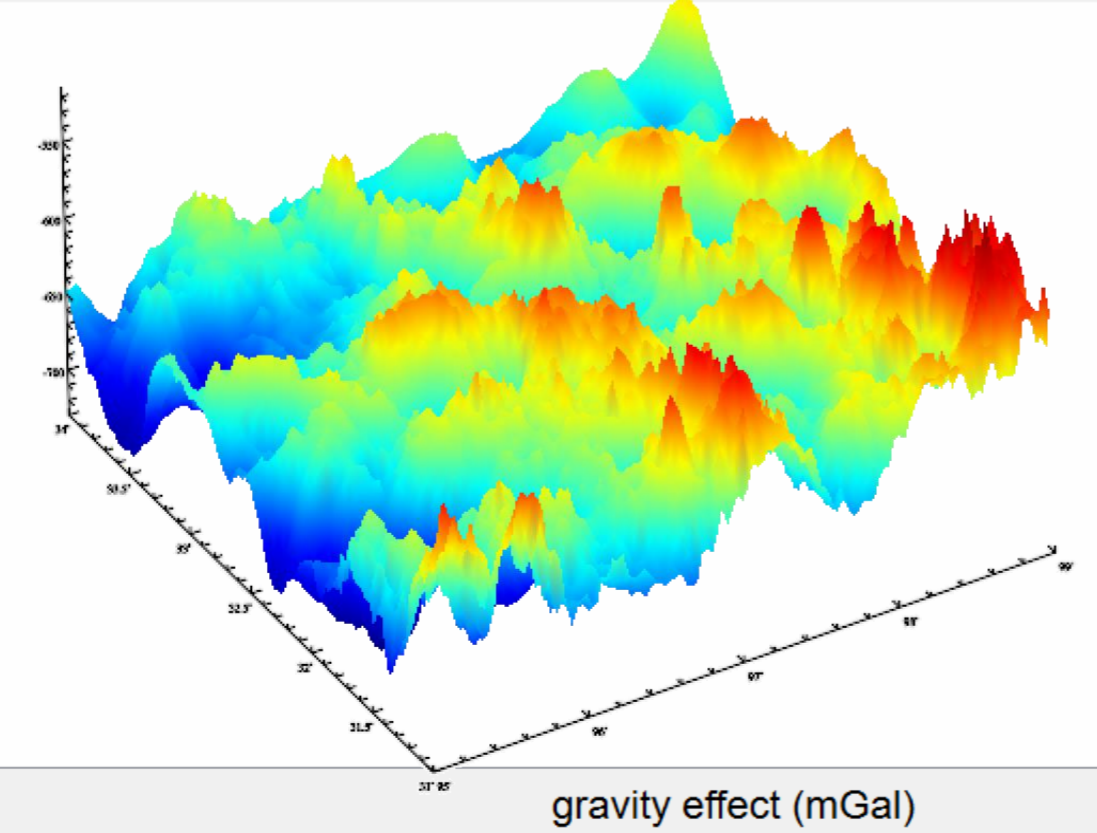
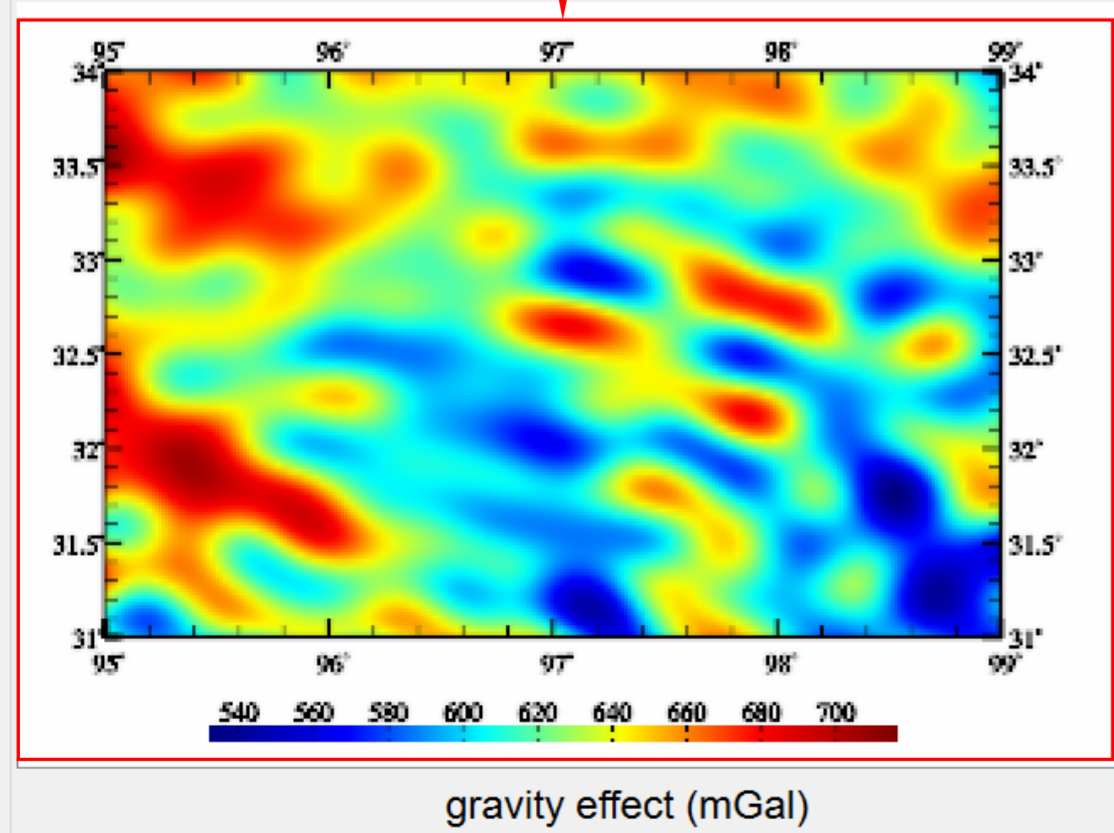
>> The parameter settings have been entered into the system!

\*\* Click the [Start Computation] control button, or the [Start Computation] tool button...

\*\* The calculation process need wait during which you can open the output file to look at the calculation progress

95.000000	99.000000	31.000000	34.000000	0.03333333	0.03333333					
4476.8350	4476.8348	4476.8365	4476.8522	4476.8577	4476.8643	4476.8				
4476.9302	4476.9403	4476.9518	4476.9660	4476.9855	4476.9976	4477.0				
4477.1683	4477.1826	4477.2002	4477.2126	4477.22	4477.22	4477.22				
4477.3383	4477.3369	4477.3402	4477.3426	4477.34	4477.34	4477.34				
4477.3162	4477.3113	4477.3065	4477.3017	4477.29	4477.29	4477.29				
4477.2949	4477.3014	4477.3107	4477.3215	4477.33	4477.33	4477.33				
4477.5921	4477.6261	4477.6627	4477.7016	4477.74	4477.74	4477.74				
4478.2944	4478.3510	4478.4090	4478.4673	4478.52	4478.52	4478.52				

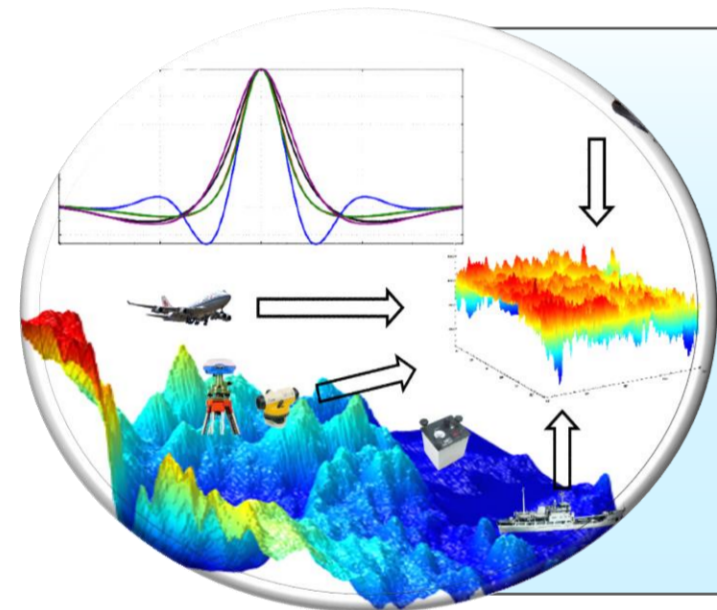
## (7) Generate the 120" complete Bouguer gravity disturbance on the terrain equiheight surface.



The program is suitable for the unified computation of the complete Bouguer and residual terrain effects on various gravity the geoid and its outer Earth space.



# The analytic relations of gravity field as strong constraints



**Computation scheme of gravity prospecting by analytic fusion of heterogeneous observations**

- 🌍 **Observation mode:** Terrestrial, marine, aviation, altimeter and satellite.
- 🌍 **Observations:** Gravity, gravity gradient, vertical deflection, and GNSS-leveling etc.
- 🌍 **Target type:** Gravity anomaly, gravity gradient, and vertical deflection etc.

# Computation theory of gravity prospecting by analytic fusion of heterogeneous observations by PAGravf4.5



Computation of various terrain effects on various field elements outside geoid

<b>Computation of local terrain effect on various field elements outside the geoid</b>	<b>Integral of land, ocean and lake complete Bouguer effect on gravity outside geoid</b>	<b>Computation of terrain Helmholtz condensation effect on various field elements outside geoid</b>	<b>Computation of residual terrain effect on various field elements outside geoid</b>
<b>Computation of land-sea unified classical gravity Bouguer / equilibrium effect</b>	<b>Ultrahigh degree spherical harmonic analysis on land-sea terrain and construction of model</b>	<b>Spherical harmonic synthesis of complete Bouguer or residual terrain effects</b>	<b>Computation process demo of complete Bouguer anomaly outside geoid</b>
			<b>Computation process demo of various terrain effects outside geoid</b>

Programs and functions structure of the subsystem

Quantitative criterions for terrain effects defined by PAGravf4.5

(1) In order to improve the gridding performance of discrete field elements, it is expected to improve the smoothness of discrete field elements after the terrain effect removed. In this case, the optimal criterion is that the standard deviation of field elements would decrease, and the statistical mean of terrain effects in the range of tens of kilometers is small after the terrain effect removed.

(2) The terrain effect is expected to consist of only ultrashort wave components for gravity field approach purpose, so the optimal criterion is that the standard deviation of field elements would decrease, and the statistical mean of terrain effects in the range of tens of kilometers is small after the terrain effect removed.

(3) When the sizes of several modes of terrain effects are roughly same, the greater the ratio of the standard deviation of terrain effect on gravity disturbance to the standard deviation of terrain effect on gravity disturbance, the more favorable it is for geoid refinement.

(4) When the sizes of several modes of terrain effects are roughly same, the greater the ratio of the standard deviation of terrain effect on gravity disturbance to the standard deviation of terrain effect on gravity disturbance, the more favorable it is for geoid refinement.

Precision approach and full elements modeling of Earth gravity field

<b>External vertical deflection computation using Vening-Meinesz integral</b>	<b>External vertical deflection computation using Vening-Meinesz integral</b>	<b>Inverse integral and integral of inverse operation on anomalous field element</b>	<b>Gradient and Poisson integral computation of external gravity field element</b>
<b>Feature and performance analysis of spherical radial basis functions</b>	<b>Gravity field approach using SRBFs in spectral domain and performance test</b>	<b>Full element modelling on gravity field using SRBFs from heterogeneous observations</b>	<b>Computation process demo of full element modelling on gravity field by integral method</b>
			<b>Simple process demo of full element modelling using SRBFs in orthometric height system</b>
			<b>Simple process demo of full element modelling using SRBFs in normal height system</b>
			<b>Modeling process exercise of regional gravity field and geoid</b>

The high-precision analytical computation abilities of various terrain effects on any type of gravity field element.

The full-element analytic functions on gravity field from various heterogeneous observations.

The computation of fine gravity prospecting that can deeply fuse all the gravity field information in multi-source heterogeneous observations in any complex cases with the analytic relations of gravity field as strong constraints.

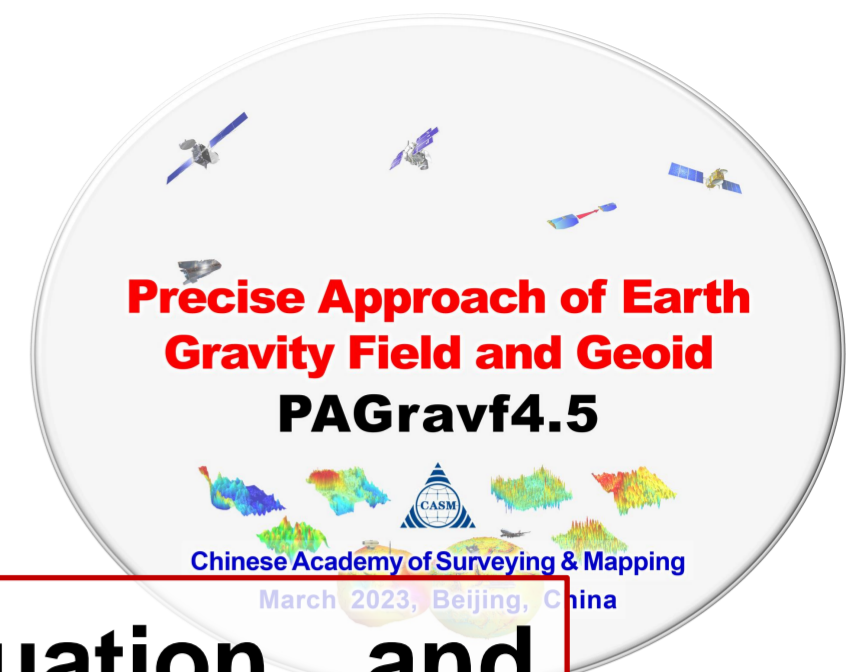
# **The general computation process for the fine gravity prospecting model from heterogeneous observations by PAggravf4.5**



- ☆ **Select the calculation area, target calculation surface (terrain equiheight surface is recommended here) for gravity exploration and obtain (or collect) all the gravity field and geodetic observations as much as possible.**
- ☆ **Call the related programs in the subsystem [Precision approach and full element modelling on Earth gravity field] to determine the high-resolution grid of gravity field element corresponding to the target prospecting model on the calculation surface.**
- ☆ **Call the related programs in the subsystem [Computation of various terrain effects on various field elements outside geoid] to determine the terrain effect grid on gravity field element corresponding to the target prospecting model on the calculation surface.**
- ☆ **By subtracting the terrain effect grid from the gravity field element grid directly, you can obtain the target gravity prospecting model which have deeply fuse all the gravity field information in heterogeneous observations.**



# Solve a series of bottleneck problems to achieve a comprehensive technical breakthrough



**No direct reduction and continuation**

**Control signal attenuation and algorithm inaccurate**

**No non-analytical gridding required**

**Solve the problems for gravity field distortion and terrain effect difficult to control**

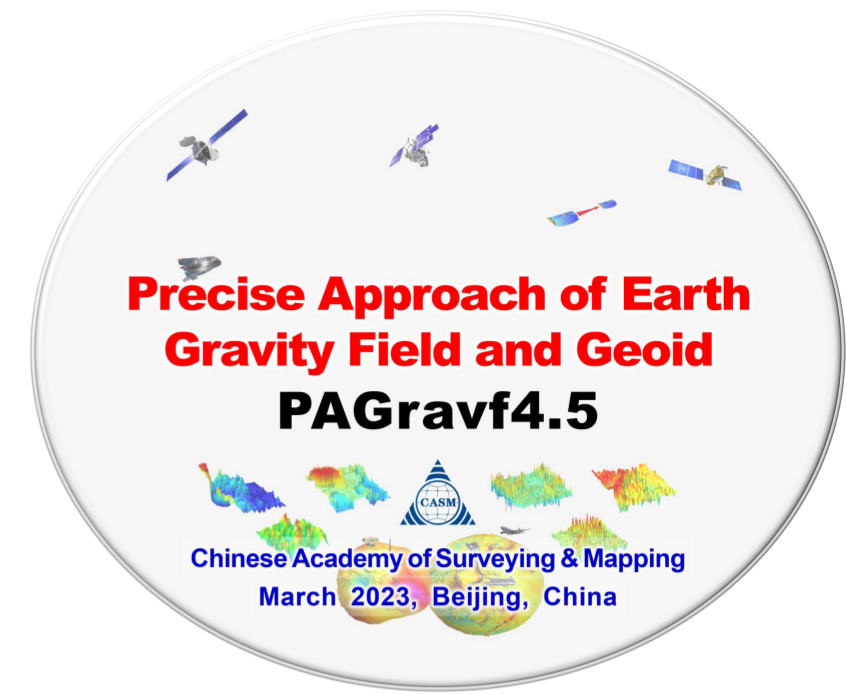
**One step of direct and analytical modeling from various heterogeneous observations**

**Achieve the major breakthrough in gravity exploration from single type of observation to multi-source heterogeneous observations.**

**Analytically fuse all the gravity field signal in in any complex cases**

**The full-element analytical modeling of gravity prospecting such as complete Bouguer gravity gradient and vertical deflection etc.**

**Significantly improve the fine characteristics detection of gravity field for gravity exploration.**



# **Theoretical basis and support technology**

**External terrain effect +  
Approach of gravity field**

**More innovation and application potential need to be discovered and excavated in the future computing practice !**